



**LVX**  
**VERITAS**  
**VIRTVS**



# Role of Artificial Intelligence in Nanomanufacturing

## Photolithography and Plasma Etch

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# Acknowledgment



- Amit Lal and SonicMEMS team, ECE, Cornell
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- Chris Ober, CNF technical staff members (Garry Bordonaro, Vince Genova, Jeremy Clark and John Treichler)
- Hitachi HTA (Marco Hauser, Steve Ayres)

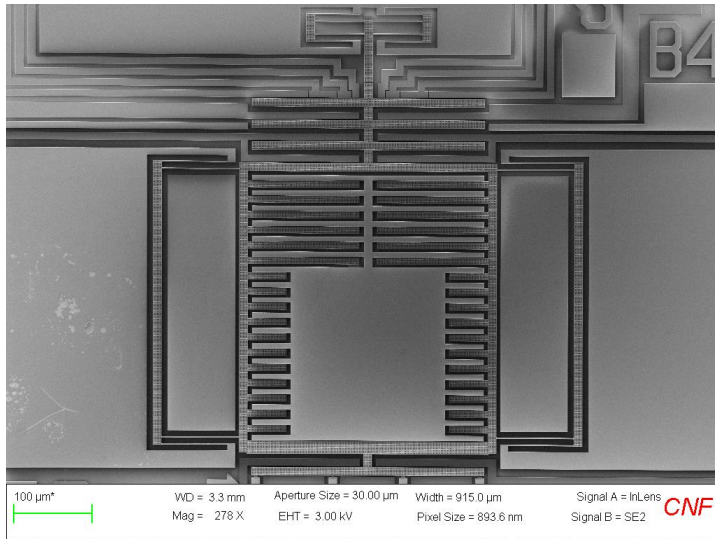
## **Supporting programs:**

- DARPA PAI program
- SEMI-FlexTech/ARL
- DARPA NZERO program

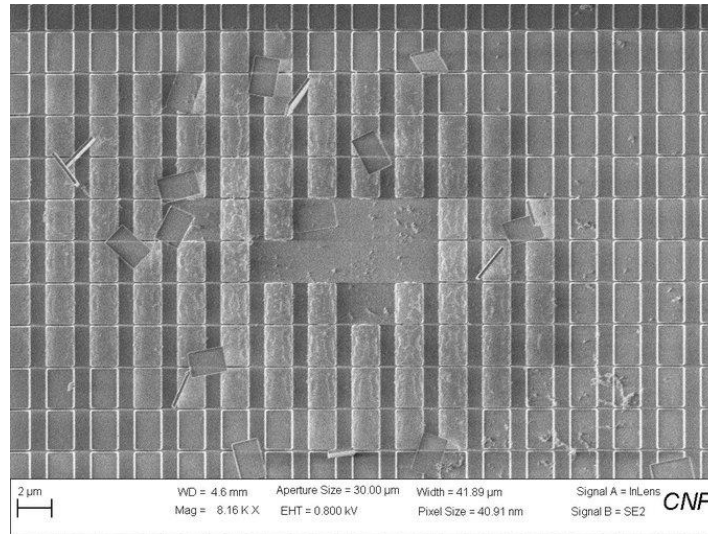
## **CNF facility:**

This work was performed in part at the Cornell NanoScale Facility, an NNCI member supported by NSF Grant NNCI-2025233.

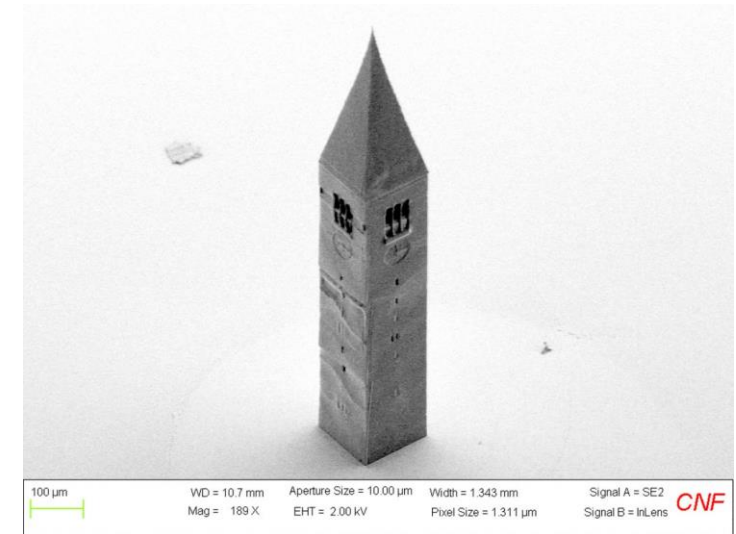
# You can build *anything* at Nanofab .....CNF!



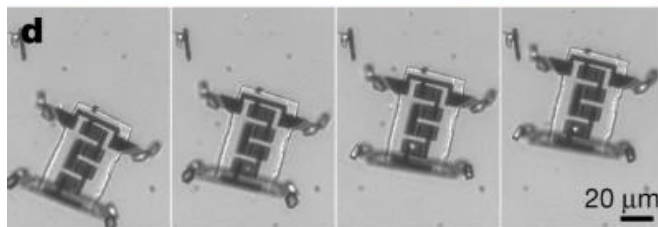
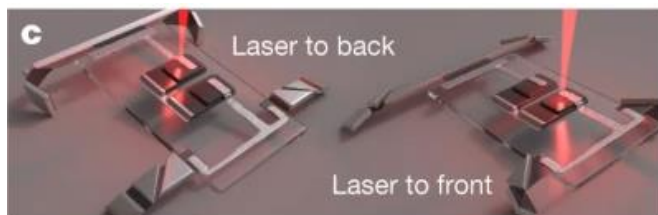
SonicMEMS, 2019



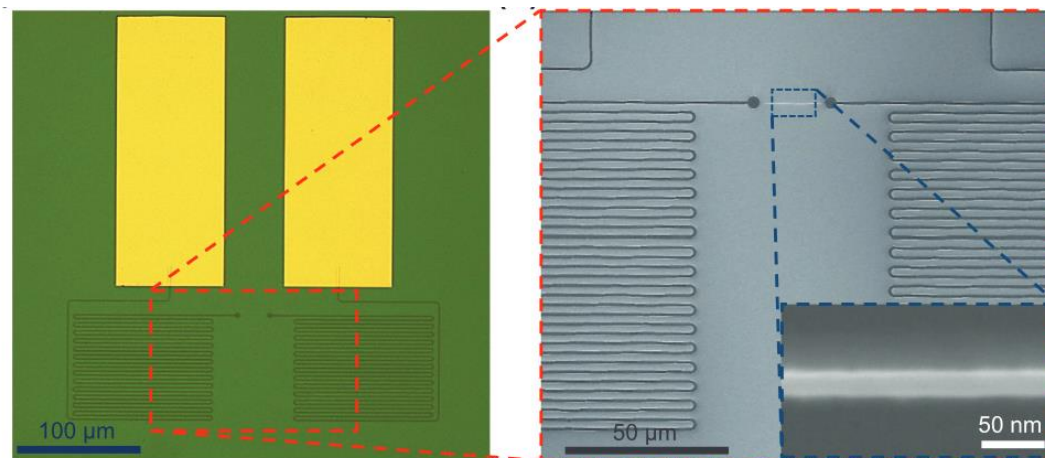
Shvets group, 2021



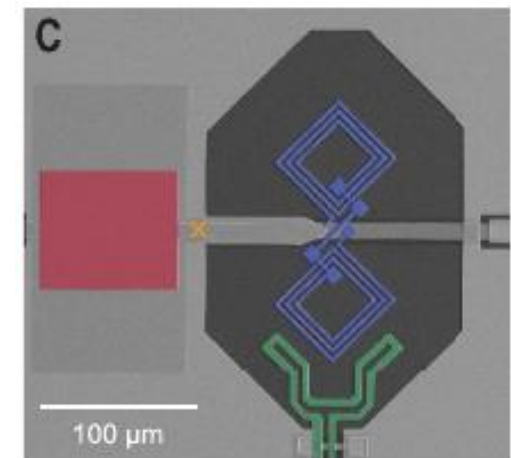
CNF, 2021



McEuen/Cohen groups, 2020



Jenna-Xing groups, 2020

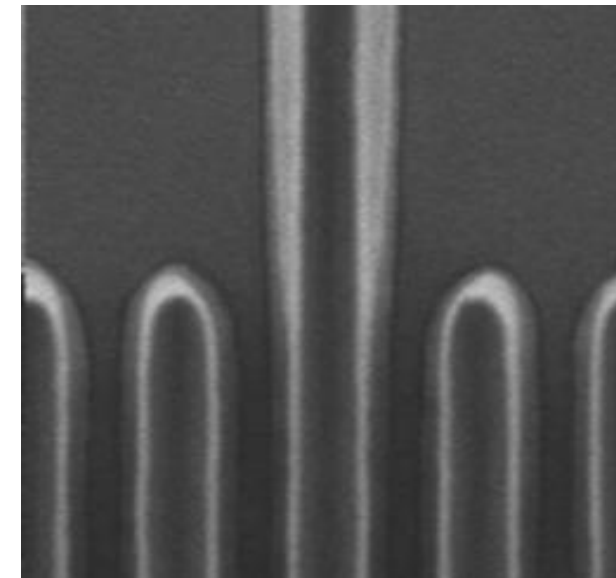
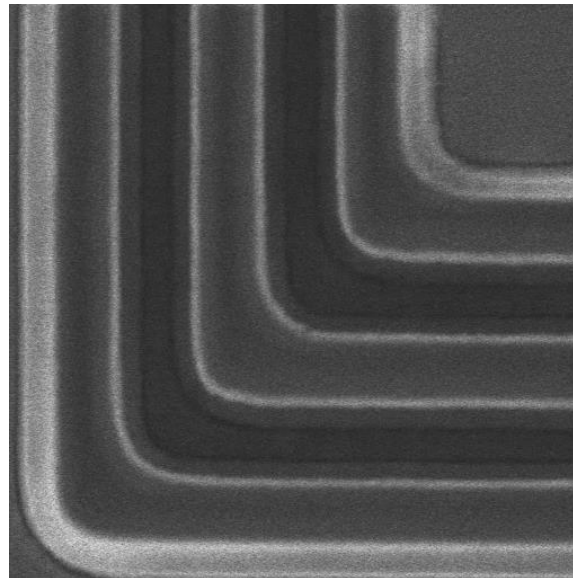
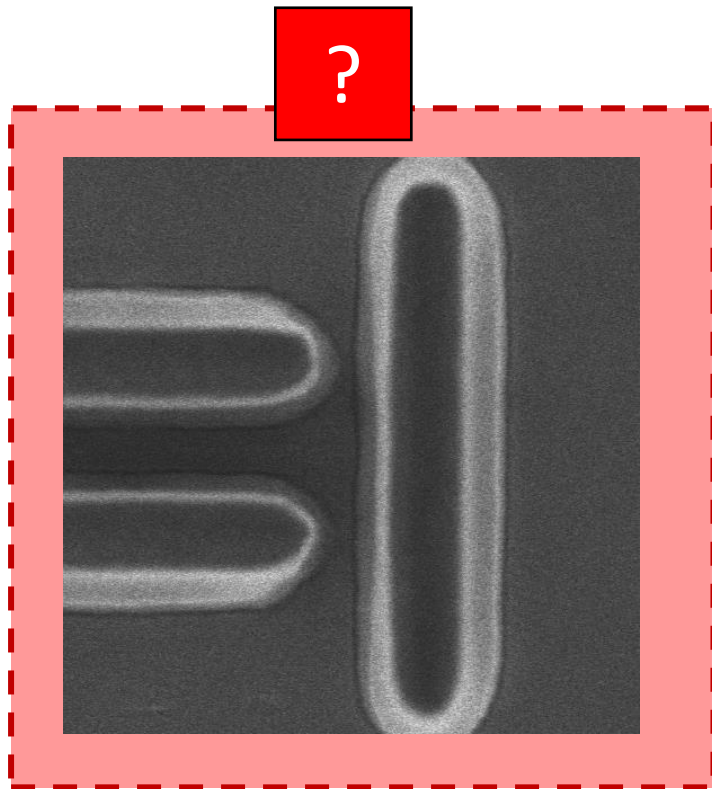


Plourde group, 2018

# Which image is a real SEM?



Process: (HBr+Ar) ICP-etched Si nanostructures, with UV210 resist mask.



These are all AI predictions!

SEM images shows a 2 x 2 um.

[SEMI master class #6, 2021]

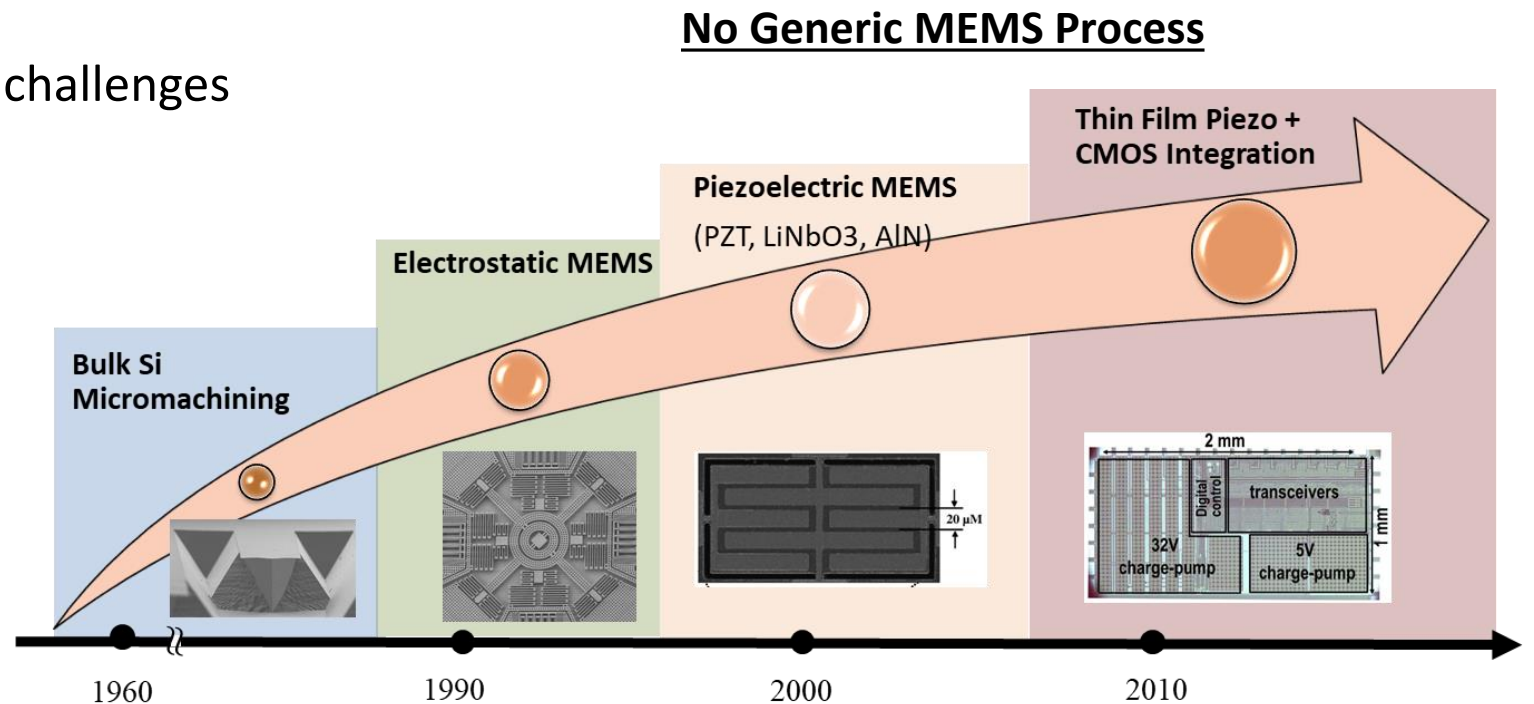
- ML and AI have made a lot of progress in recent years due to **algorithmic advances and large datasets** all enabled by **computational resources** (e.g., HPC, GPUs, TPUs ...)
- Example areas where AI already has impact includes: **E-commerce, face recognition** and **autonomous vehicles**
- AI and ML is being used in **material science**
- AI is being used to enhance the **computation** and **pattern recognition** efficiency on the data collected by micro and nanosystems (e.g, **IoT, edge devices**)
- But application of AI to **micro and nanofabrication** and **device design** is in its infancy

# Can AI/ML solve nanofabrication challenges?



## Nanodevices design and manufacturing challenges:

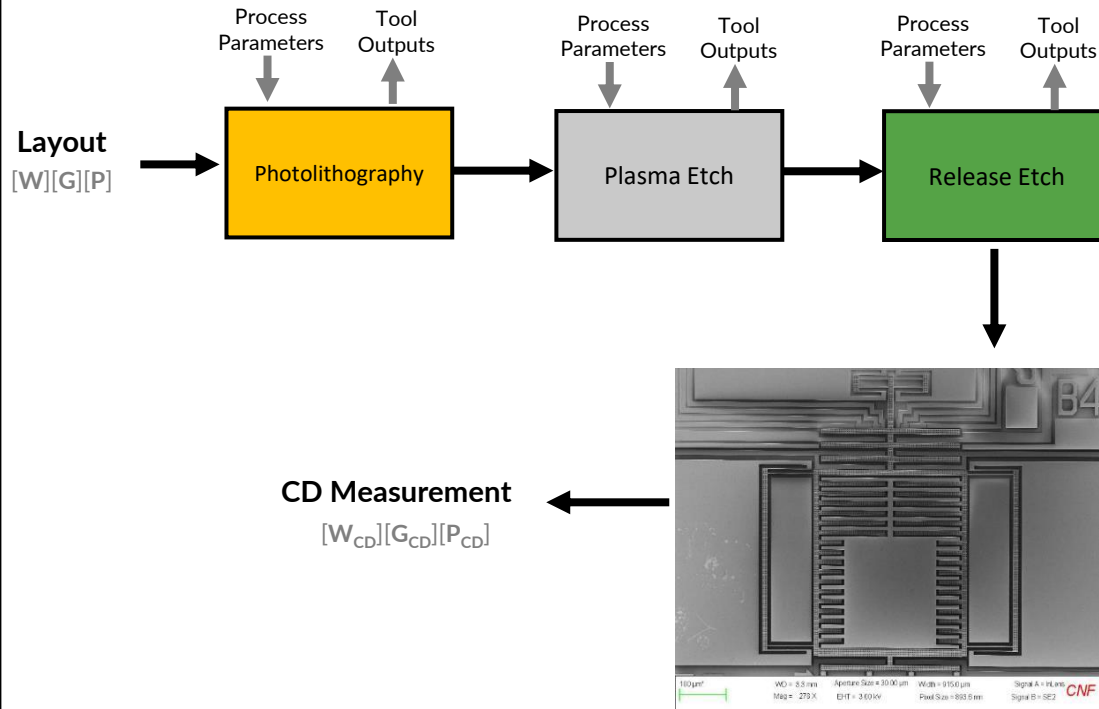
- Excessive effort and time for new device development
- Lack of standard/generic processes
- Novel materials and process development challenges
- Lack of process connection with CAD tools
- Growing demand for integration
- Multiple foundry implementation challenges



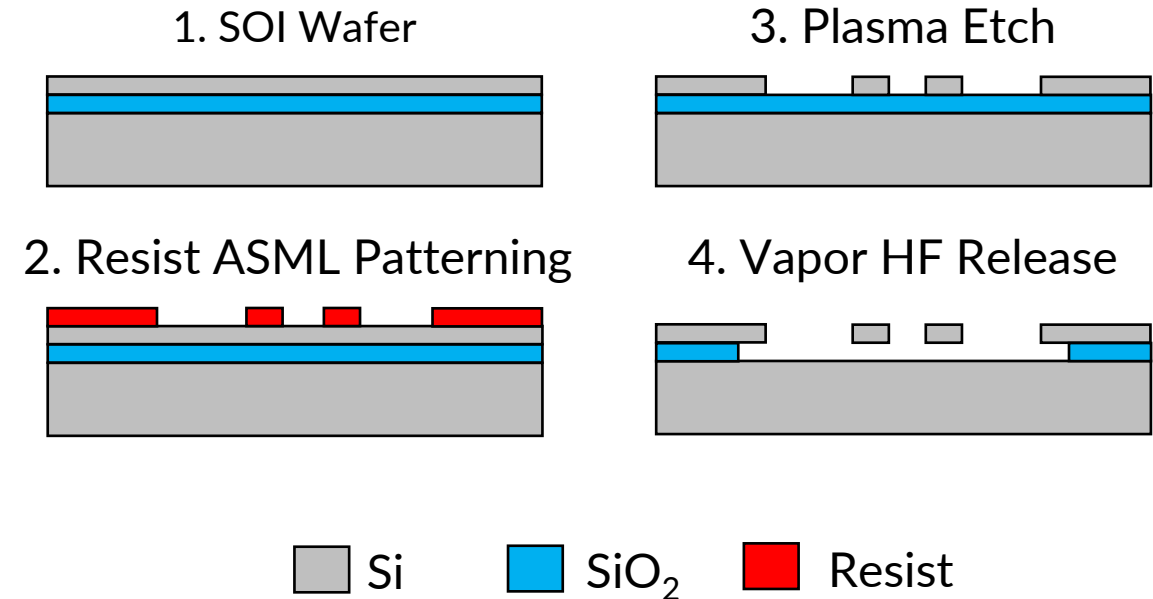
# Example: Si NEMS switch fabrication



## NEMS processing sequence



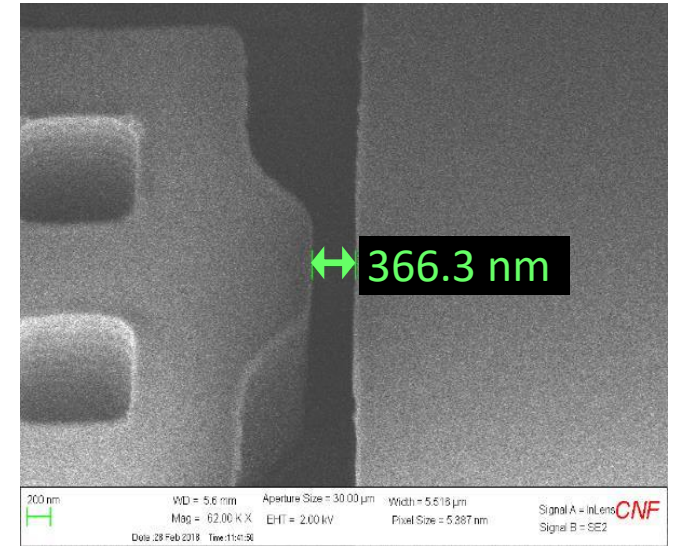
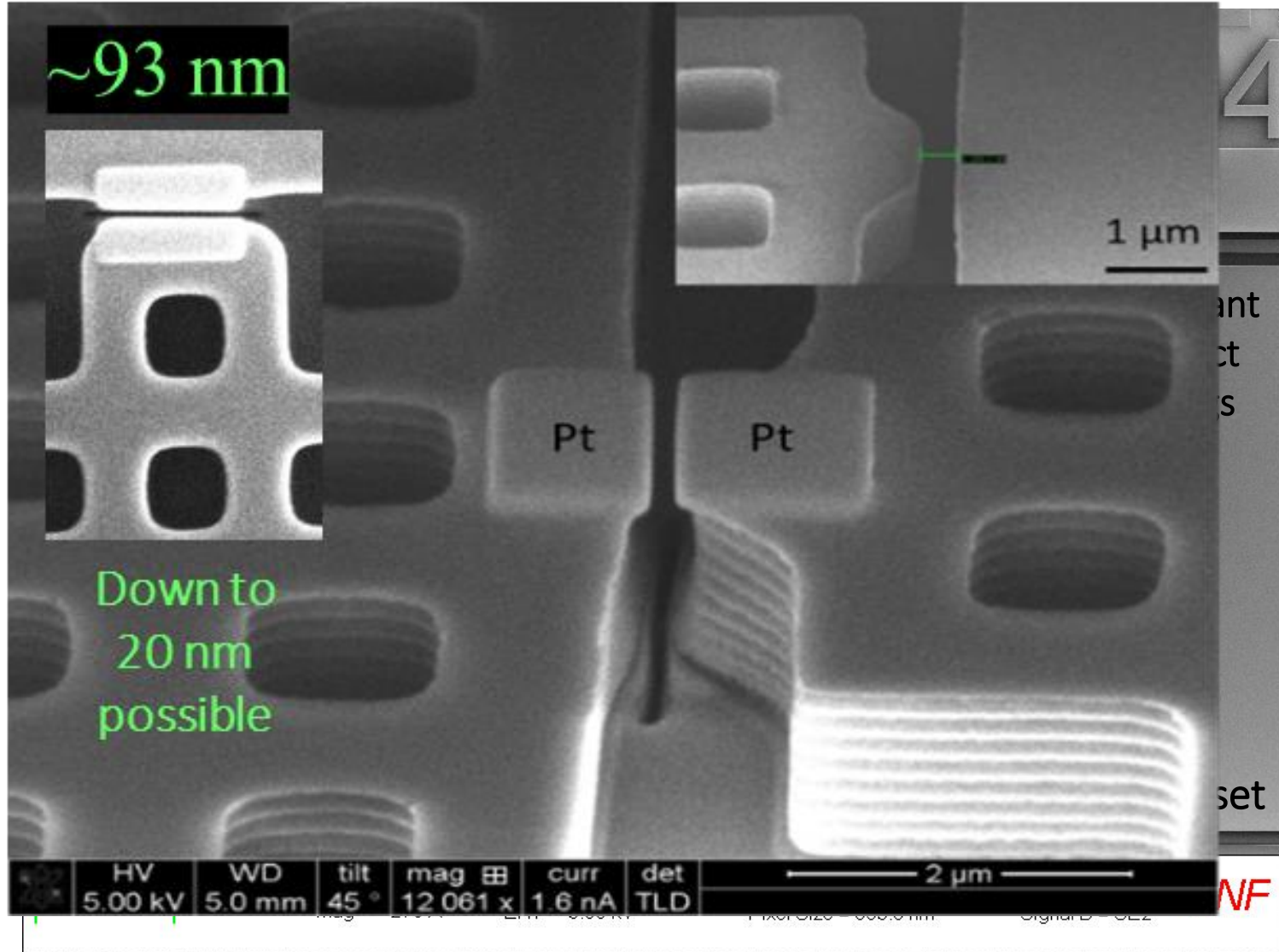
## Cross sections of wafer



[Ruyack, 2018]

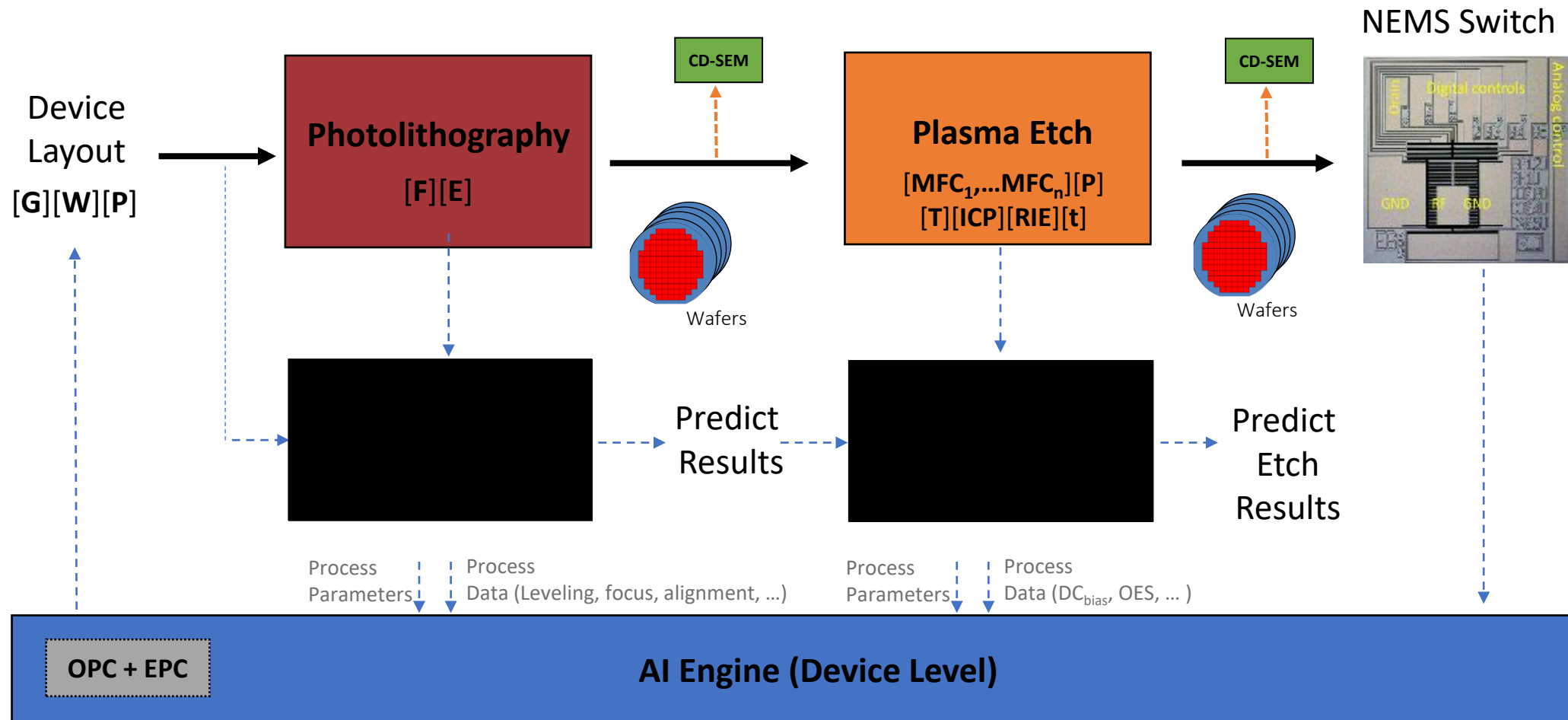


# NEMS radio switch



[Ruyack, 2018]

# Learning outcome of nanofabrication

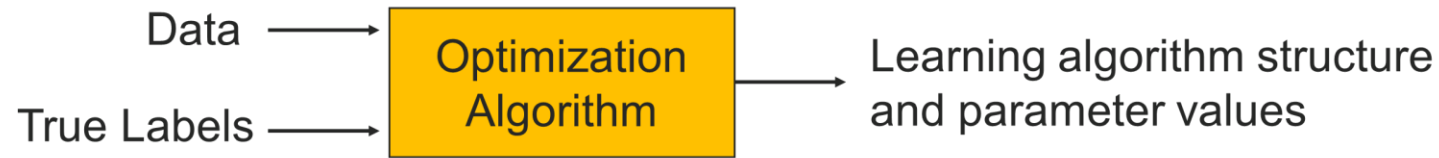


# Machine learning = Learning from examples

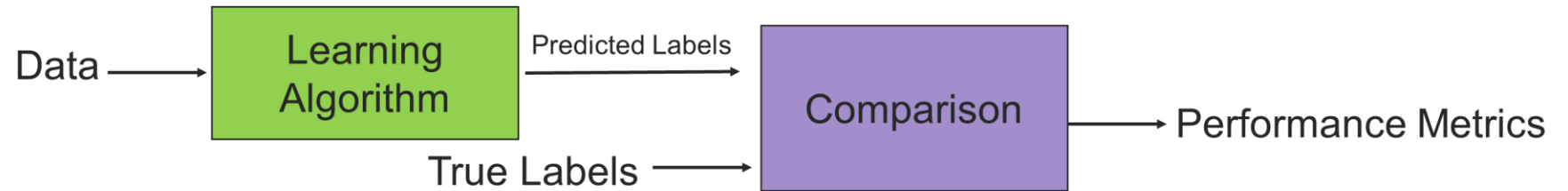


## Three Phases:

### 1. Train:



### 2. Test:



### 3. Use:

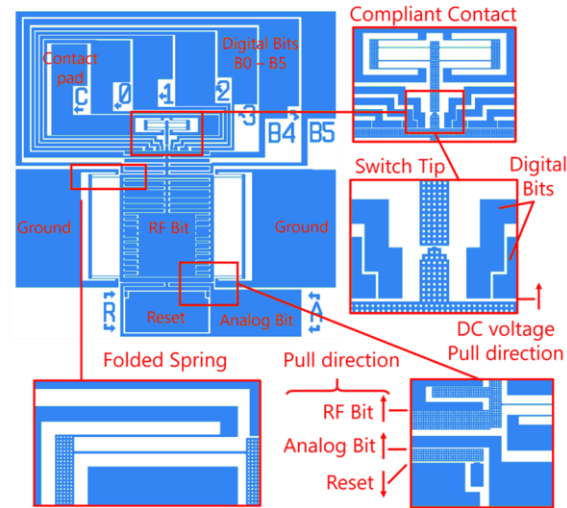
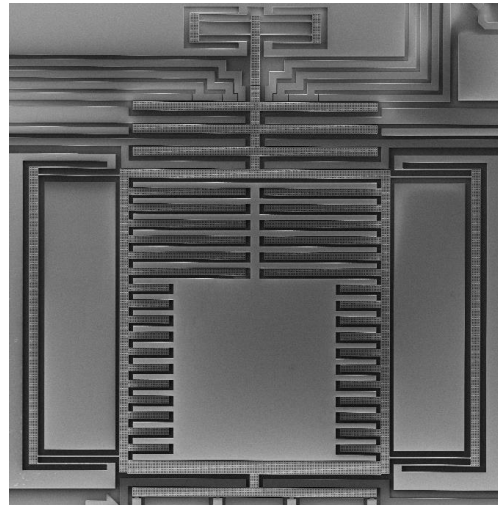


- The Learning Algorithm approximates the unknown function that maps **Data** to **Labels**.
- Accurate **True Labels** are important! Otherwise, the Learning Algorithm is trying to find a mapping of "one" to "many".
- **Example data** must match eventual **Use data**! ("transfer learning")

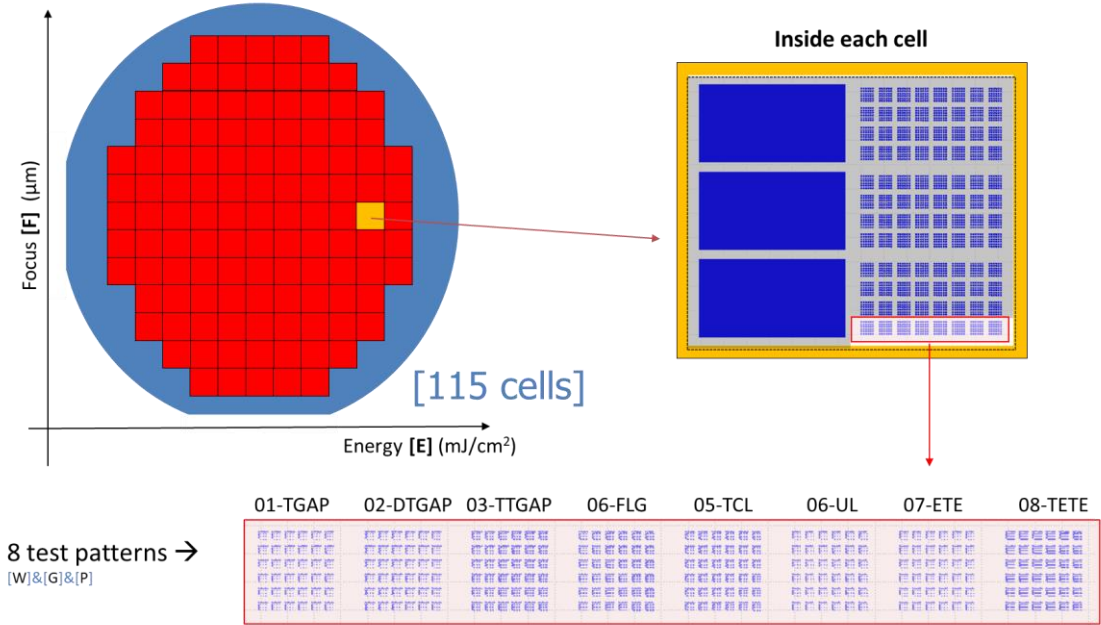
# Training dataset motivated by NEMS switch



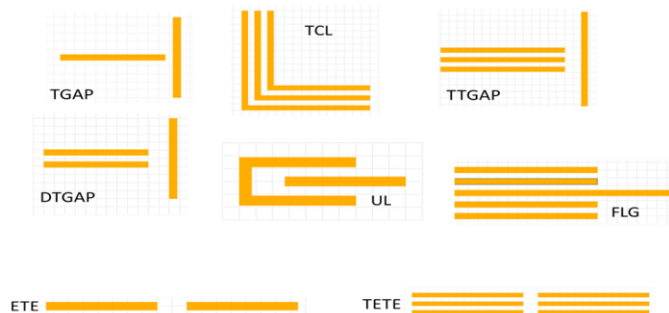
## NEMS RF switch layout:



## Wafer layout:



## Fragments of mask layout:



8 test patterns →  
[W]&[G]&[P]

### Structures on the PAI Wafer:

$$115 \times 8 \times 4 \times 2 \times 6 \times 6 \times 18 = 4,769,280$$

$$[\text{cell}] \times [\text{L}] \times [\text{P}] \times [\text{Po}] \times [\text{W}] \times [\text{G}] \times [\text{rep.}]$$

### Measured CD-SEMs for PAI program:

$$115 \times 8 \times 1 \times 1 \times 6 \times 6 \times 1 = 33,120$$

[L]: layout pattern (8 patterns)  
[P]: pitch (line/space ratio: 1,1.25,1.5&2)  
[Po]: polarity of patterns (positive and inverted)  
[W]: width of lines (150-400 nm)  
[G]: gap size (150 - 400 nm)  
[rep.]: number of repeated structures (3x9)

[SEMI master class #6, 2021]

# Nanofabrication Tools Used for NEMS Switch



## SUSS – Gamma Cluster



SussTec Gamma Photoresist Cluster  
Automated Spin-coater  
Automated Develop (Spray/Stream)  
Multiple Proximity Hot Plates and Chill Plate  
Genmark Robotic Wafer Handling  
Alta Spray Coating Module  
200mm – 100mm Wafer Capability

## ASML – DUV Stepper



ASML PAS 5500/300C  
248nm DUV  
0.63-0.40 Variable NA  
AERIAL Illuminator  
3D-Align Back Side  
Alignment  
200mm - 3" Capability

## Oxford-ICP Etcher



Oxford ICP Cobra Etcher  
Automatic Process Log Transfer  
Multiple viewports for spatial variability  
(RP Camera Installed)  
Optical Emission Spectroscopy (OES) for  
plasma species variability  
100 mm Capability

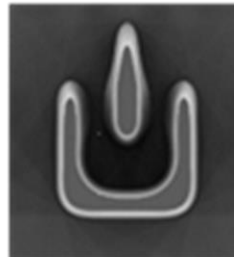
# CD-SEM Images and Preprocessing



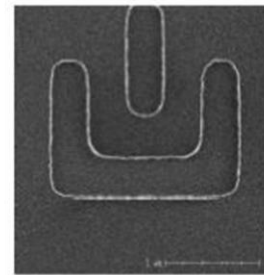
**Mask layout**



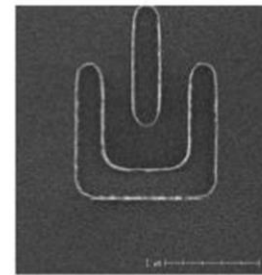
**Physics-based model**



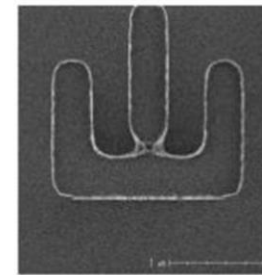
**Photoresist pattern on wafer (CD-SEM)**



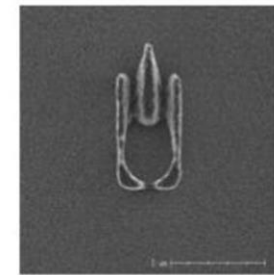
Success



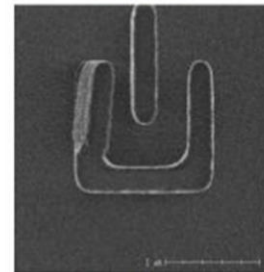
Success



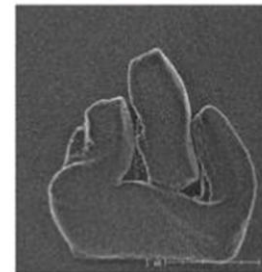
Connection



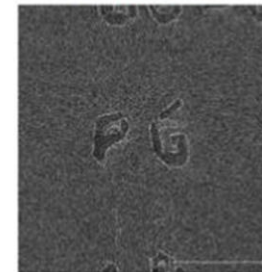
Broken



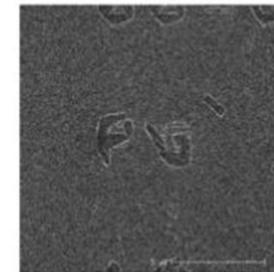
Collapse



Collapse



Text not device

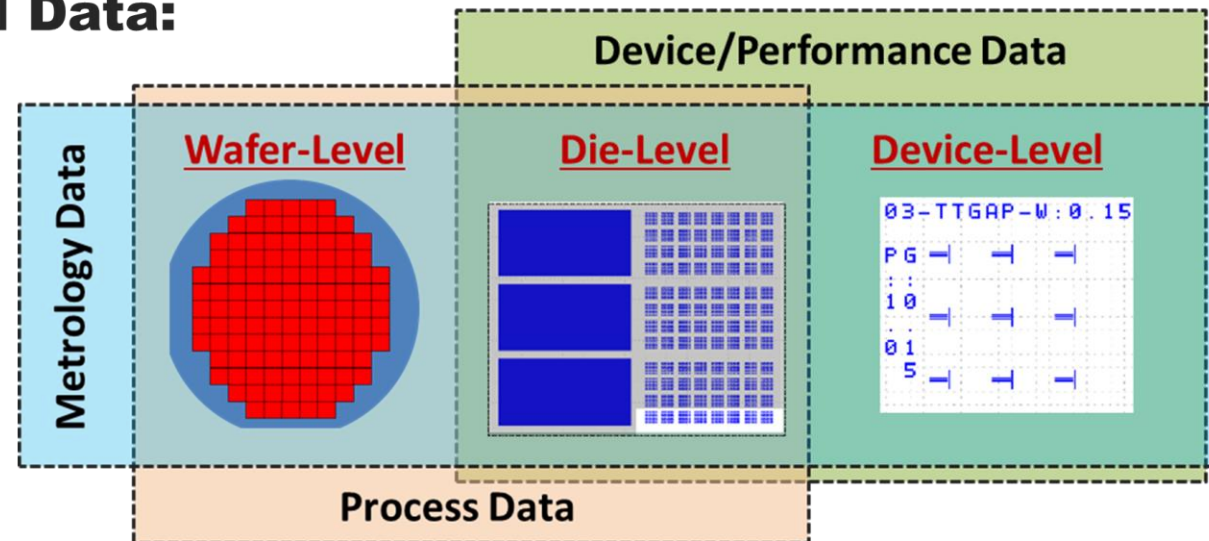


Text not device

# Data Format & Dimensionality

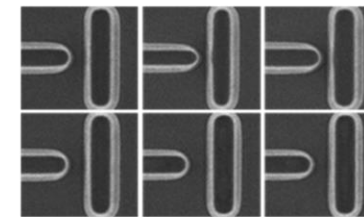
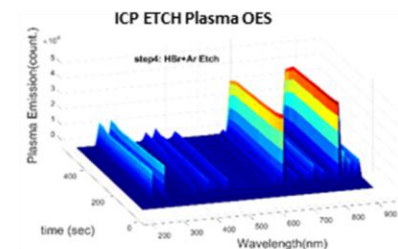


## Multi-dimensional Data:



## Multi-format Data:

HBr-PR Etch DOE				
Run	RIE(W)	ICP (W)	Pre (m Torr)	Ar (sccm)
0	20	1500	5	4
1	20	1500	5	4
2	20	1700	8	7
3	20	1900	11	10
4	30	1500	11	7
5	30	1700	5	10
6	30	1900	8	4
7	40	1500	8	10
8	40	1700	11	4
9	40	1900	8	7



Numerical

Structured Text

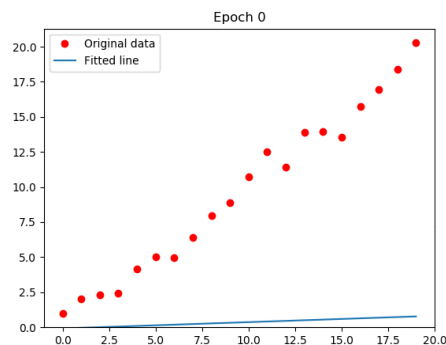
Time Series

Images(2D data)

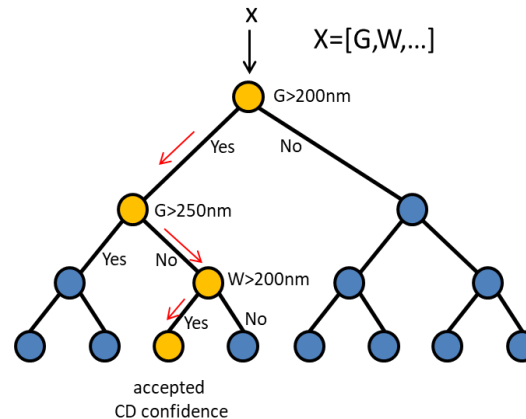
# (1) Feature-based ML approaches



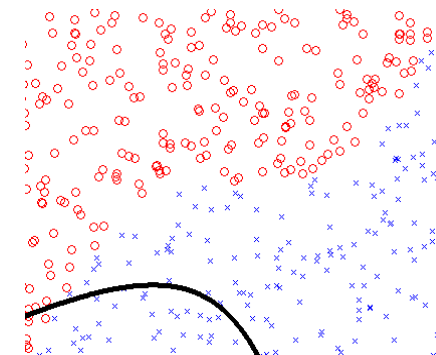
## Linear Models



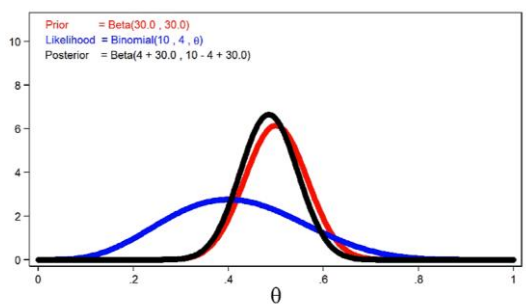
## Decision Trees



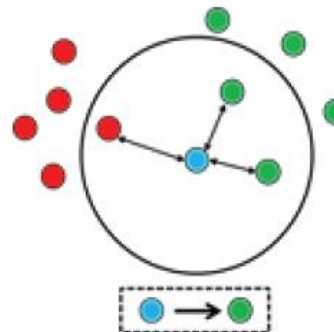
## Support Vector Machines



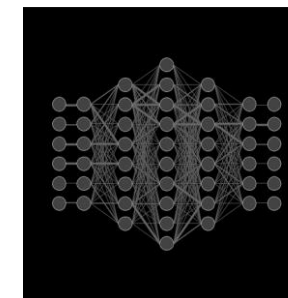
## Naïve Bayesian Classification



## K-nearest Neighbor



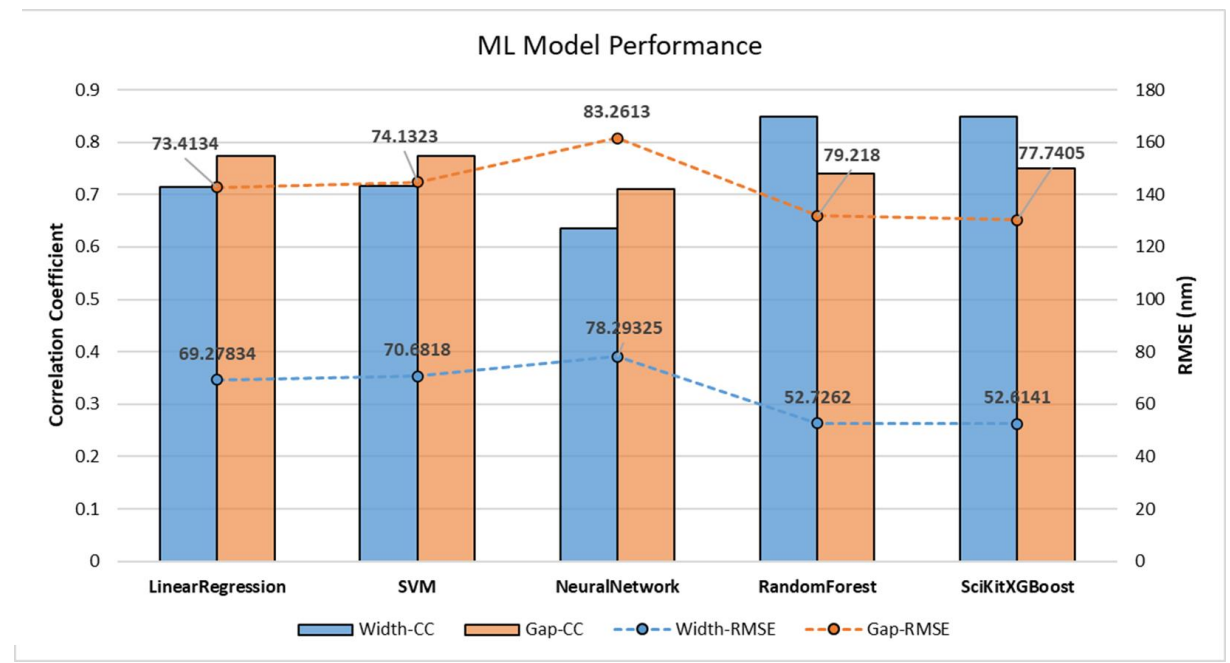
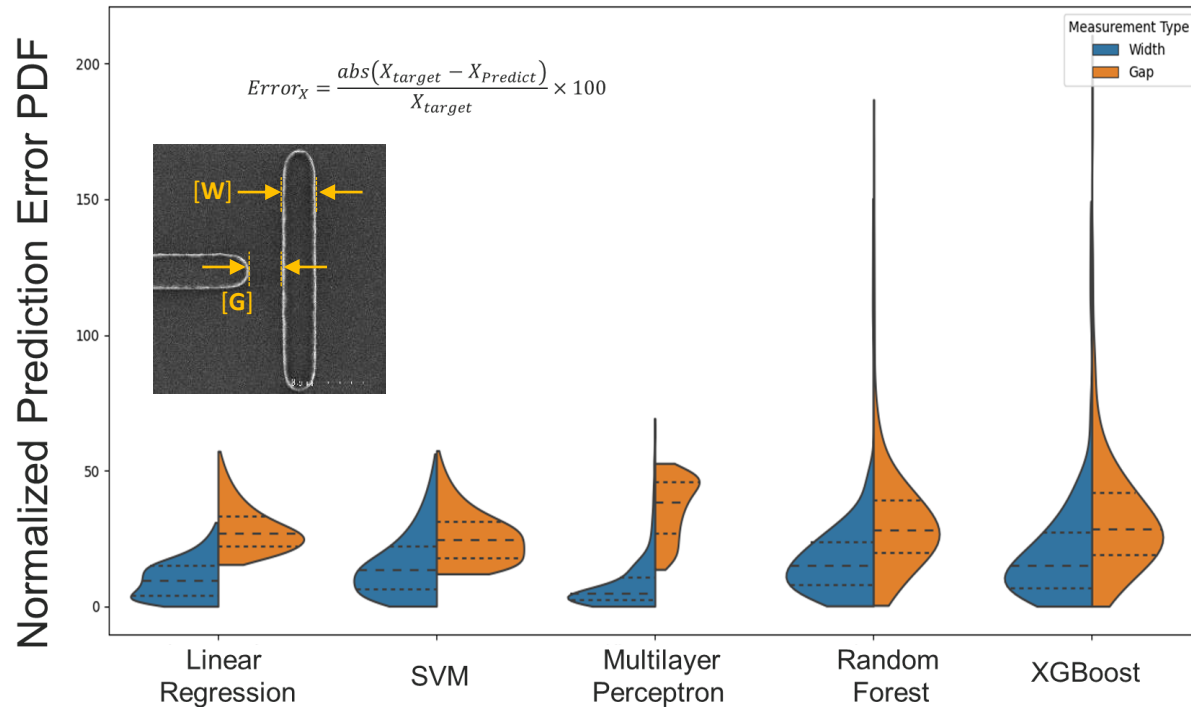
## Neural Networks



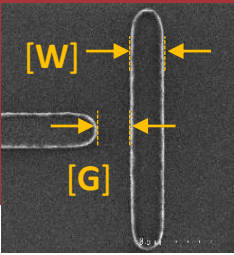
[SEMI master class #6, 2021]



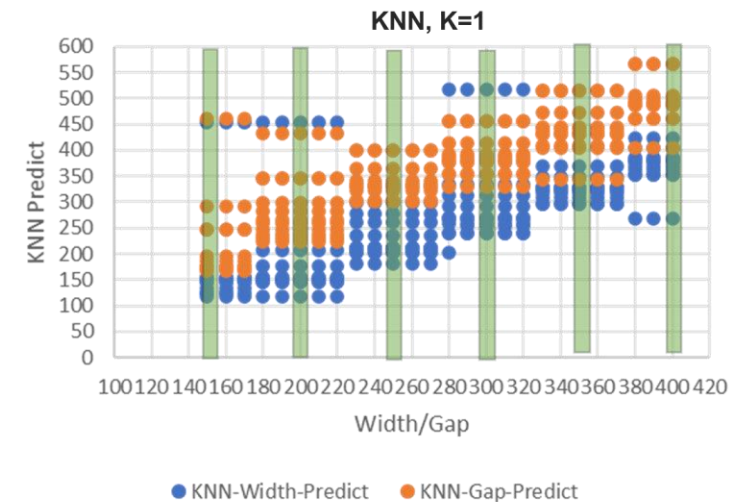
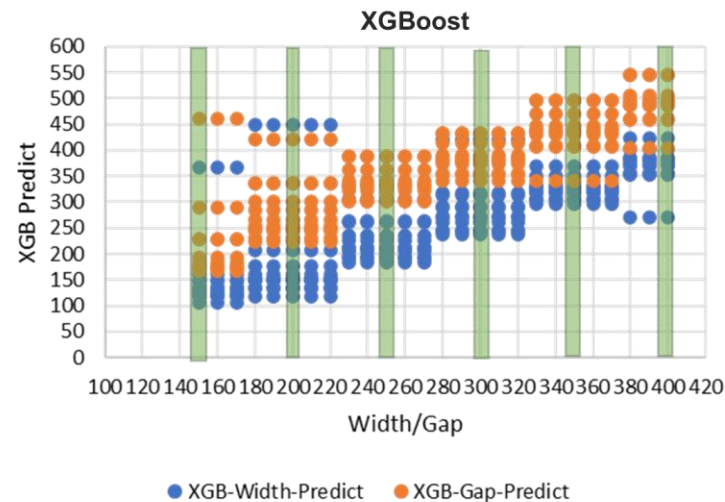
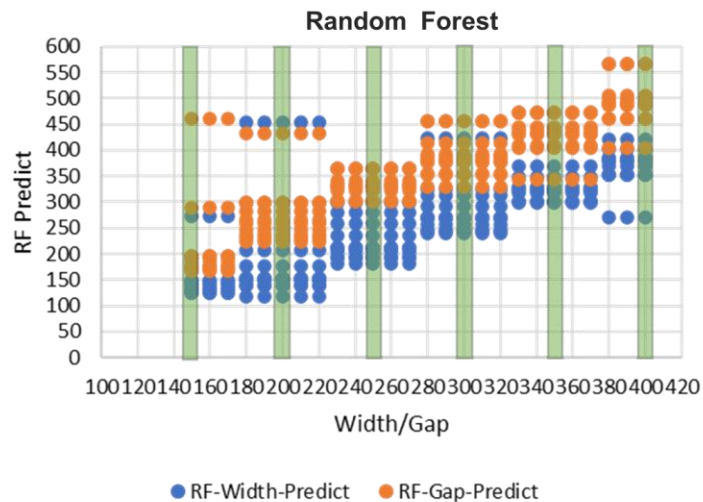
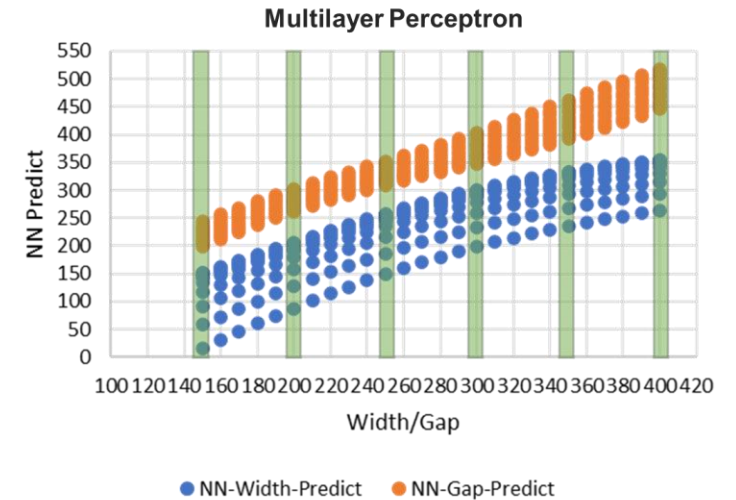
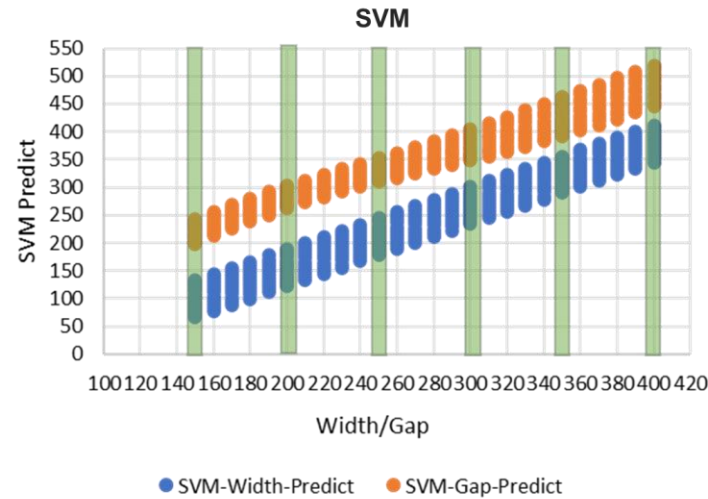
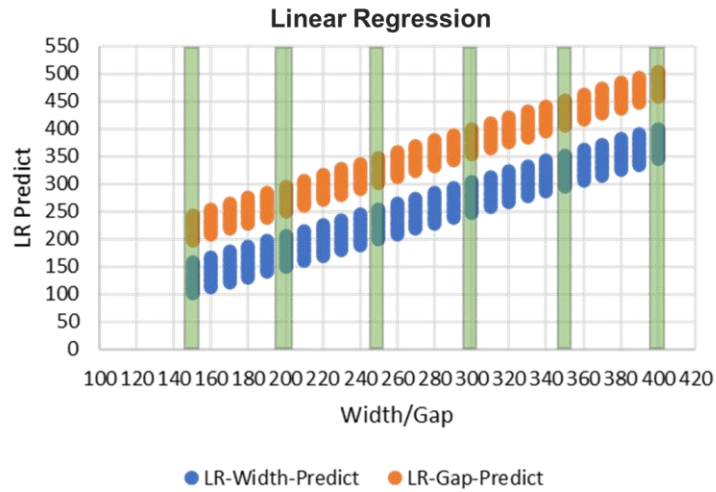
# ML based regression applied to design



# ML for design: width & gap interpolation



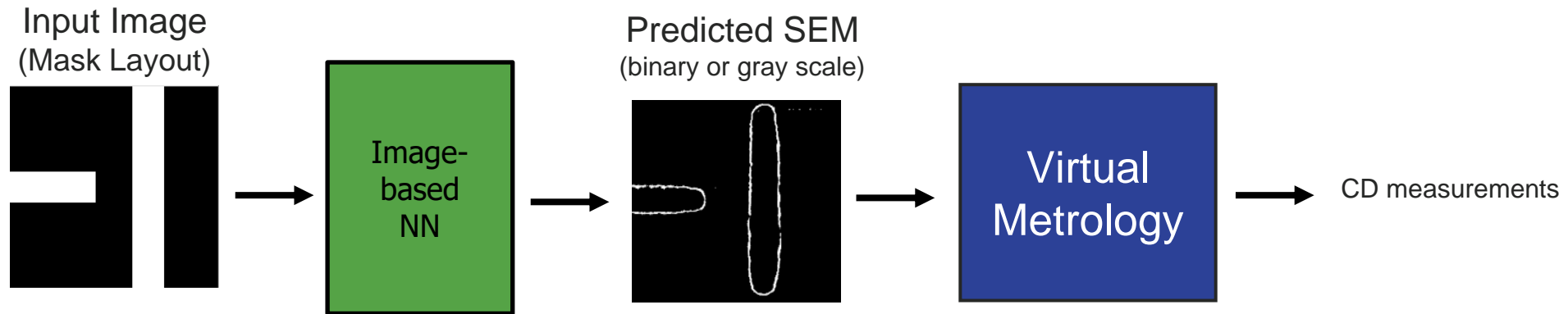
Green=Training data



# (2) Deep learning for image-to-image translation



## Overall Plan:



## One approach: Pix2Pix method for image-to-image translation:



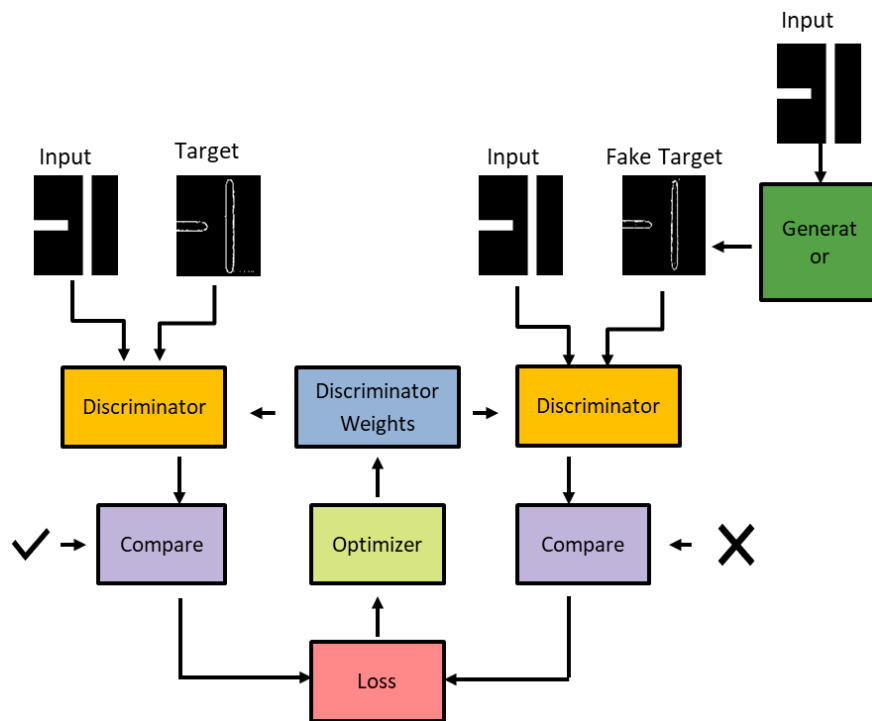
## Summary of Pix2Pix method:

- Conditional Generative Adversarial Network (cGAN)
- Two main parts:
  - **Discriminator:** measures the similarity of the input image with an unknown image (either comes from the real target image or the output image from the generator) and guess if this unknown image is produced by the generator
  - **Generator:** predict the output image from the input image
  - In **use mode** we only use the generator.

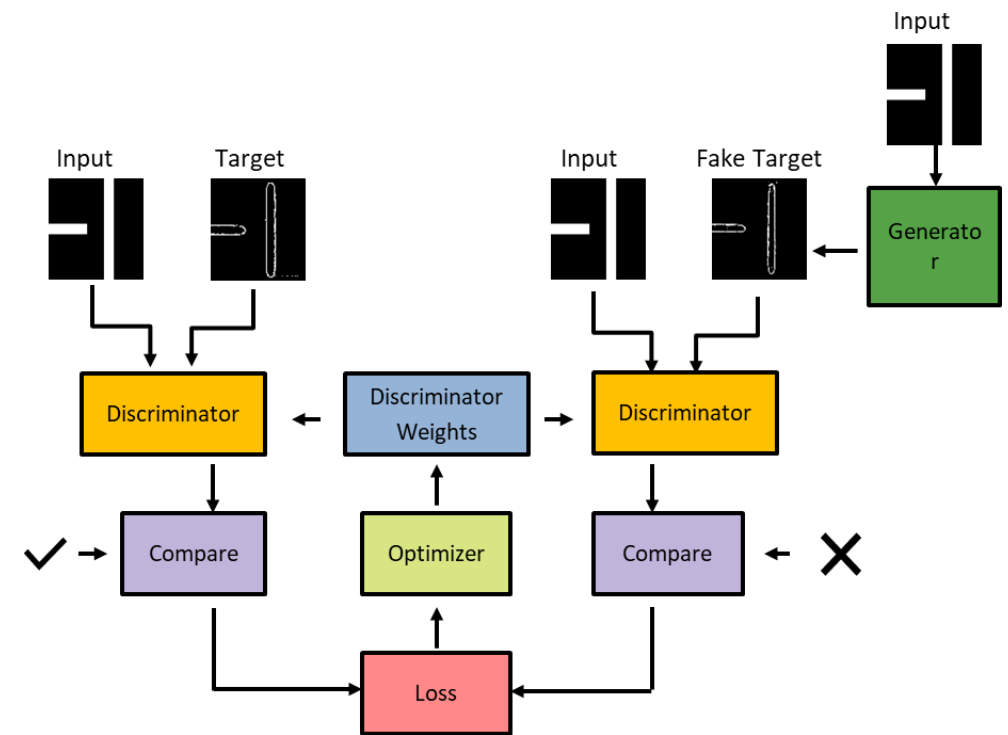
# Pix2Pix Training: Generator and Discriminator



## Generator Training



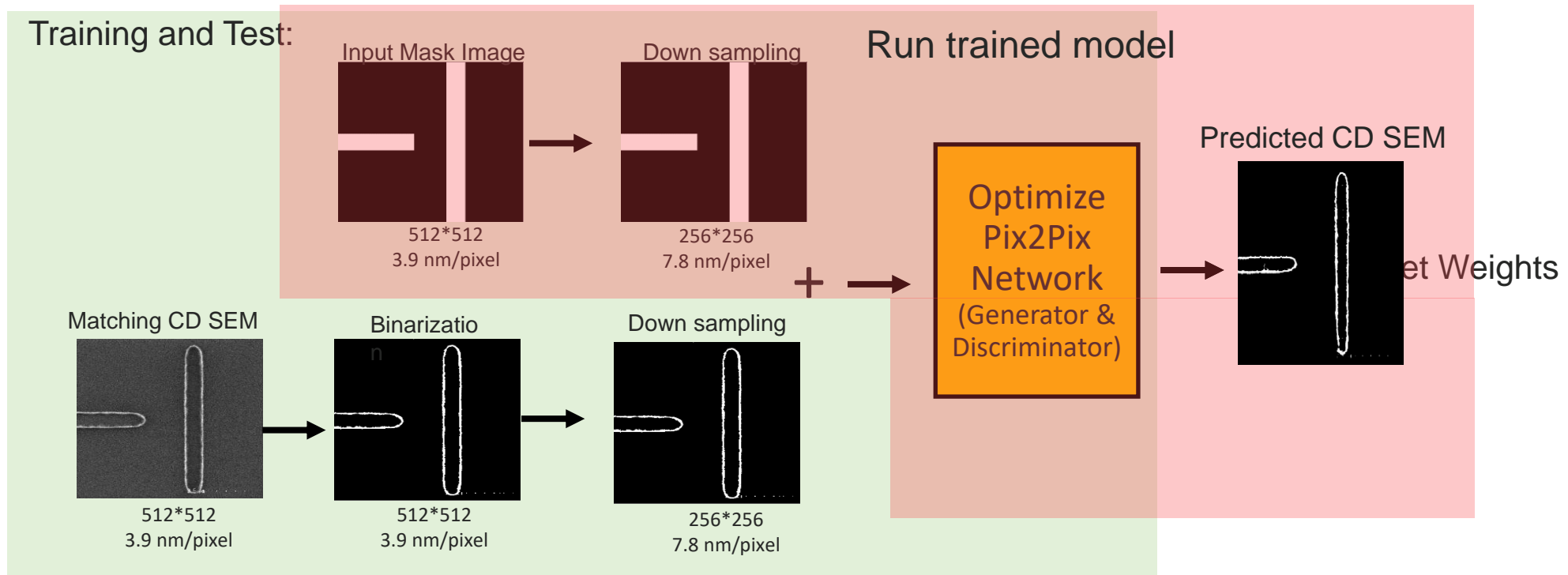
## Discriminator Training



Ref: [arXiv, 1611.07004]

[MEMS 2022]

# Pix2Pix Method: Training & Testing versus Using



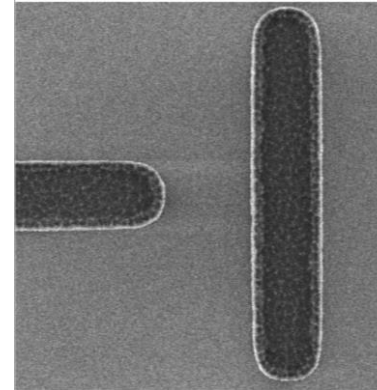
# Learning process outcomes and prediction by Pix2Pix



### DUV Lithography Process



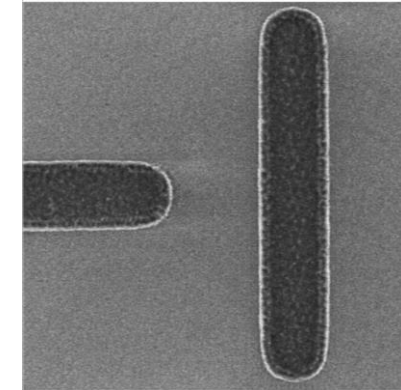
**Mask Layout**  
Binary



**Resist Profile**  
UV 210- 500nm

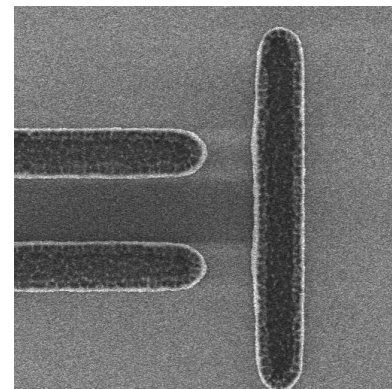


Pix2Pix  
Prediction

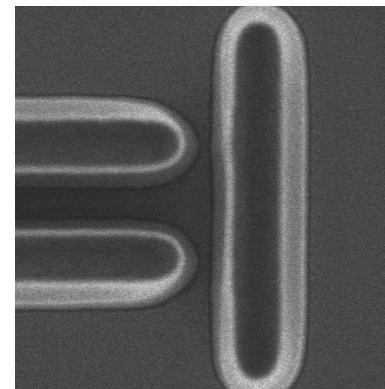


**Prediction**  
Synthesized SEM

### ICP Plasma Etch



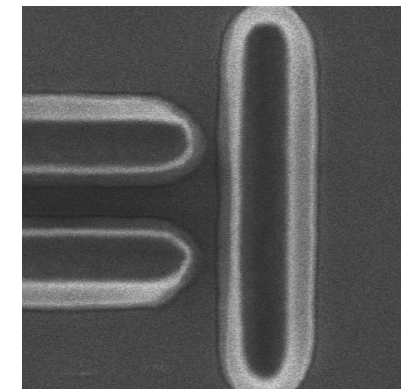
**Pre-Etch**  
Resist Profile



**Post-Etch**  
Si Profile



Pix2Pix  
Prediction



**Prediction**  
Synthesized SEM

SEM images shows a 2 x 2 um area.

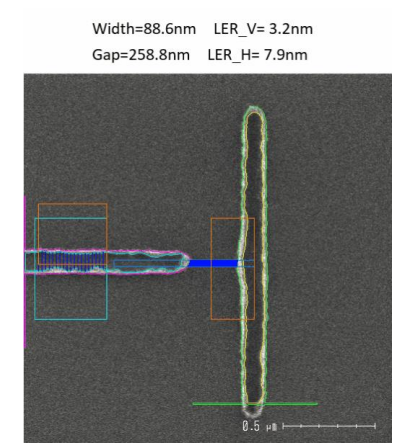
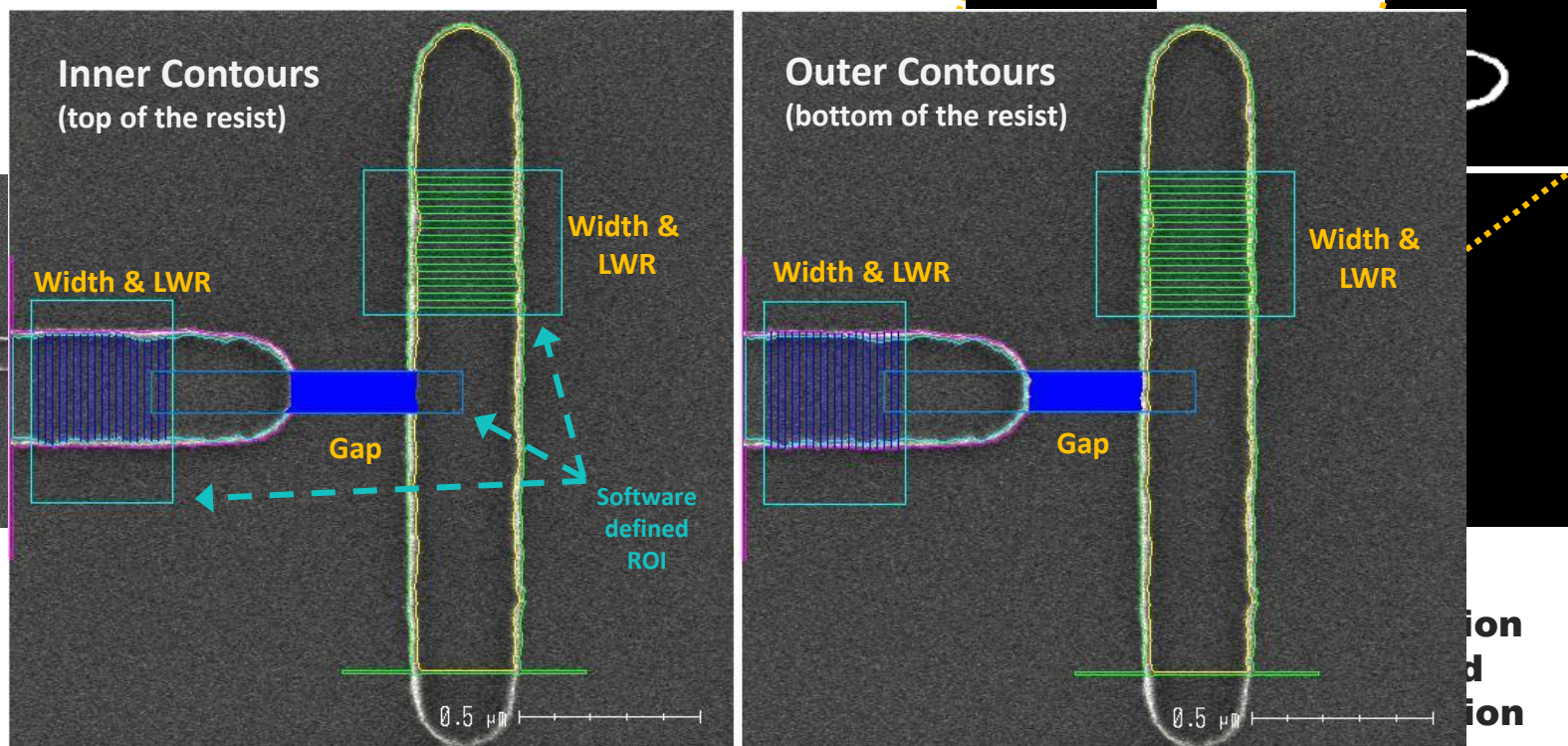
[MEMS 2022]

# What AI can do for ...



- Quantification and Metrology
- Learning process parameters
- Reverse direction
- AI-powered autonomous nanostructure design tool
- AI-powered autonomous device design tool

# Virtual Metrology: Resist CD-SEM



➔ **CD Values**

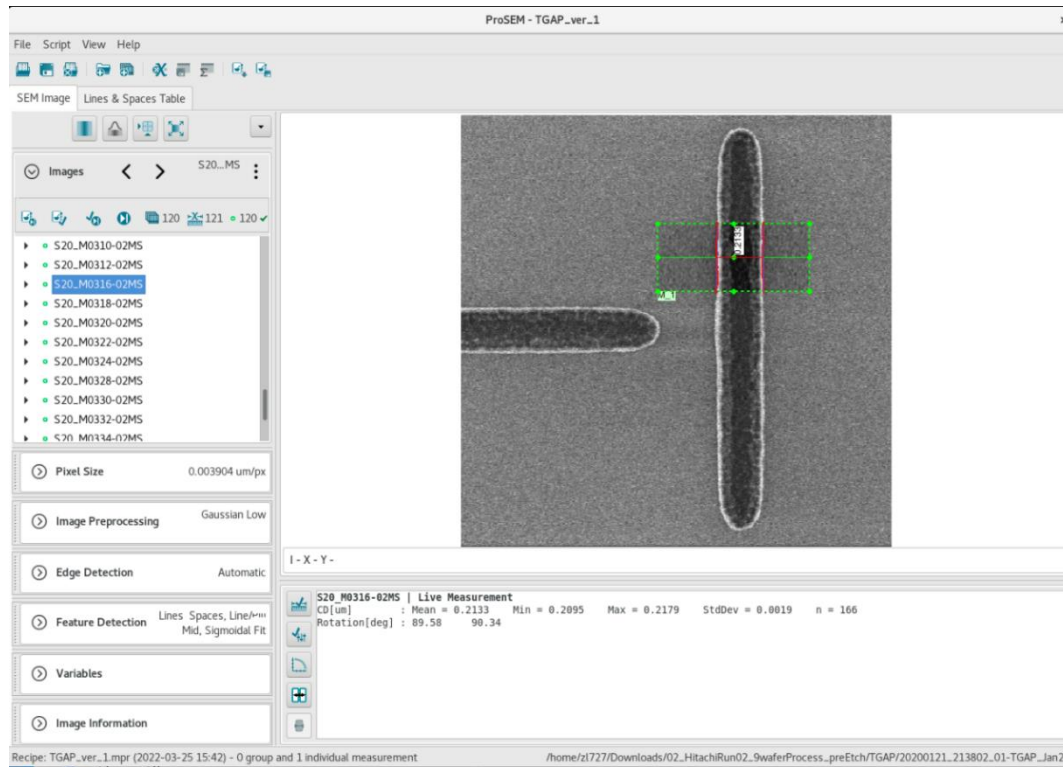
	CD-SEM images	filtering and edge detection	PR sidewall
TGAP			
DGAP			
TTGAP			
FLG			
TCL			
UL			
ETE			
TETE			



# Virtual Metrology Verification



Goal: ProSEM will serve as a gold standard to compare the accuracy of measurements



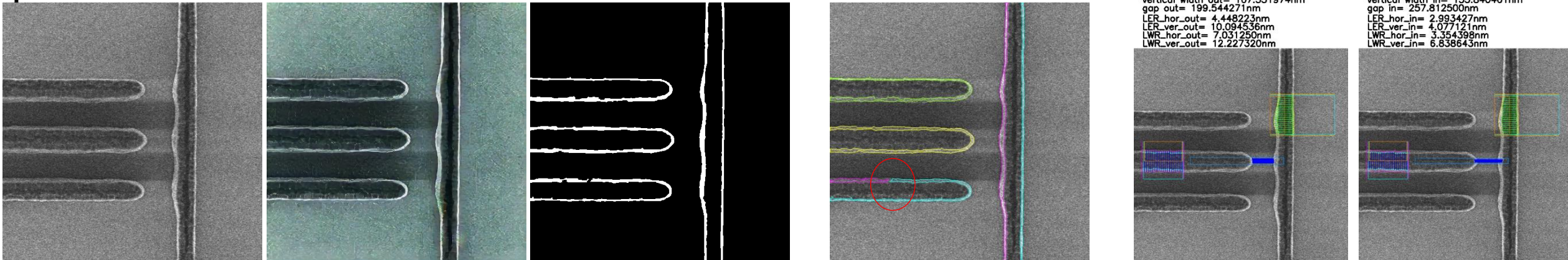
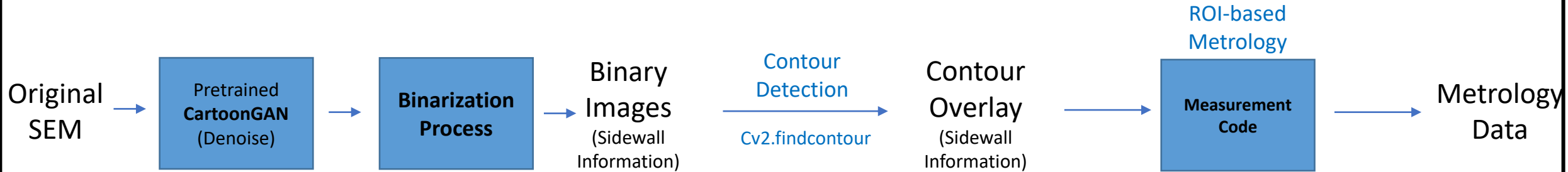
Scripting interface (Python) for automation

## ProSEM measurement results

Edge Mode	Fine Mode	Cd Pos	Auto Conti	Filter Type	Gauss X	Gauss Y	Line Scan	LL X[um]	LL Y[um]	UR X[um]	UR Y[um]
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9426	1.1154	1.6436	1.431	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9426	1.241	1.6436	1.5567	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9426	1.0525	1.6436	1.3682	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9426	1.2882	1.6436	1.6038	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9897	1.1625	1.6907	1.4782	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9426	1.0682	1.6436	1.3839	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9426	1.1154	1.6436	1.431	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.974	1.3196	1.675	1.6353	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9269	1.0997	1.6278	1.4153	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9426	1.2568	1.6436	1.5724	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9426	1.1311	1.6436	1.4467	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9426	1.1625	1.6436	1.4782	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.9269	1.1782	1.6278	1.4939	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.974	1.1154	1.675	1.431	
Automatic Sigmoidal	Mid	On	Gaussian	1	3	0	0.974	1.1154	1.675	1.431	

Automatic measurement on large batch of data is possible.

# DNN1: cartoonGAN + Thresholding



**Binarization Process**

- Median Filter + **Adaptive Thresholding** + Remove Small Connected Components + Erosion Dilation
- Median Filter + (**Sobel Edge Detection** + **Absolute Thresholding**) + Remove Small Connected Components + Erosion dilation

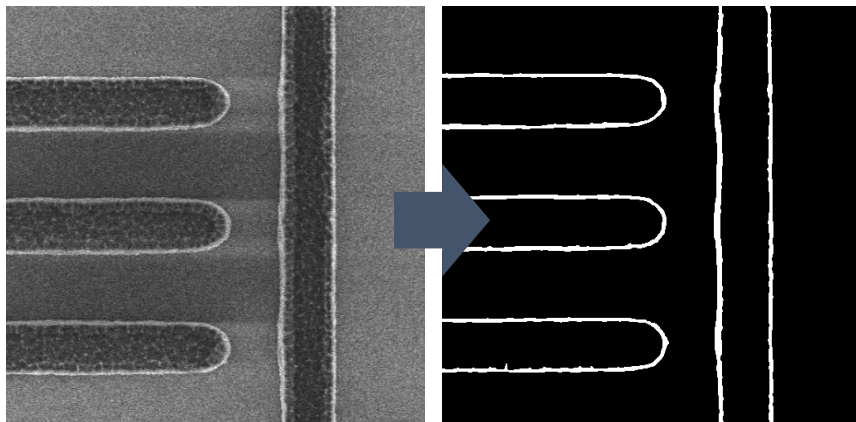
# Deep Learning Training Dataset



## Training Dataset Part 1:

Raw SEM images and Binary image from DNN1 are paired to form a **train & test dataset** for Pix2Pix and BasNet

Only **Well-connected** results are included

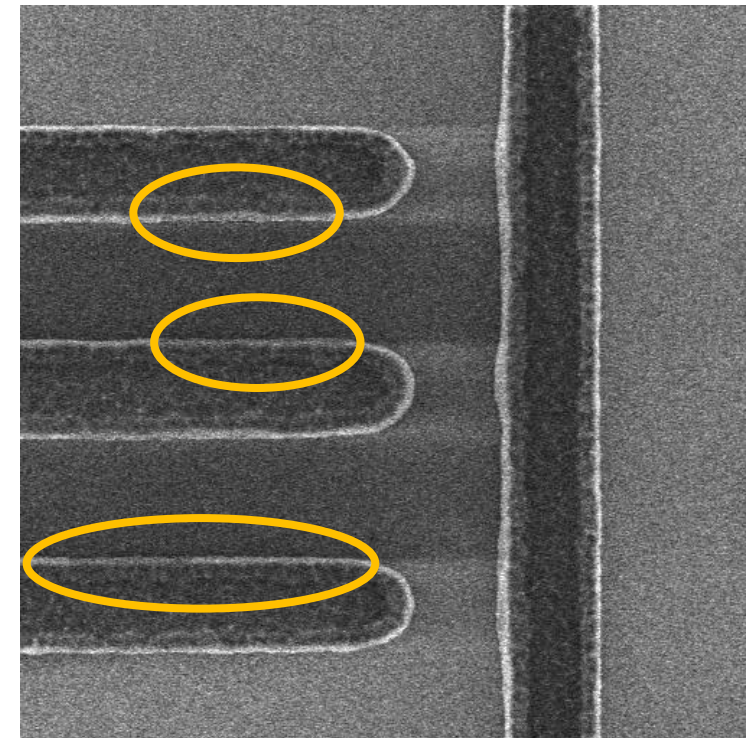


- A- The final trainset has **5572** image pairs including all eight structures from **wafer 1 to wafer 8**
- B- The testset has **908** image pairs including all eight structures from **wafer 9**

## Training Dataset Part 2:

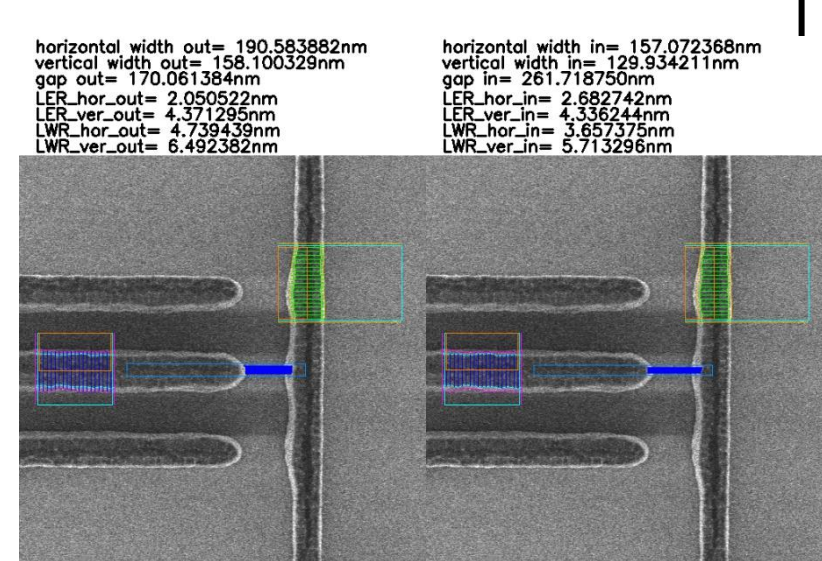
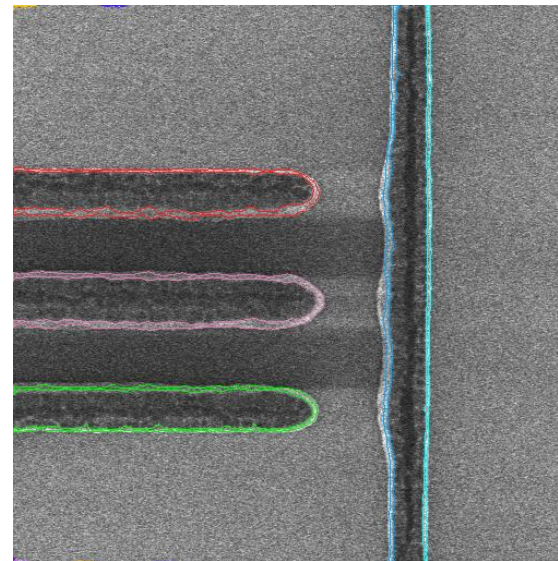
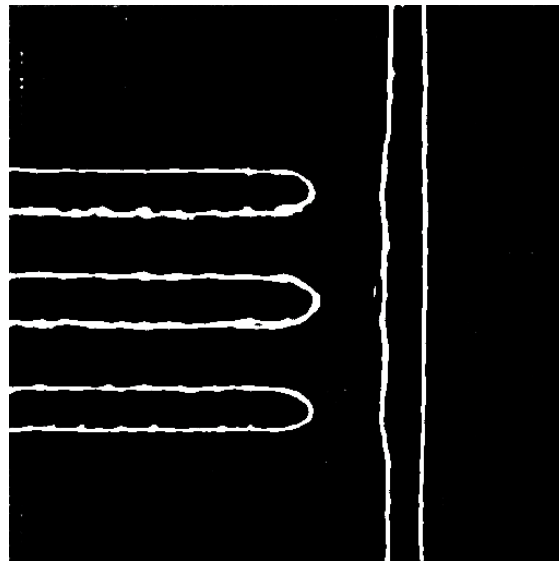
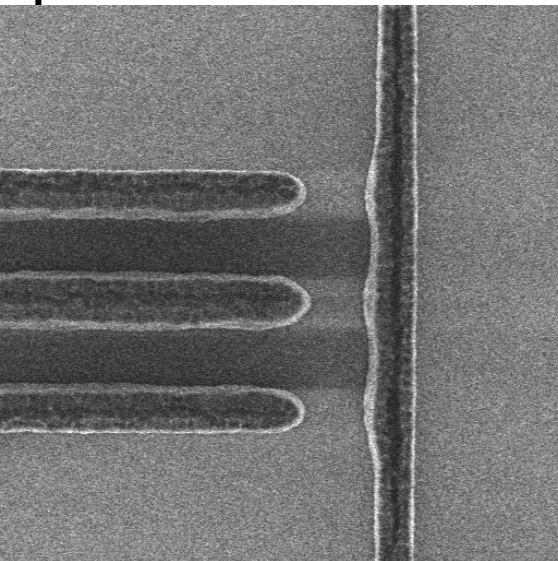
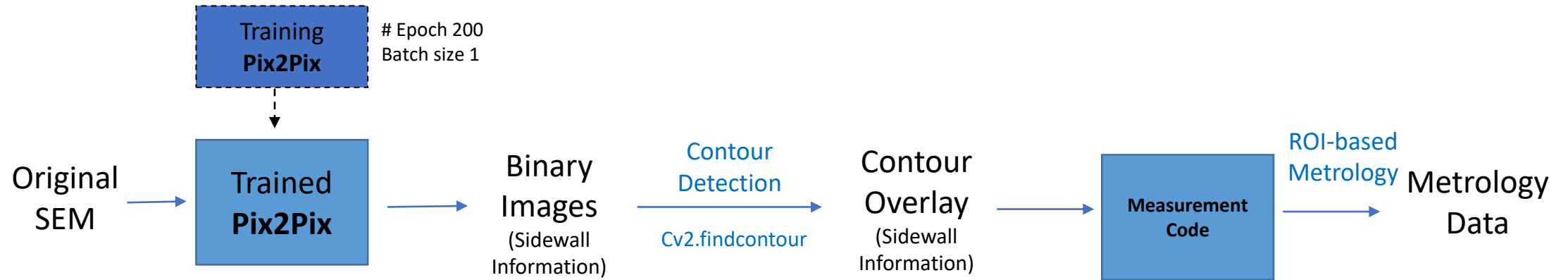
### Data Augmentation

Reduced contrast of selected areas of sidewalls

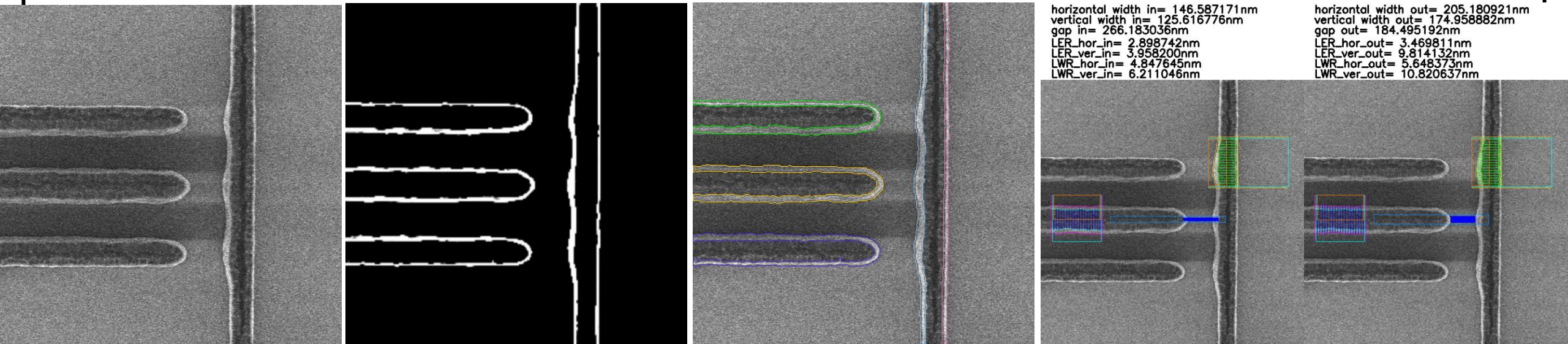
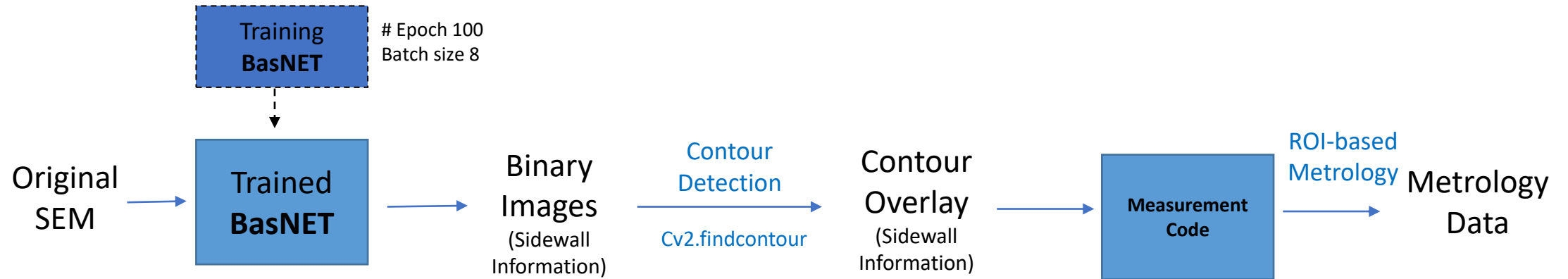


**Note:** Augmented SEM with reduced contrasted is paired with well-connected binary image in the training dataset.

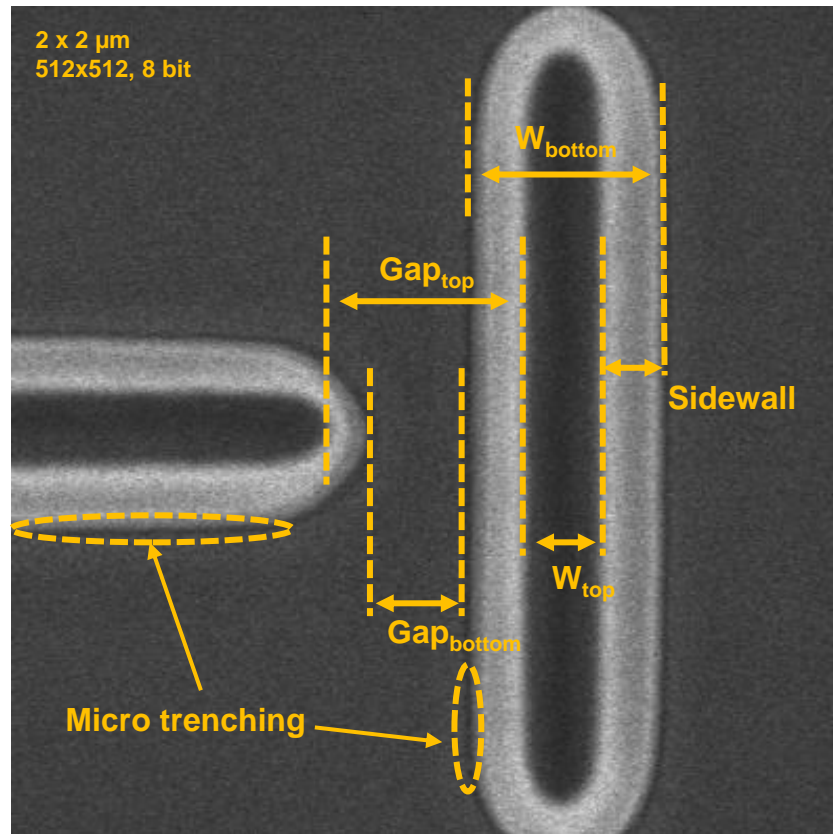
# DNN2: DNN1 + Pix2Pix



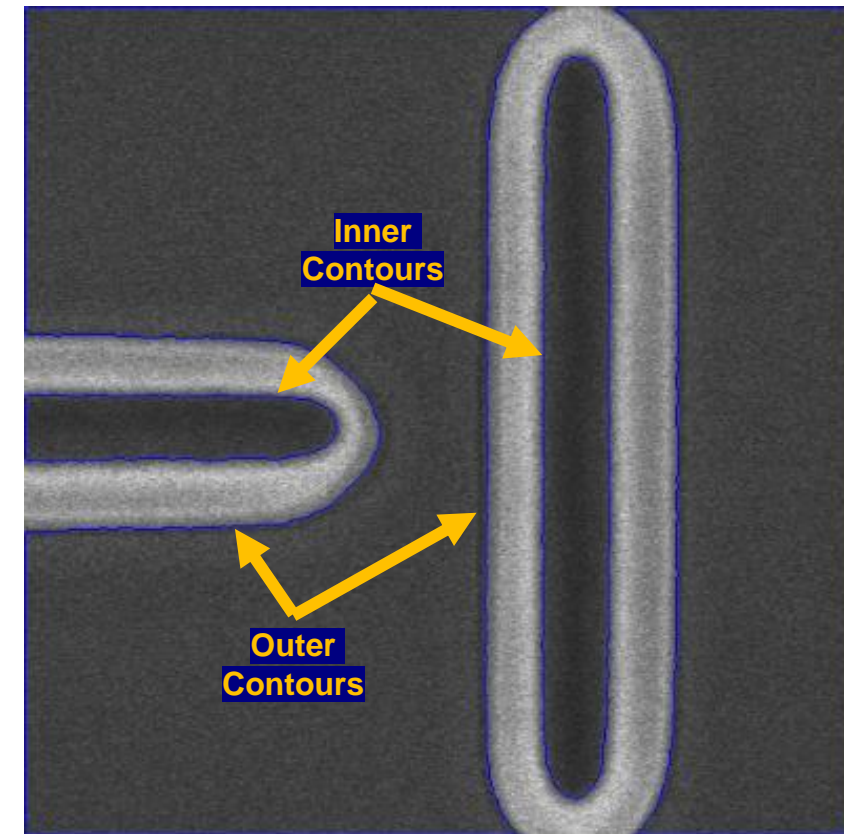
# DNN3: DNN1 + BasNET



# Virtual Metrology: Post-Etch CD-SEM



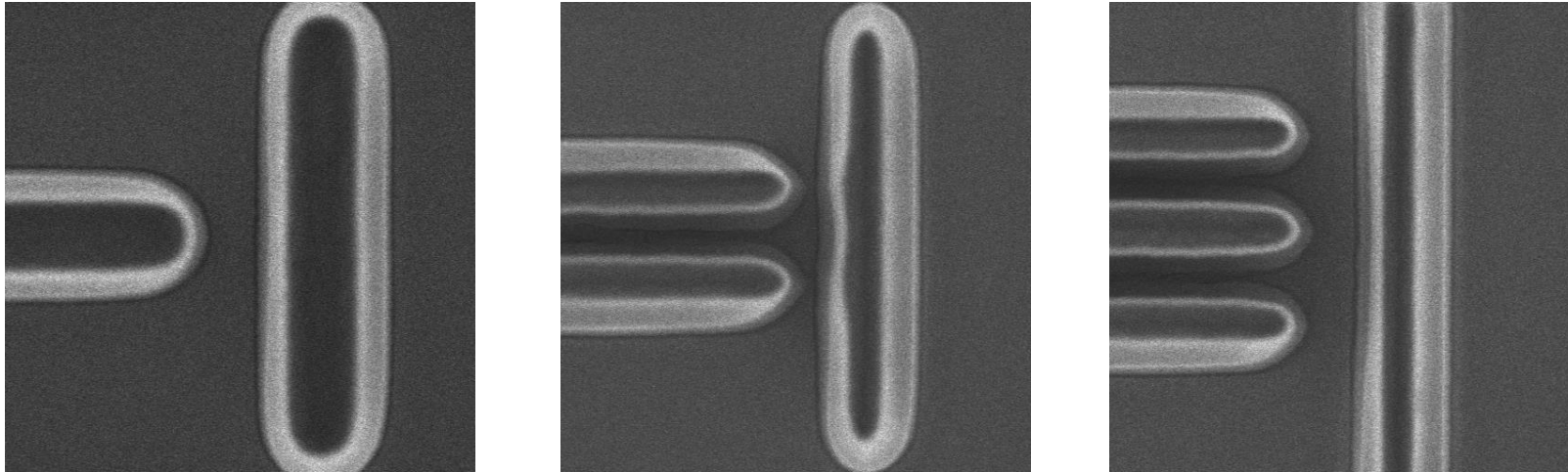
Active  
contour  
→



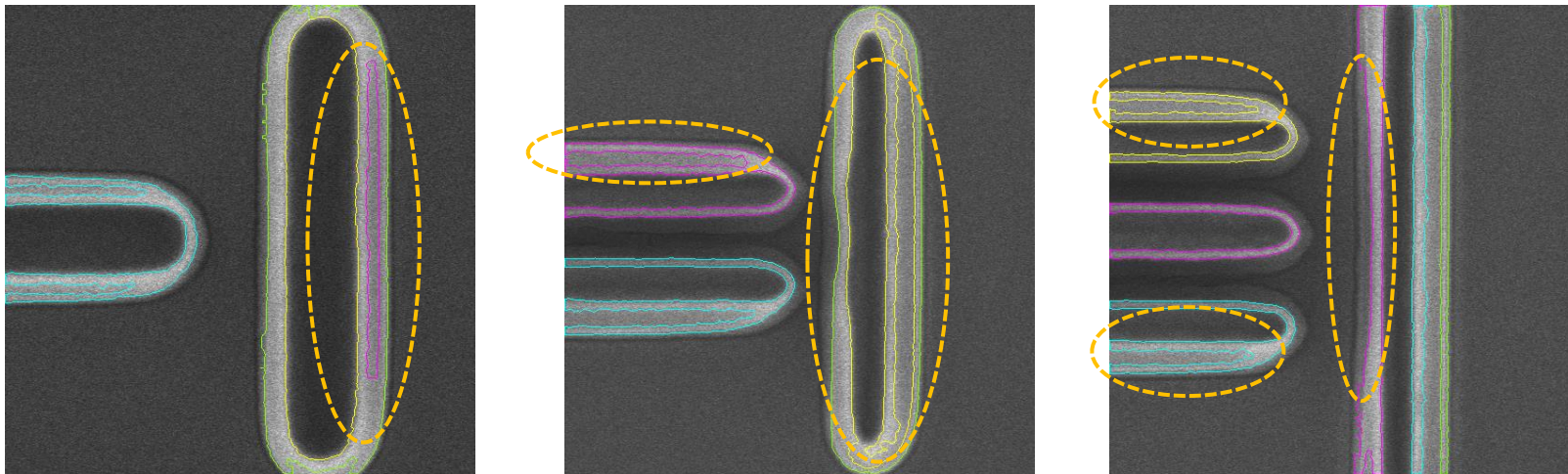
# Virtual metrology challenges with complexities of post-Etch CD-SEM images



Post Etch  
CD-SEM Images



Virtual Metrology  
Results  
(using Pre-Etch  
algorithms)



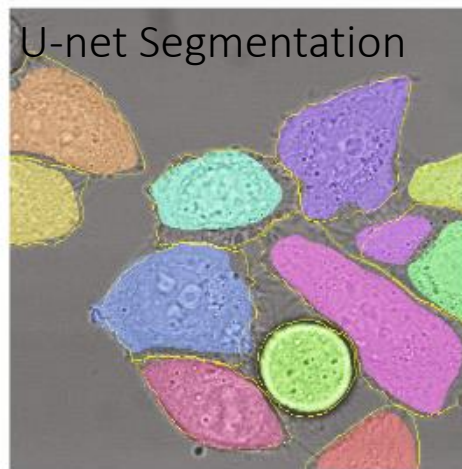
# U-net for image segmentation



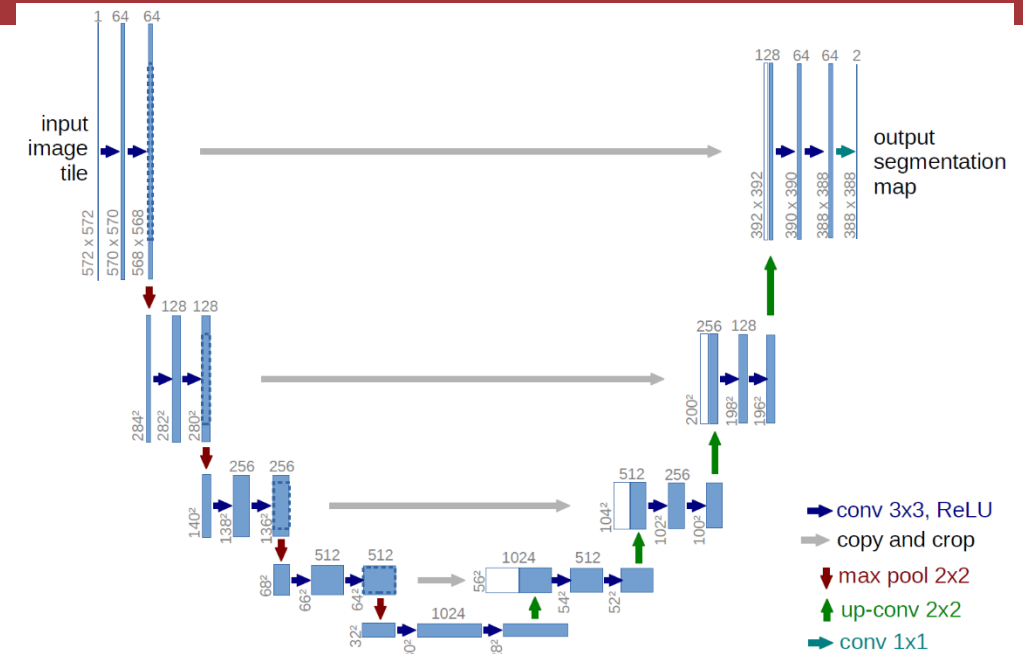
**Goal:** automatic and robust segmentation of sidewalls in post-etch CD-SEM images

**Progress:** training U-net with successful results of simple segmentation algorithms

Differential Interference Contrast (DIC)  
Image-HeLa Cells



## U-net Architecture

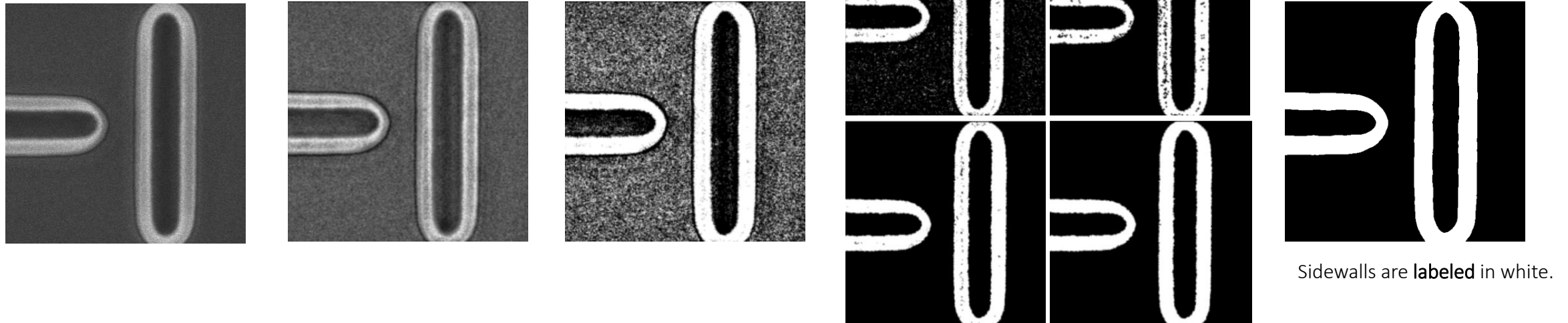


[https://link.springer.com/content/pdf/10.1007%2F978-3-319-24574-4\\_28.pdf](https://link.springer.com/content/pdf/10.1007%2F978-3-319-24574-4_28.pdf)



# Post-Etch binarization process

Goal: automatic labeling to train a U-net for image segmentation



**CD-SEM  
RAW  
image**



**Histogram  
equalization**



**Thresholding**



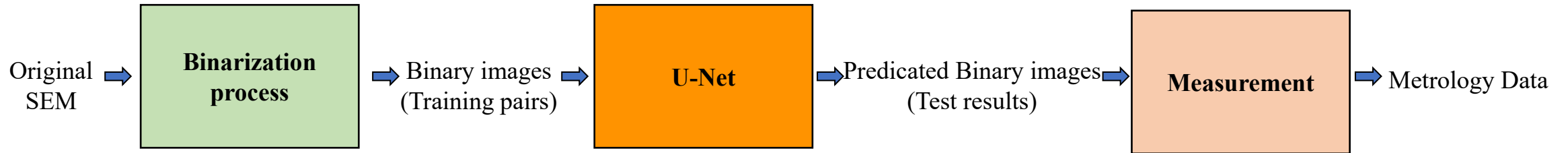
**1.Erosion  
2.Small contours  
removal  
3.Dilation  
4.Small contours fill**



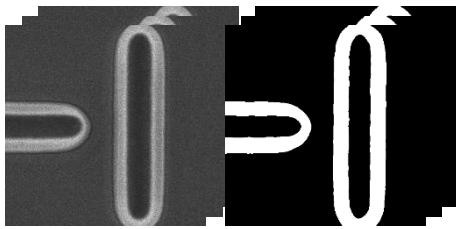
**Median filter**

Sidewalls are labeled in white.

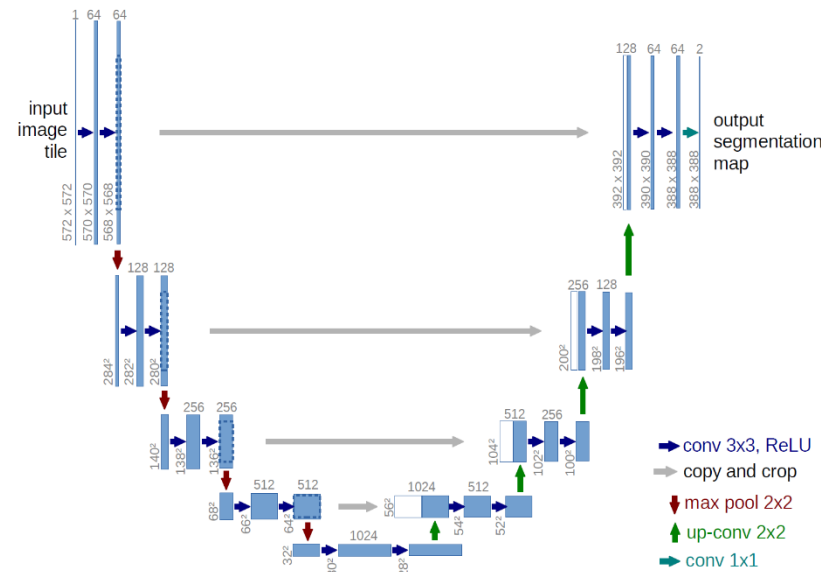
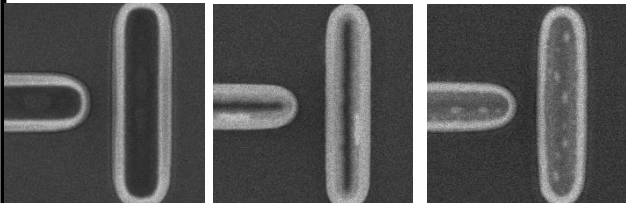
# U-net: one structure type (TGAP/DTGAP)



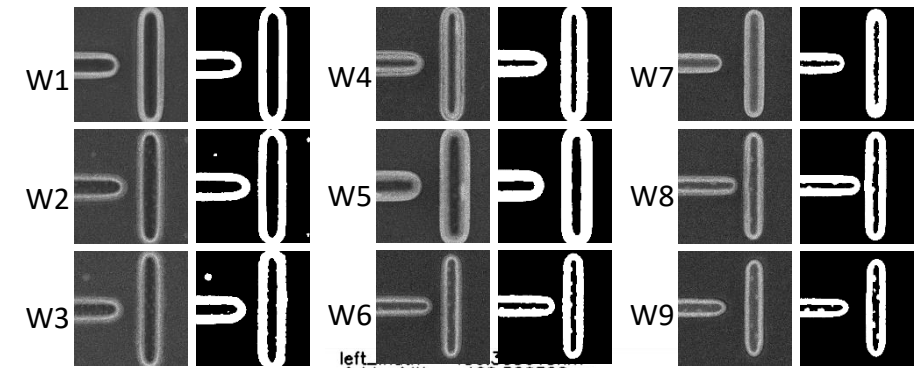
**Train set**  
TGAP W1 104 pairs



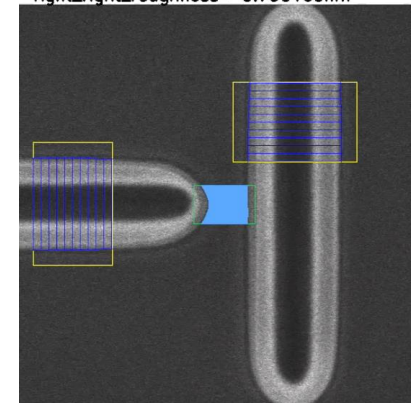
**Test set**  
TGAP W1-9



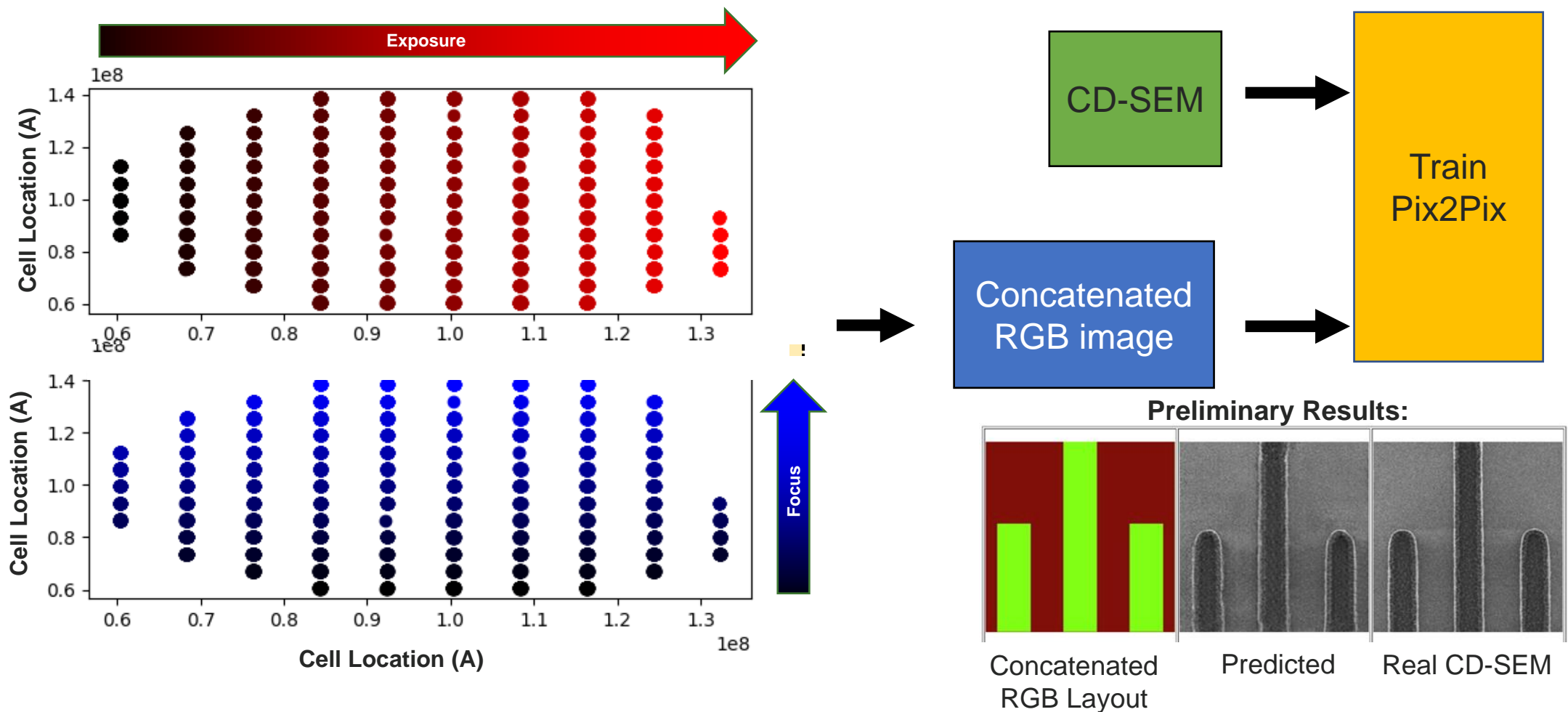
**Predicted binary images**



left\_width = 460.520328nm  
 gap = 205.652574nm  
 left\_up\_roughness = 0.660804nm  
 left\_bottom\_roughness = 1.413594nm  
 right\_left\_roughness = 2.459586nm  
 right\_right\_roughness = 0.790160nm

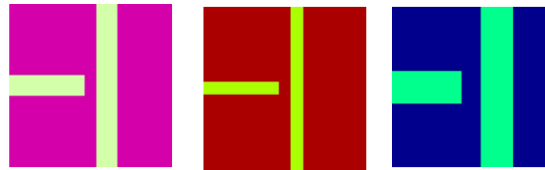
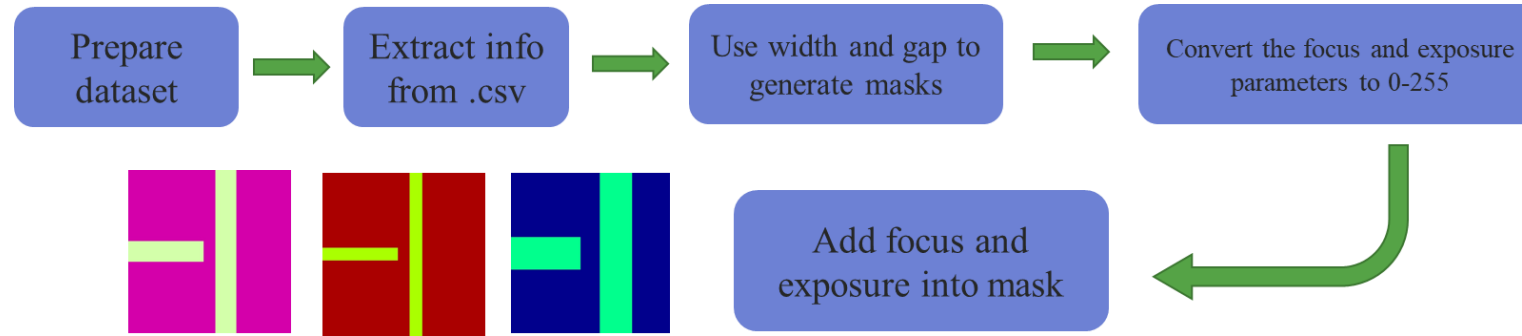


# Using RGB channels to merge process parameters with CD-SEM data

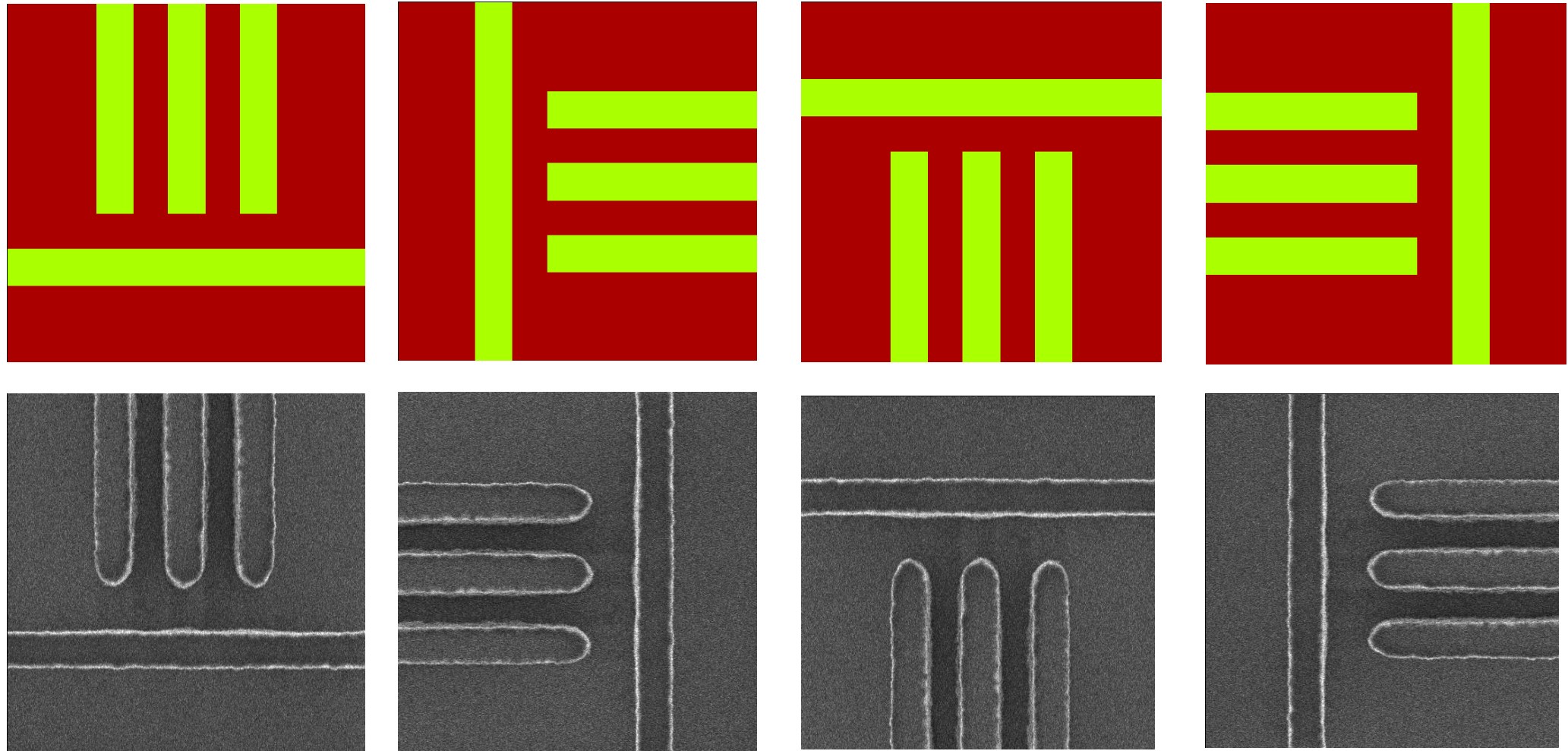


# Training dataset: pseudo-colored layouts

- Layout + Process Parameters



# Augmentation to enhance the learning (rotation example)



# Results: with augmentation (16X)

## Best result parameters for pix2pix: with augmentation

Crop\_size = 256

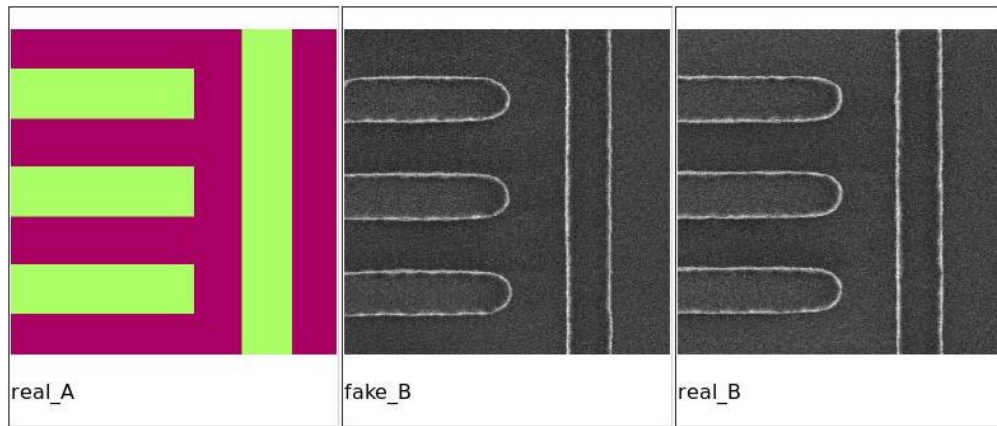
batch\_size = 16

N\_epoch = 400

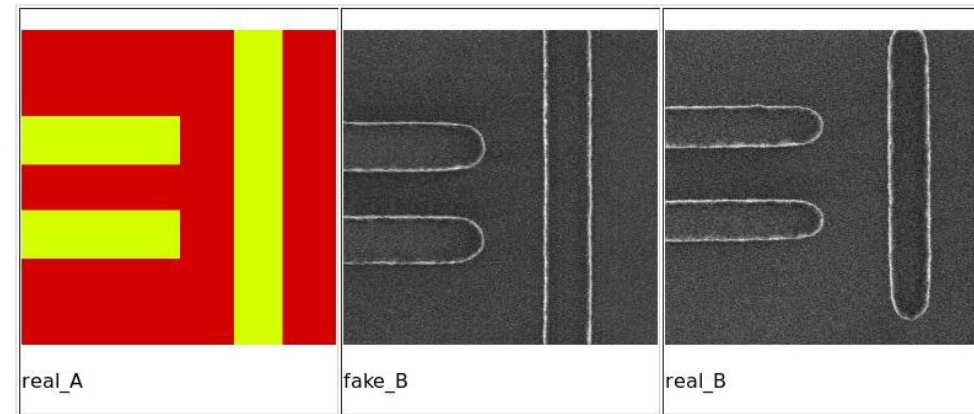
Epoch\_decay = 100

Learning\_rate = 0.0001

Augmentation: Rotated 90° 180° 270°, randomly cropped (4 times each)



**BS15\_M0190-02MS**

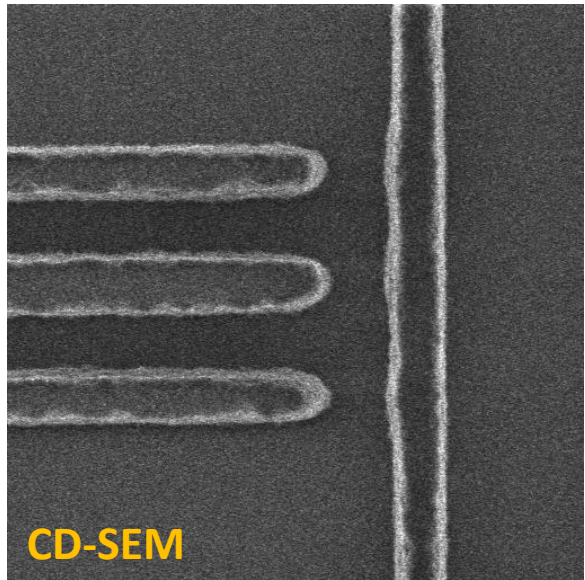


Test results for other layout (Not included in the training set)

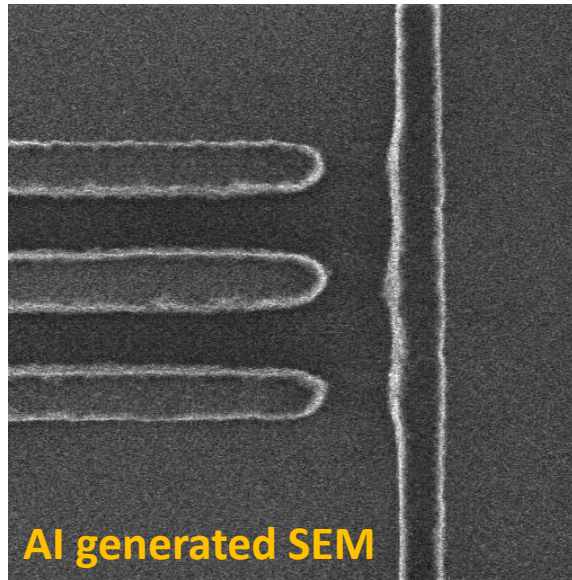
# Toward assessment of learning outcomes

## Experimental Image

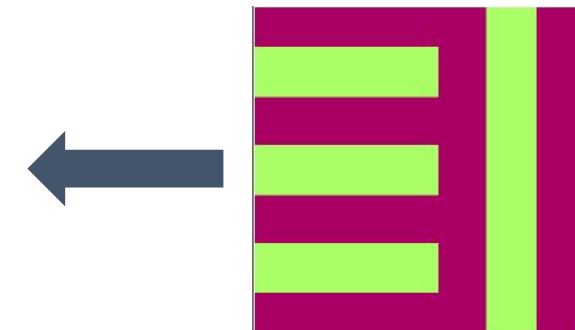
S15\_M2740-02MS.tif



## Process-aware AI Predicted Image

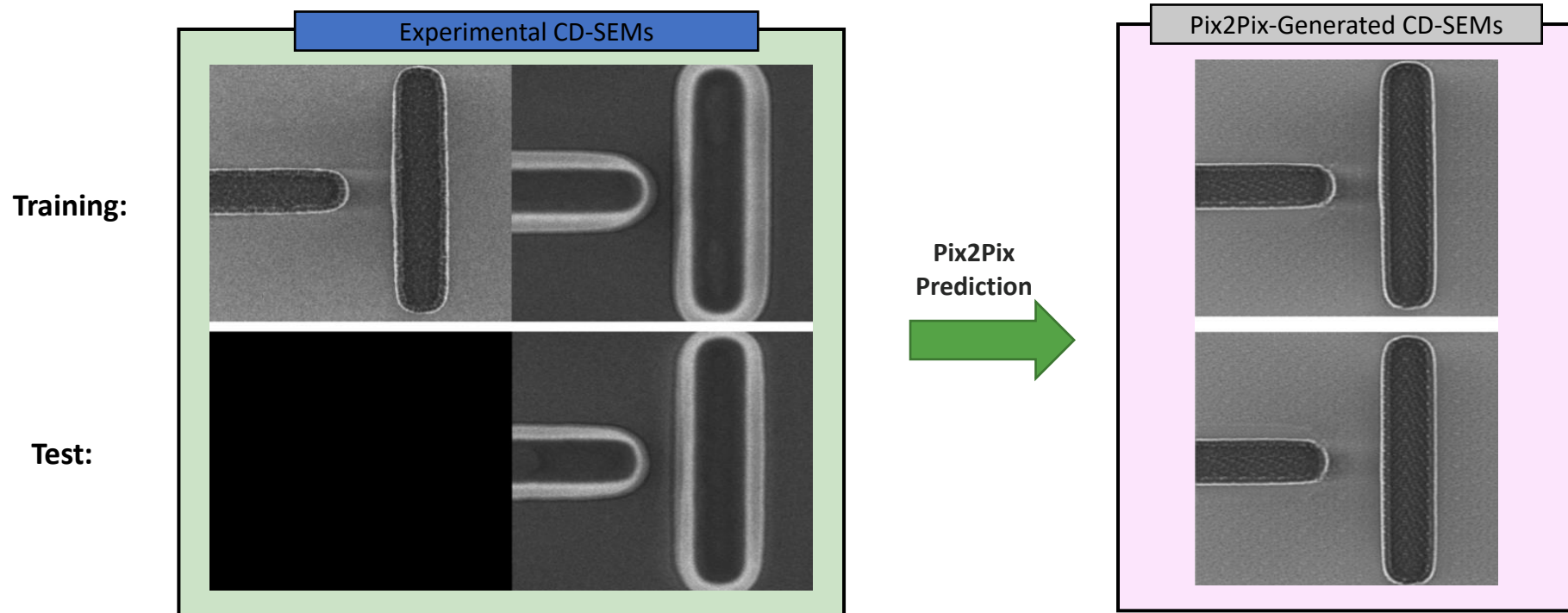


Pseudo-colored layout with process parameters



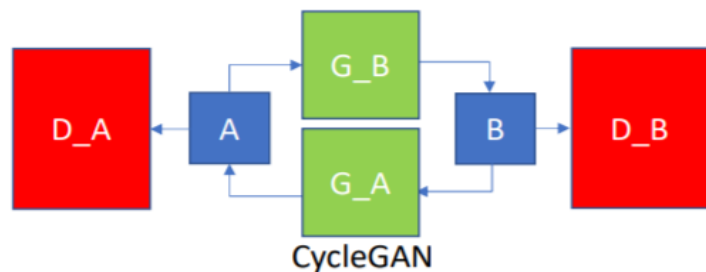
Process Parameters:  $E=21 \text{ J/cm}^2$ ,  $F=-0.5 \text{ }\mu\text{m}$   
SEM images show  $2 \times 2 \text{ }\mu\text{m}$  area (3.9 nm/pixel)

# Reverse direction: process diagnostics

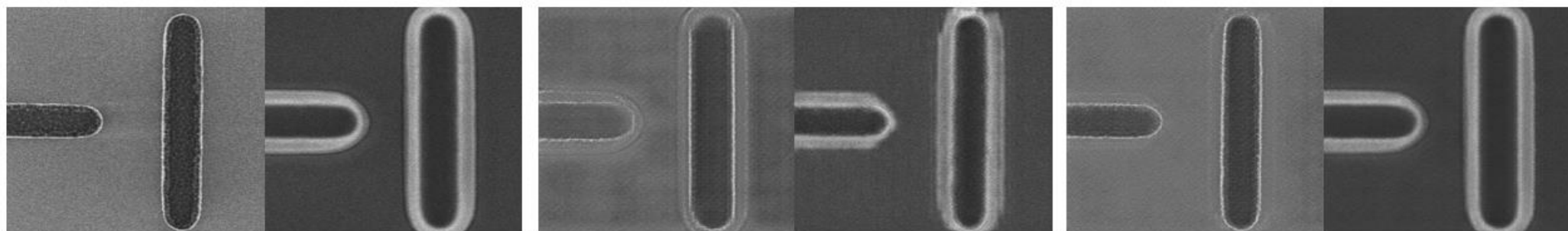




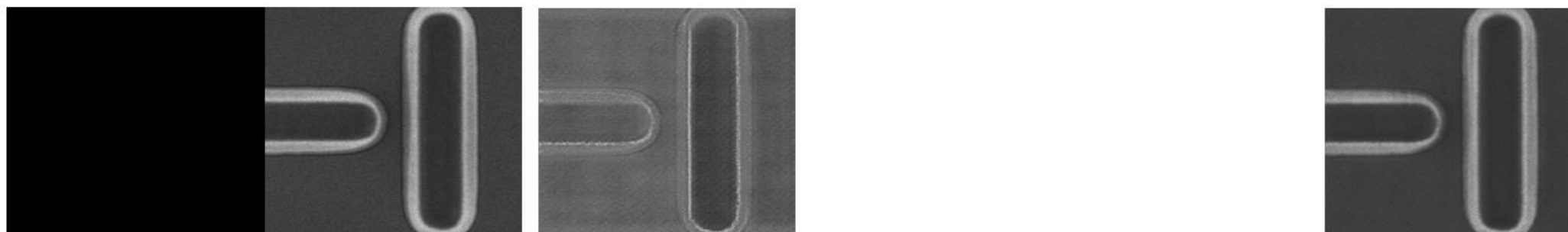
# CycleGAN and Cycle Consistency



Training:



Test:



A  
Pre-Etch

B  
Post-Etch

$G_A(B)$   
Fake Pre-Etch

$G_B(A)$   
Fake Post-Etch

$G_A(G_B(A))$   
Recovered Pre-Etch

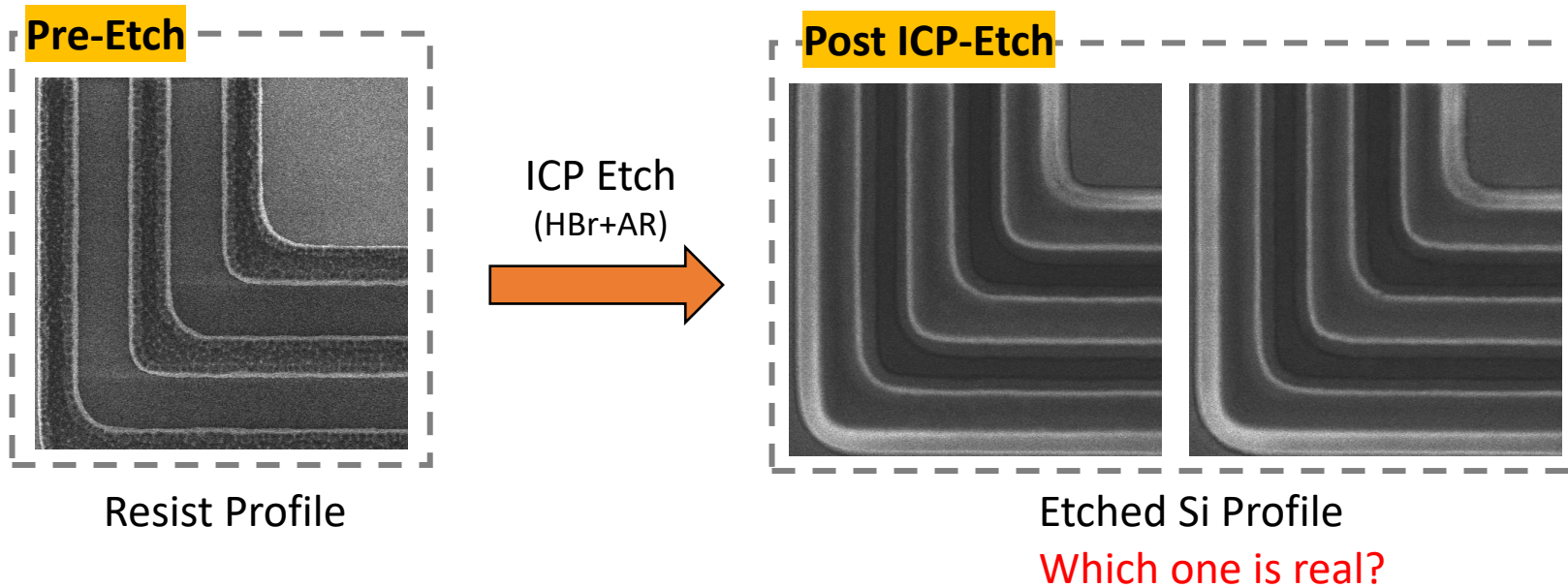
$G_B(G_A(B))$   
Recovered Post-Etch

# Can AI make nanodevice fabrication Ubiquitous?



- We developed ML models to learn the DUV lithography process and we demonstrated interpolation beyond training dataset
- We trained deep learning models to learn and predict the outcomes of DUV lithography and Plasma Etch Processes
- AI models can be used as a design tool (mask, process parameters,...) for micro and nanofabrication
- AI potentially simplifies integration of multiple foundries working on one device, which potentially provides privacy gains at hardware level
- AI driven design improvement are not limited to MEMS and can be applied to IC industries, printed electronics, optics, and so forth

# What do you think?



\* SEM Images are 2x2  $\mu\text{m}$ , 512x512, 8 bit



KRENTZMAN QUADRANGLE

NORTHEASTERN

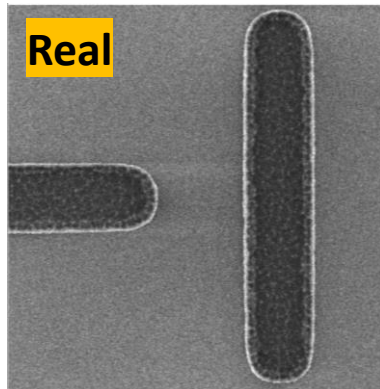


UNIVERSITY

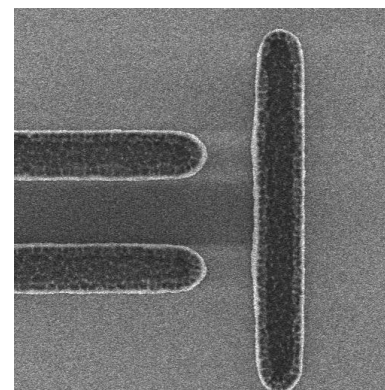
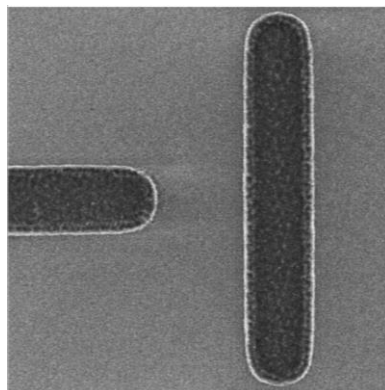


Mask Layout

Experimental  
DUV Lithography

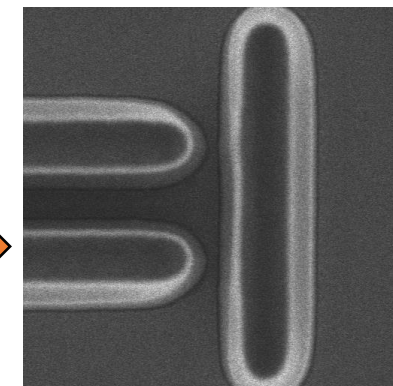


Pix2Pix  
Prediction

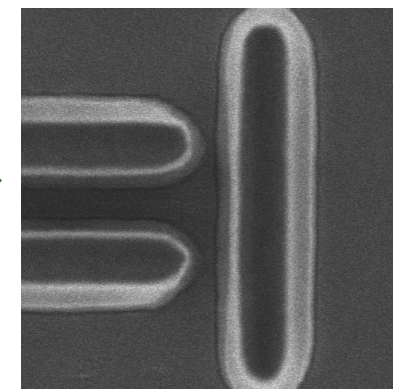


Resist Pattern

Experimental  
Plasma Etch



Pix2Pix  
Prediction

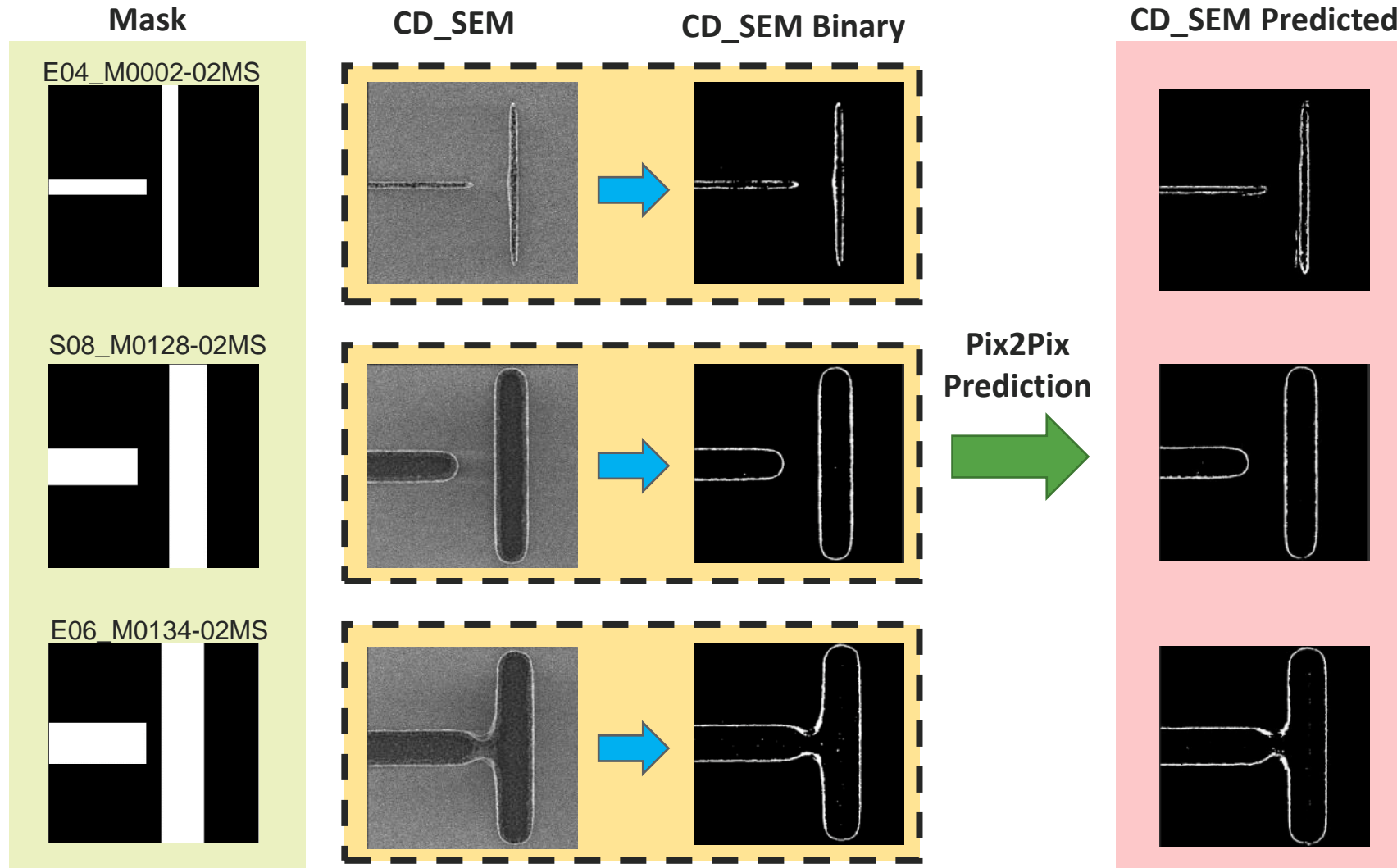


# Back UP Charts: TA1-AI

This section contains the supporting data and charts to support extended discussions and the Q&A section.

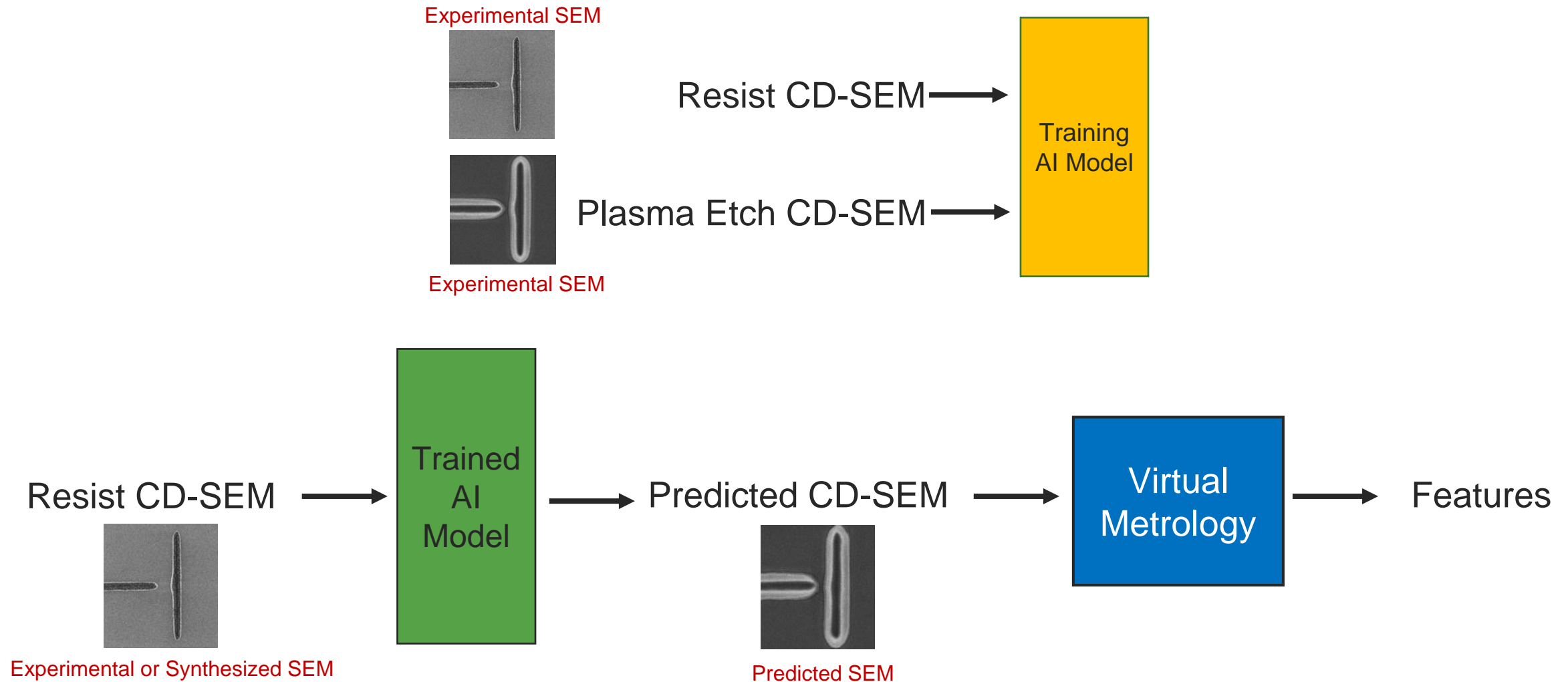
- Pix2Pix details
- Augmentation
- Quantification and virtual metrology
- Process parameters

# DUV lithography prediction by trained Pix2Pix





# Learning outcomes Plasma Etching by Image Translation

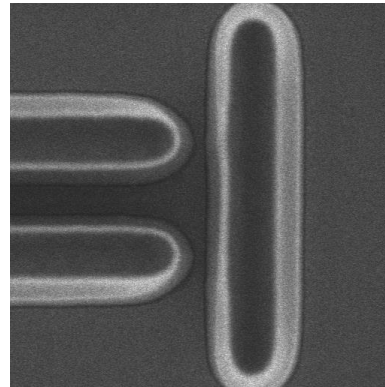
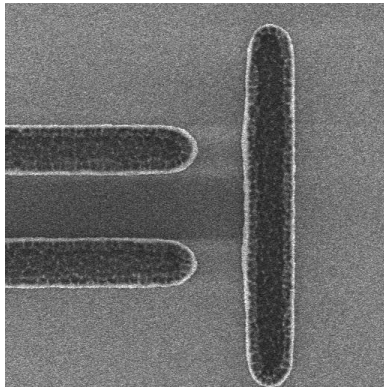


[this work, unpublished preliminary results]

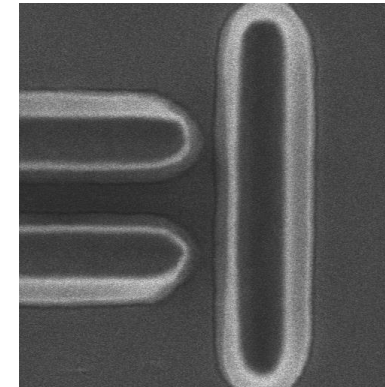
# Pix2Pix Results for Plasma Etch



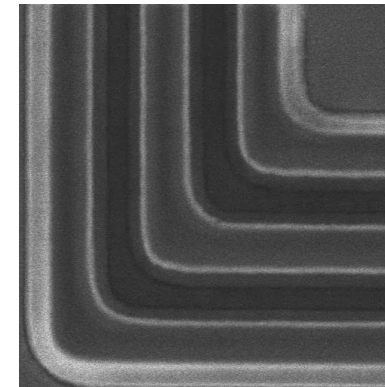
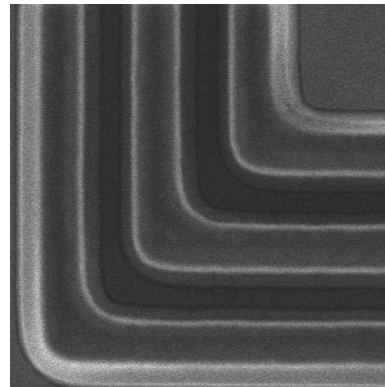
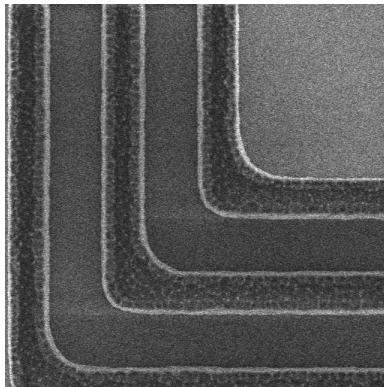
DTGAP



Pix2Pix  
Prediction



TCL



Pre-Etch  
Resist Profile

Post-Etch  
Si Profile

Prediction  
Synthesized SEM

SEM images shows a 2 x 2 um area.

[SEMI master class #6, 2021]

# Summary



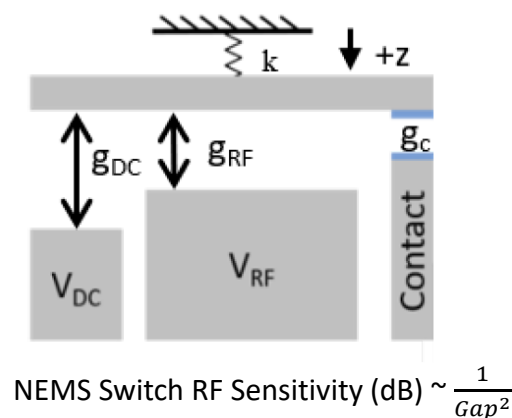
- ML feature-based model for DUV lithography process
- Pix2Pix model to learn to predict the outcomes of the DUV Lithography and Plasma Etch

## Future Directions:

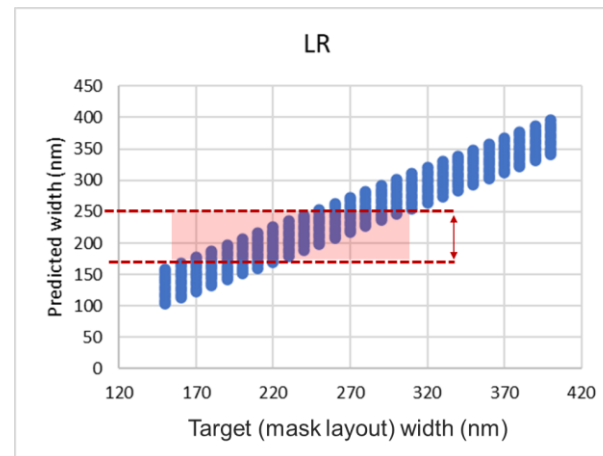
End-to-End implementation: adjusting layout to achieve target performance metric

OES feature-based plasma etch improvement

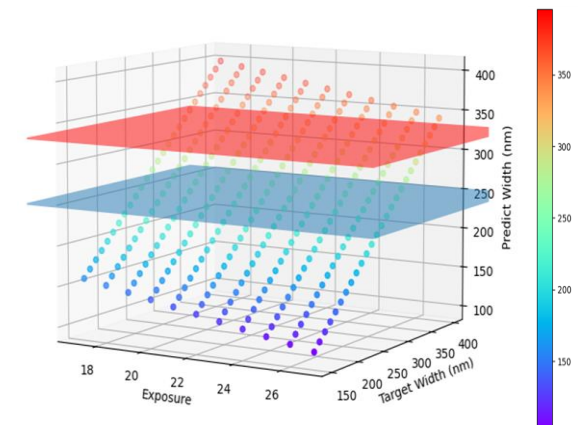
Design tool to improve the electrical and mechanical performance



Selected feature  
→



Process window  
→



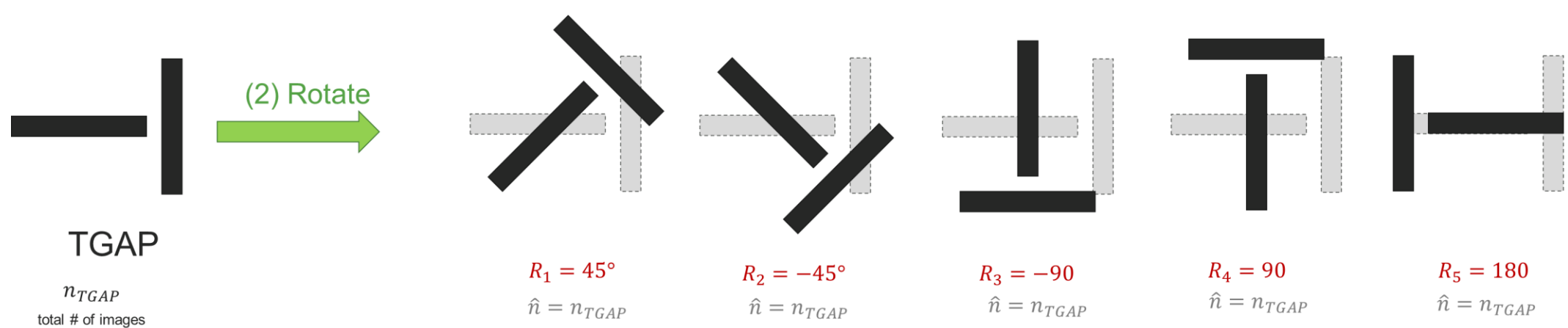
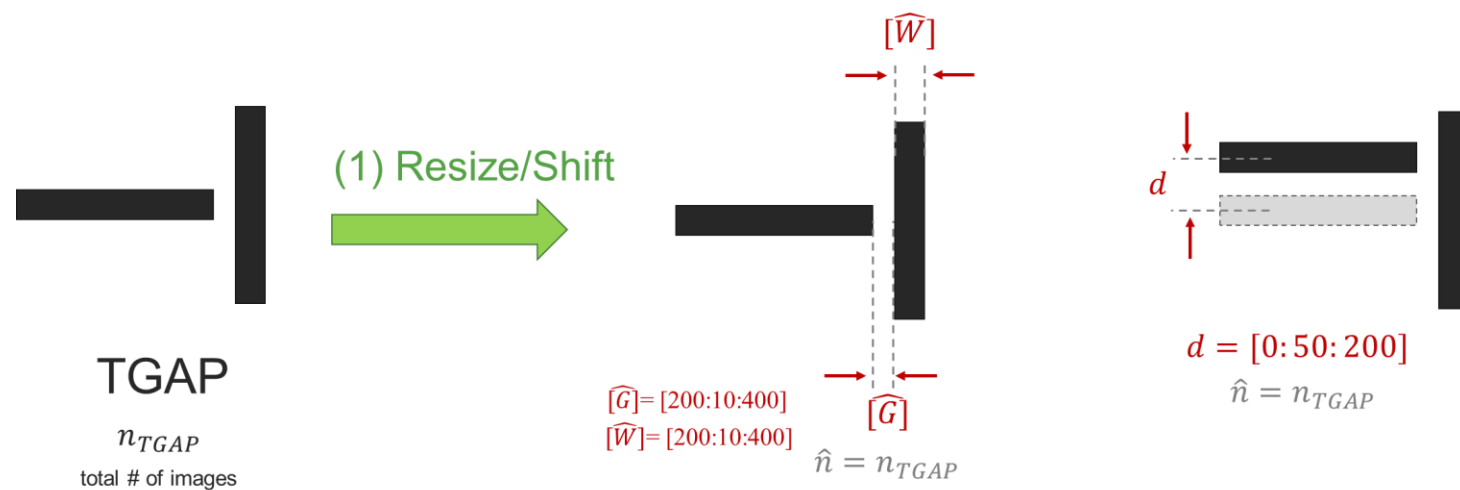
# Summary



- AI can improve design (mask, process parameters,....) for micro and nanofabrication
- AI driven design improvements can be used for microcalorimeter and Ultrasound microdevices that are also important applications
- AI potentially simplifies integration of multiple foundries working on one device, which potentially provides privacy gains at hardware level
- AI driven design improvement are not limited to MEMS and can be applied to IC industries, printed electronics, optics, and so forth

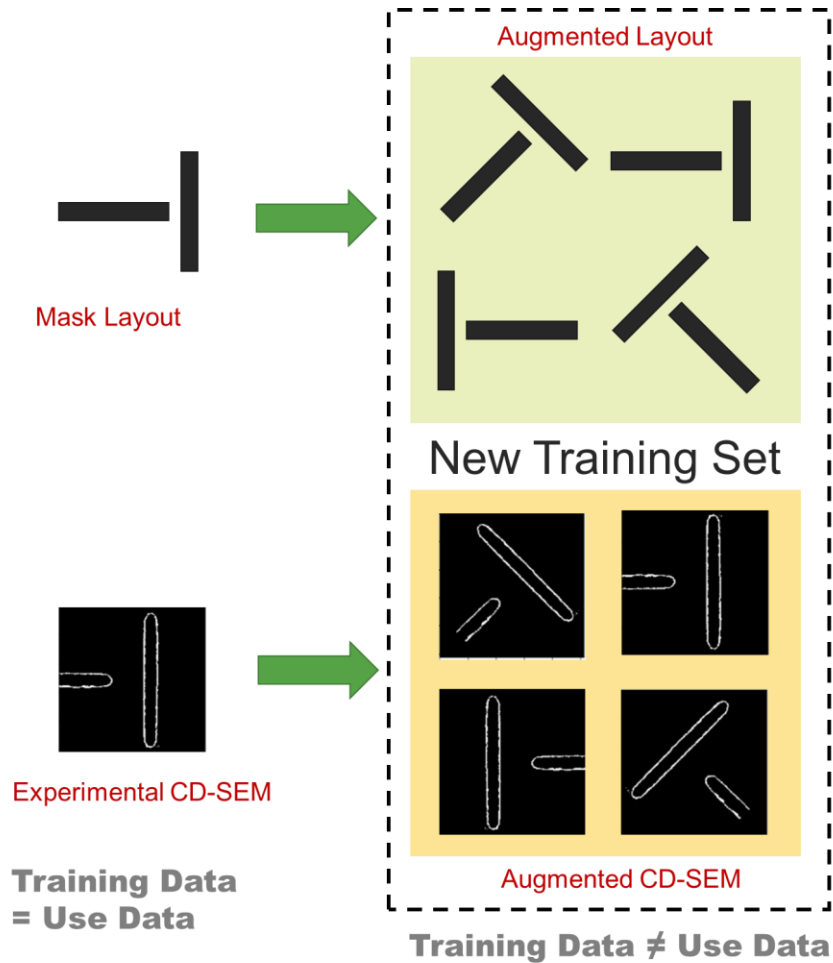
# Beyond Training Database: Augmentation

Training Data  $\neq$  Use Data



[this work, unpublished preliminary results]

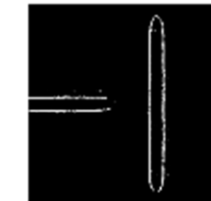
# Augmented Data and Pix2Pix Results



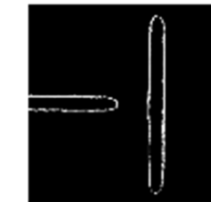
Augmented Layout



Prediction

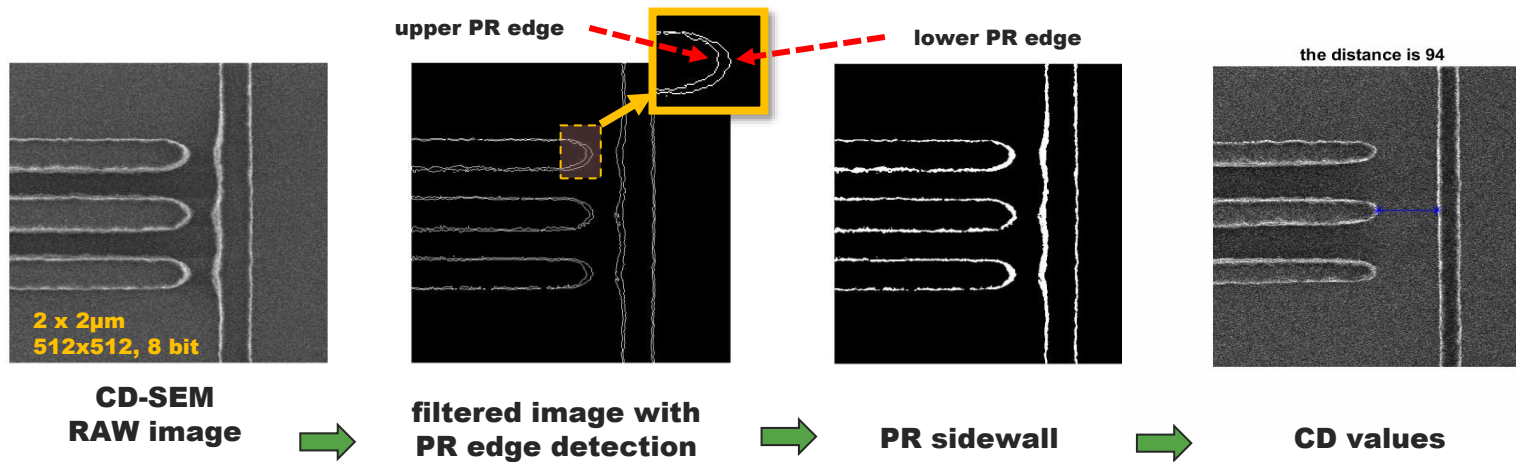
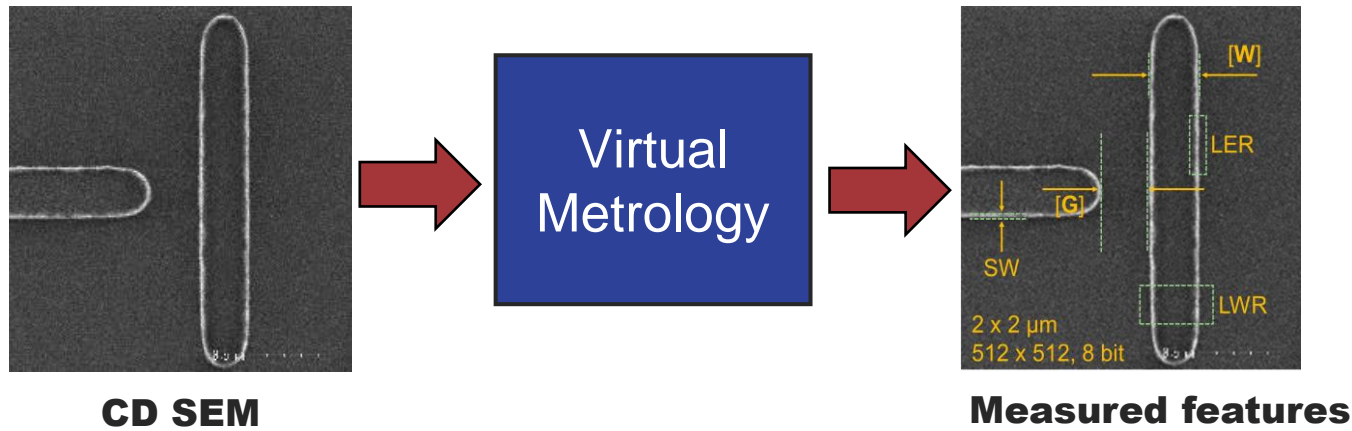


Augmented CD-SEM



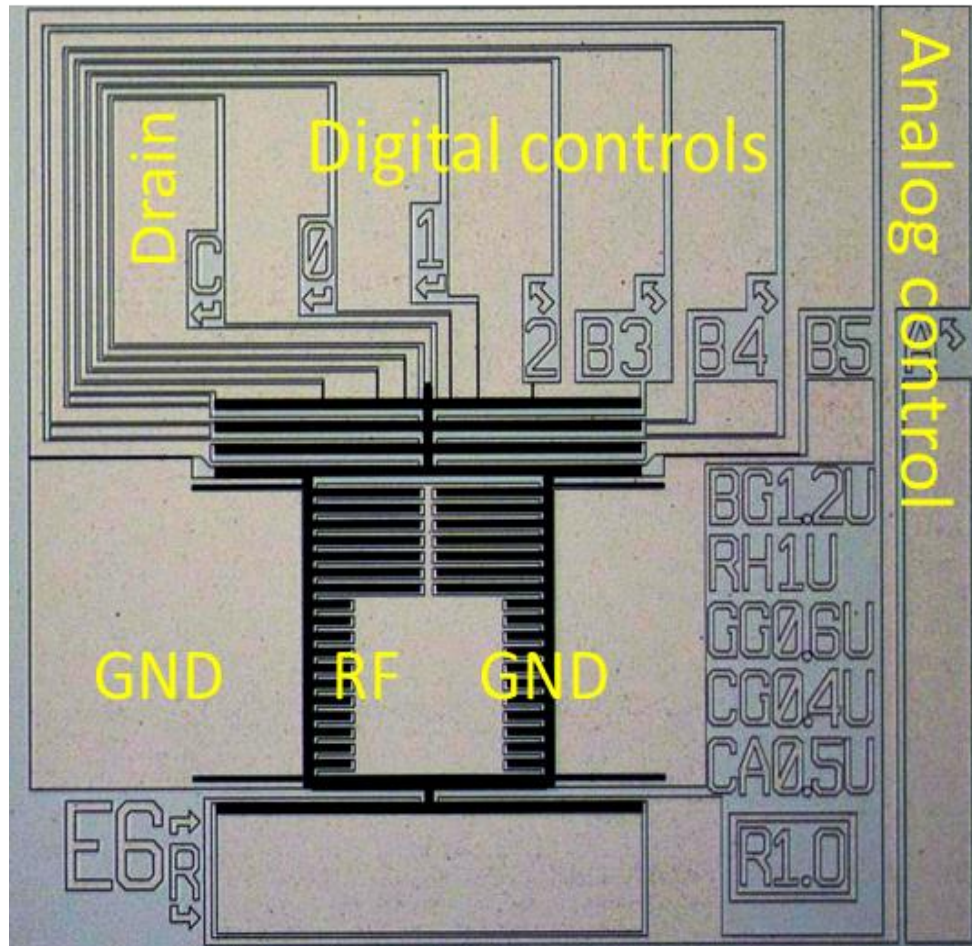
[this work, unpublished preliminary results]

# Virtual Metrology



	CD-SEM images	filtering and edge detection	PR sidewall
TGAP			
DGAP			
TTGAP			
FLG			
TCL			
UL			
ETE			
TETE			

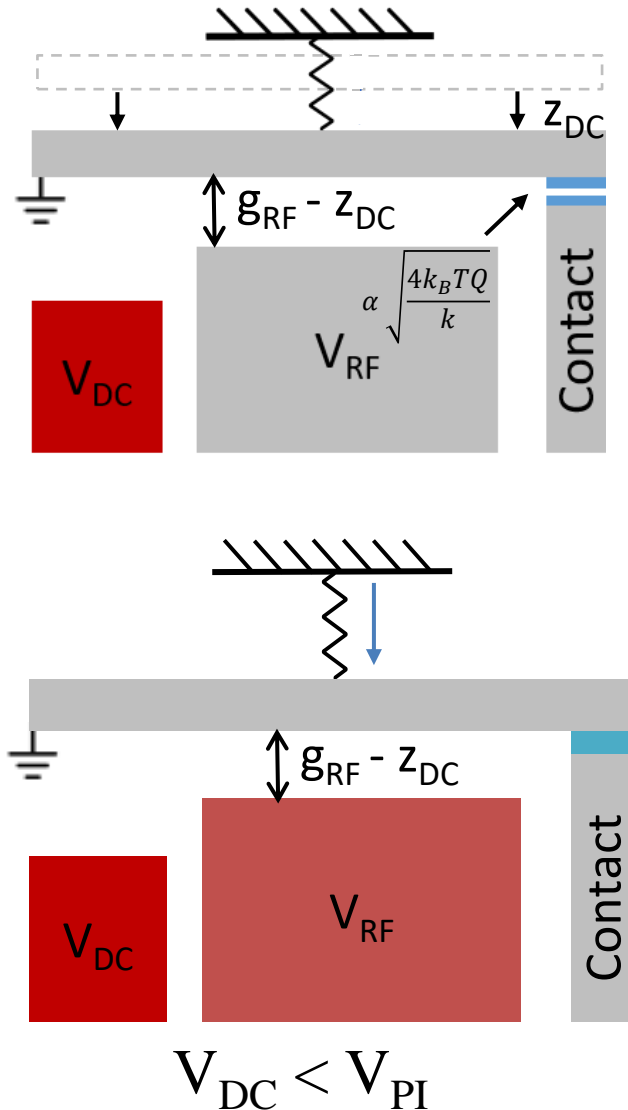
# Test vehicle: NEMS switch for RF wakeup



- NEMS switch can trigger at near zero power at the receipt of a specific very low RF signal
- Low power wakeup enables long-battery lifetime devices
- NEMS switch critical to ultralow signal wakeup radio – both for DOD and civilian IoT applications
- NEMS switch uses both lithography and etching for testing AI framework



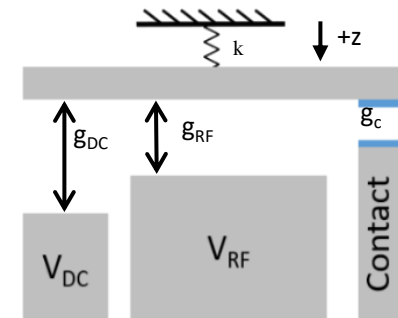
# Device Operation



1. Pre-bias until the contact gap is within a few times the thermal noise displacement ( $z_n$ )

$$z_{DC} = g_c - \alpha \sqrt{\frac{4k_B T Q}{k}}$$

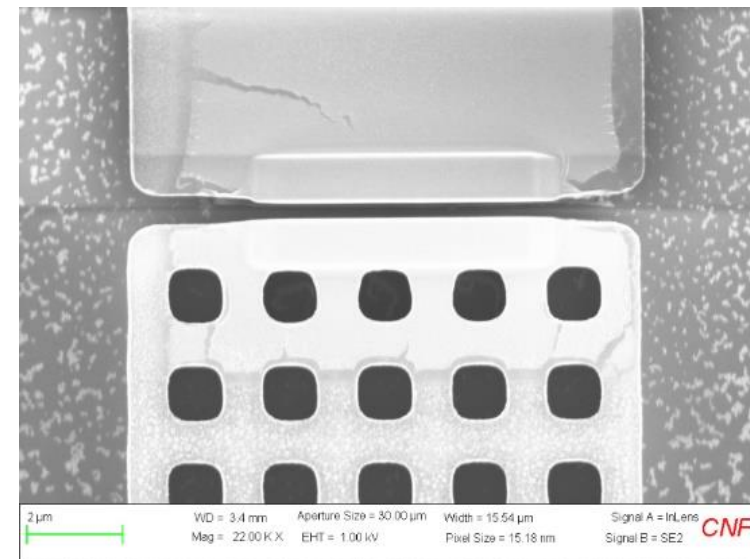
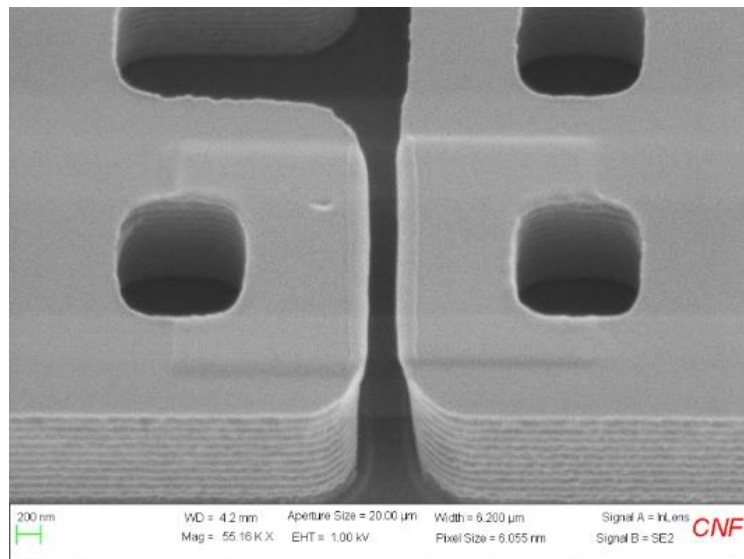
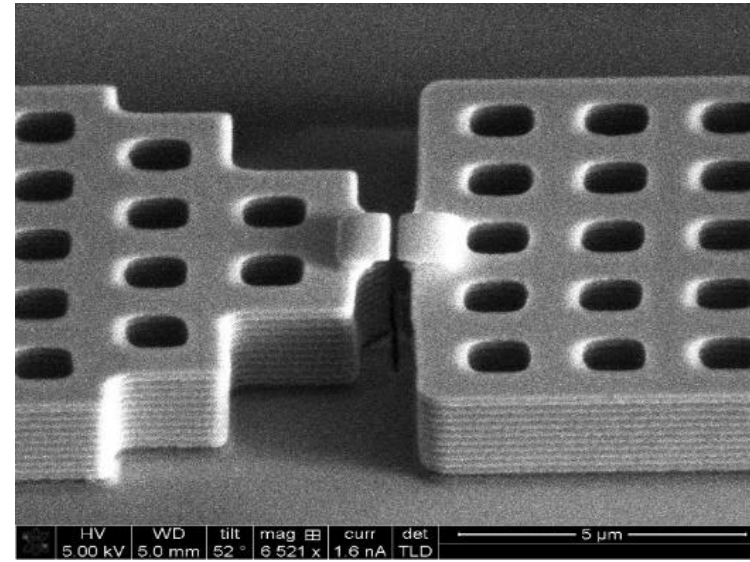
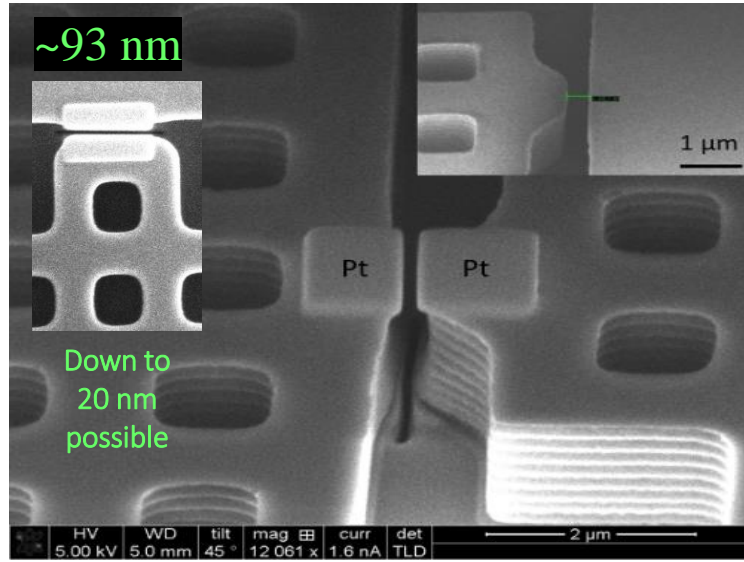
$$k z_{DC} = \frac{1}{2} \frac{\epsilon_0 A_{DC}}{(g_{DC} - z_{DC})^2} V_{DC}^2$$



2. Use RF to close the gap completely

$$F_{RF} = \frac{Q}{4} \frac{\epsilon_0 A_{RF}}{(g_{RF} - z_{DC})^2} V_{RF}^2 = k \alpha \sqrt{\frac{4k_B T Q}{k}}$$

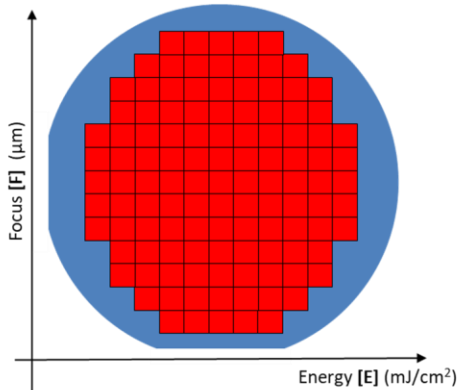
# Focused Ion Beam (FIB) for Gap Control



# Lithography Results: Data Preparation



**Spatial variation of focus and energy from ASML job file**

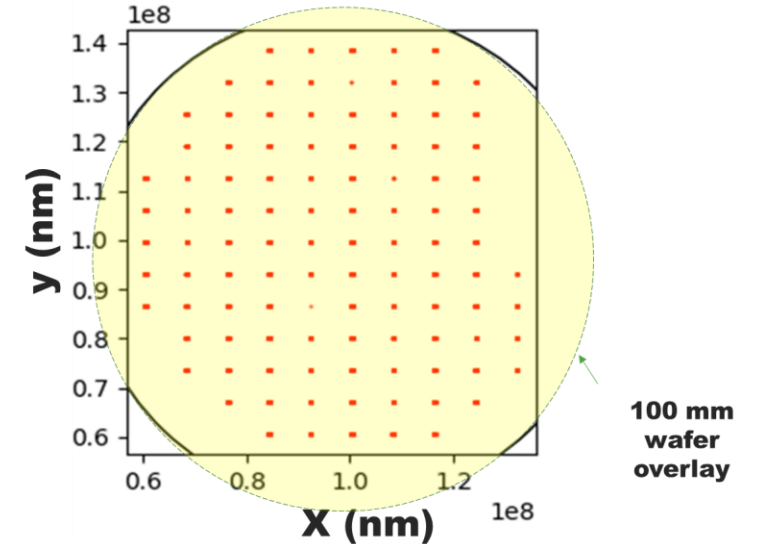


extracted from Hitachi meta data

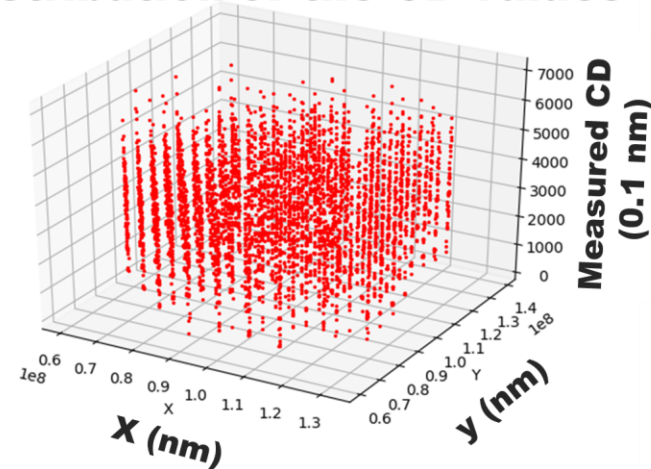


"msr" text file

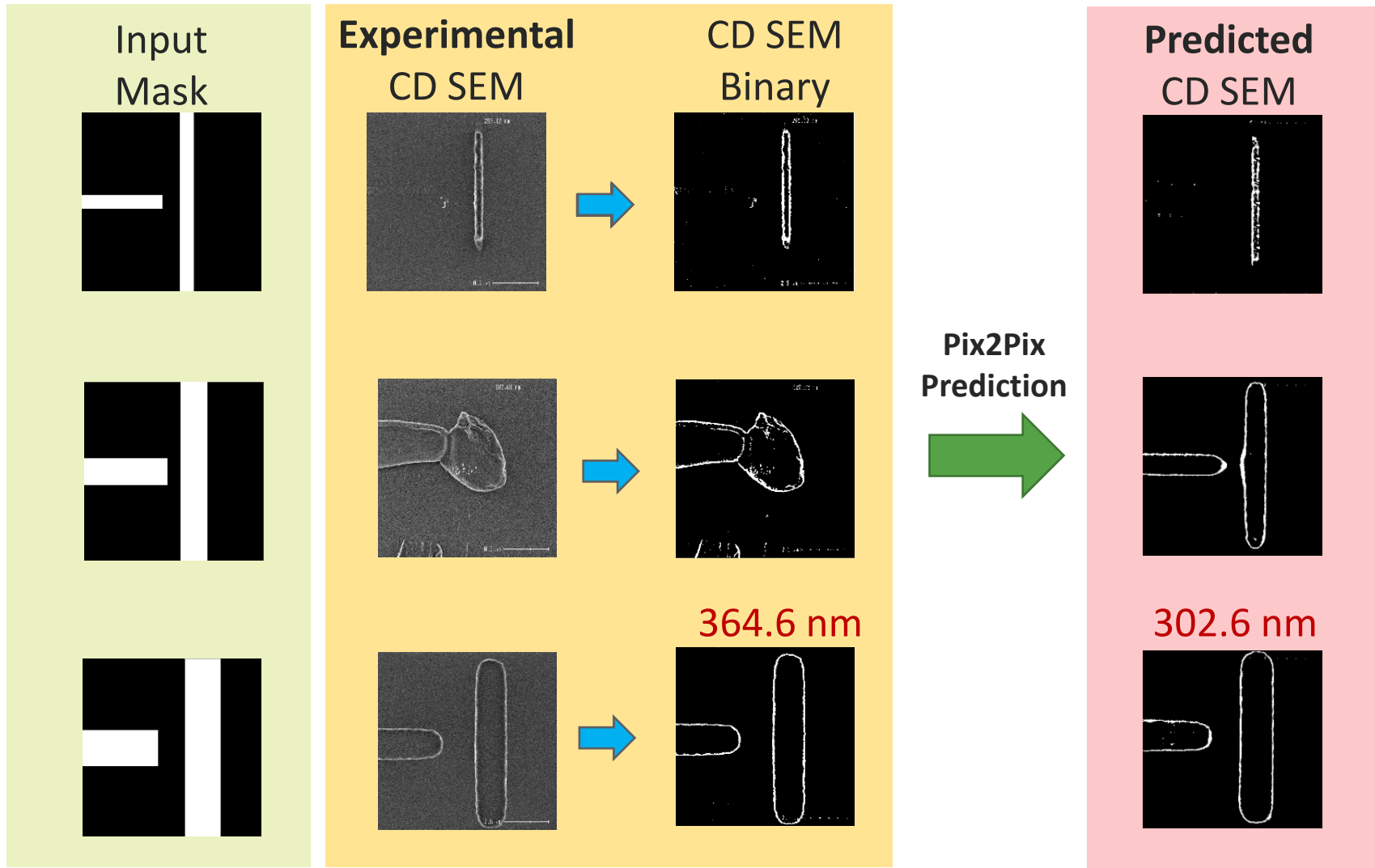
**Spatial variations of accepted CD measurements on wafer**



**Distribution of the CD values**



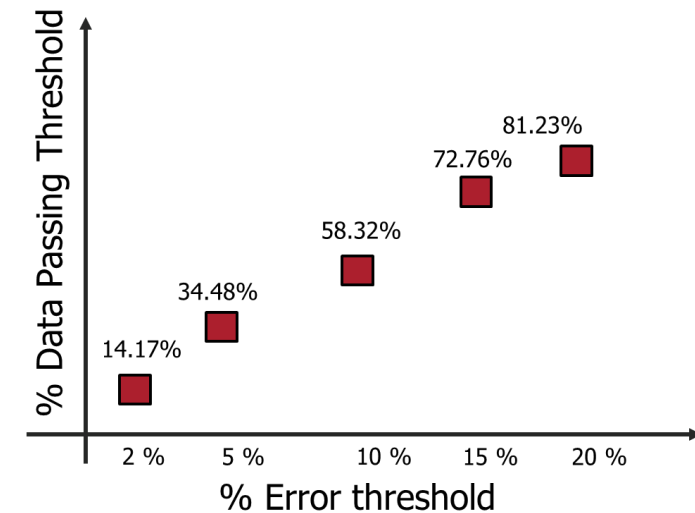
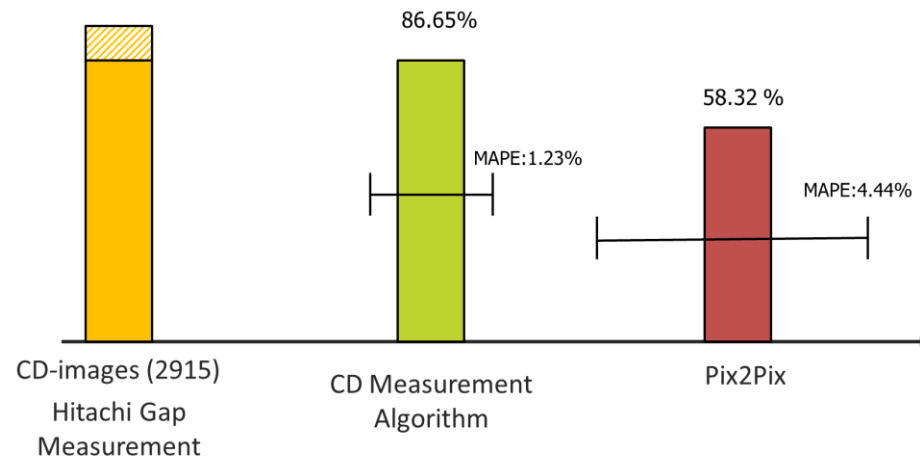
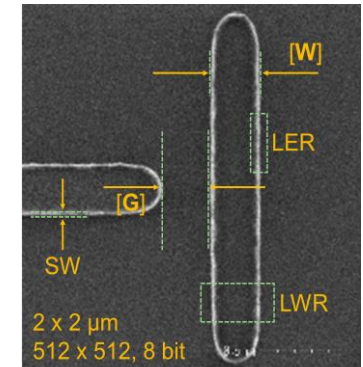
# Limitations of Pix2Pix



# Gap Prediction Performance Quantification

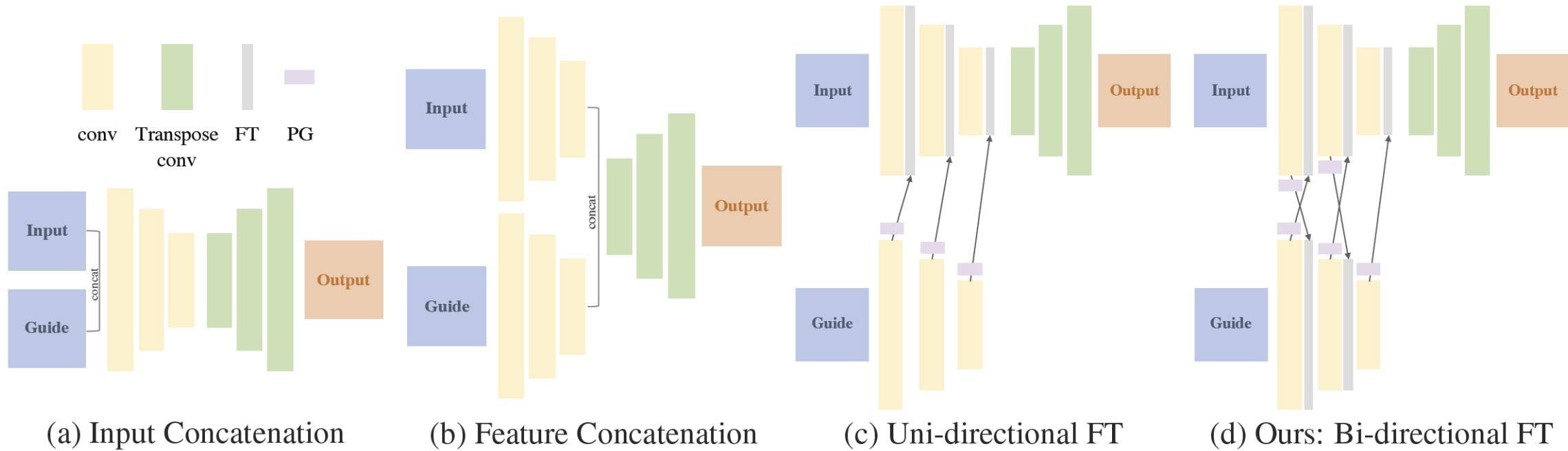


- For TGAP **predicted CD SEM from masks**, 58.32% out of 2915 images for which Hitachi gave a CD value have a percentage error smaller than 10%, and MAPE is 4.44%.
- For TGAP **experimental CD SEM from wafers**, 86.65% out of 2915 images for which Hitachi gave a CD value have a percentage error smaller than 10%, and MAPE is 1.23%.
- Algorithm parameters** (number of epochs and batch size) lead to +/- 5% change in performance.



MAPE : Mean Absolute Percentage Error

# Conditioning schemes for guiding image-2-image translation

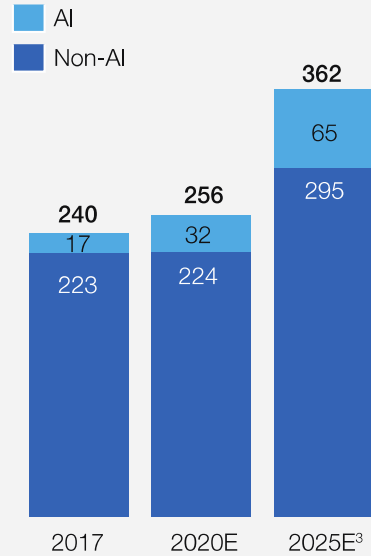


# Data & AI Projected impact on Semiconductor

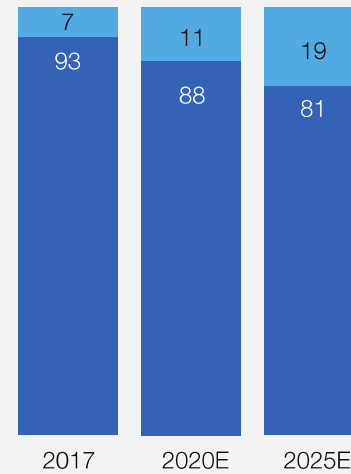


**Exhibit 3 Growth for semiconductors related to artificial intelligence (AI) is expected to be five times greater than growth in the remainder of the market.**

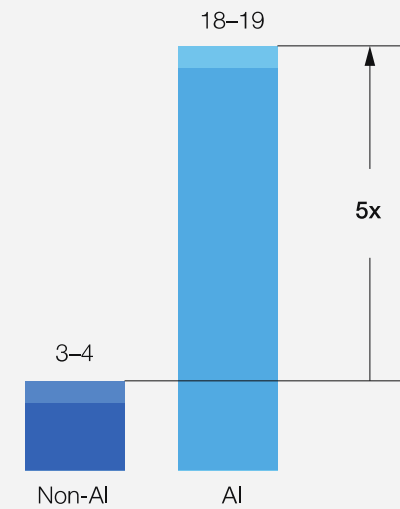
AI semiconductor total available market,<sup>1</sup> \$ billion



AI semiconductor total available market, %



Estimated AI semiconductor total available market CAGR,<sup>2</sup> 2017–25, %



<sup>1</sup>Total available market includes processors, memory, and storage; excludes discretely, optical, and micro-electrical-mechanical systems.

<sup>2</sup>Compound annual growth rate.

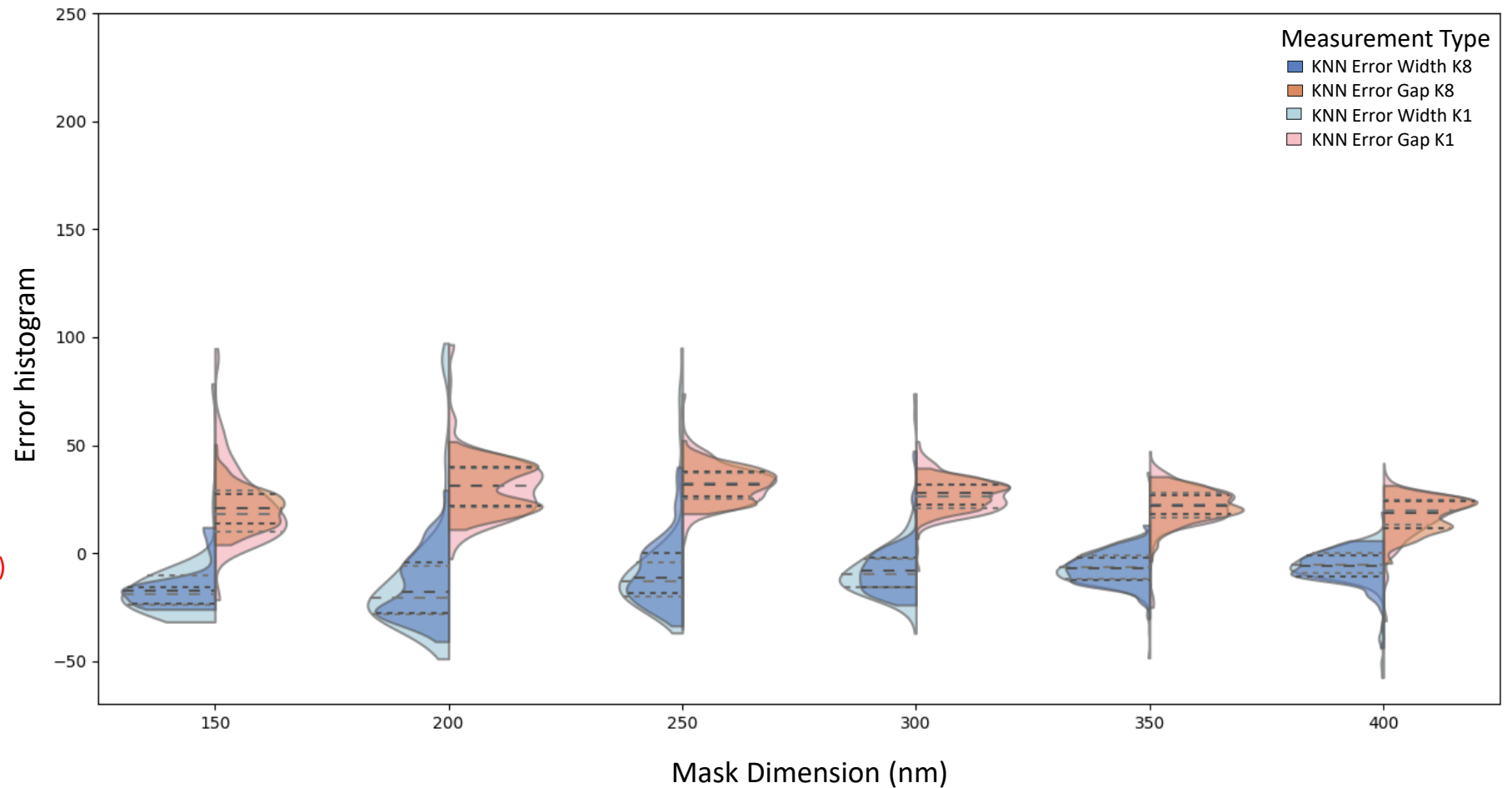
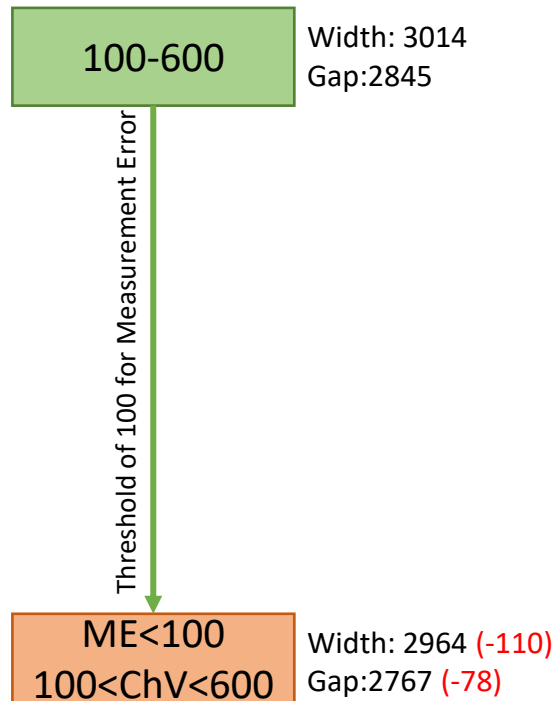
<sup>3</sup>E = estimated.

Source: Bernstein; Cisco Systems; Gartner; IC Insights; IHS Markit; Machina Research; McKinsey analysis

# KNN Performance per Feature Size

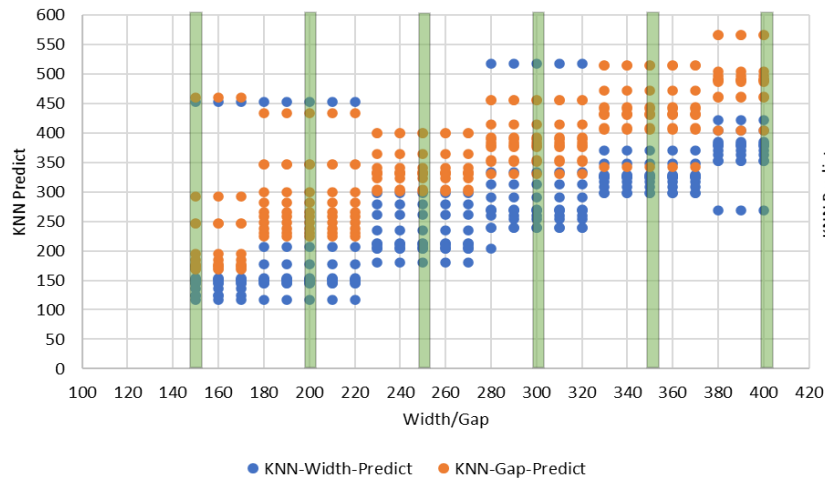


$$Error_{KNN} = \frac{(X_{Predict} - X_{Layout})}{X_{Layout}} \times 100$$

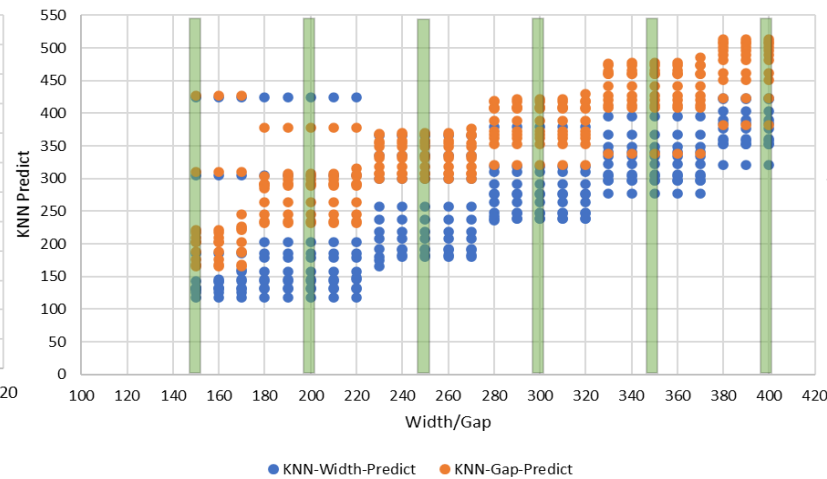




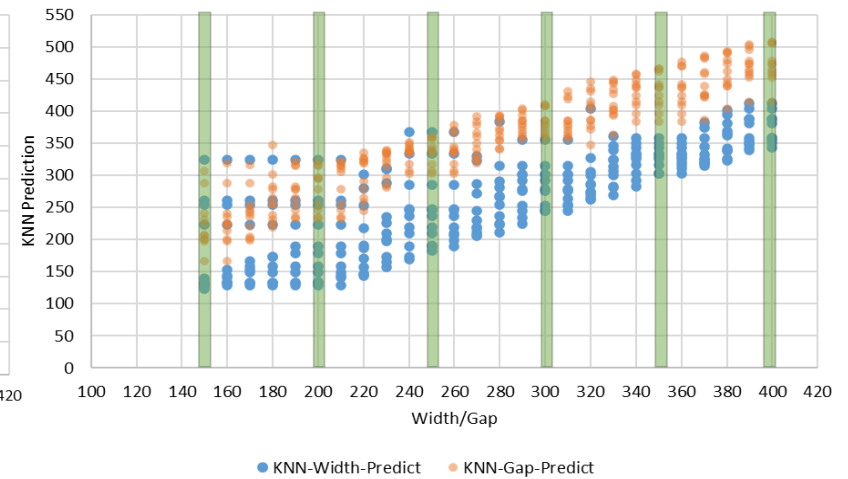
# KNN Model for width & gap Interpolation



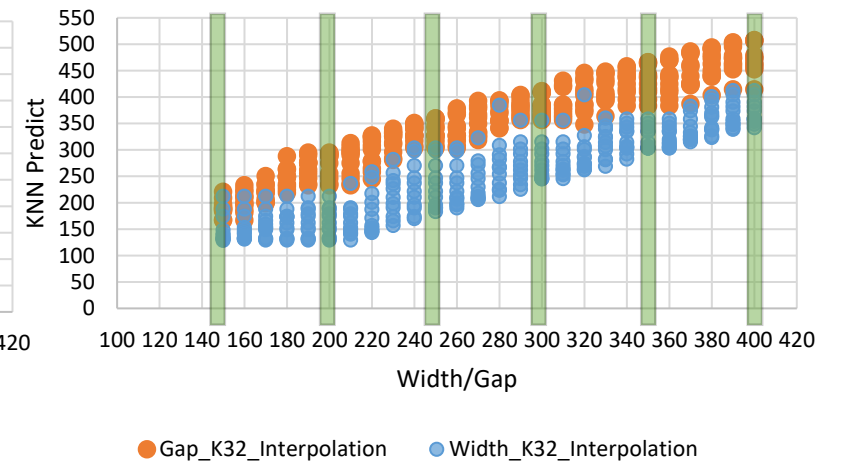
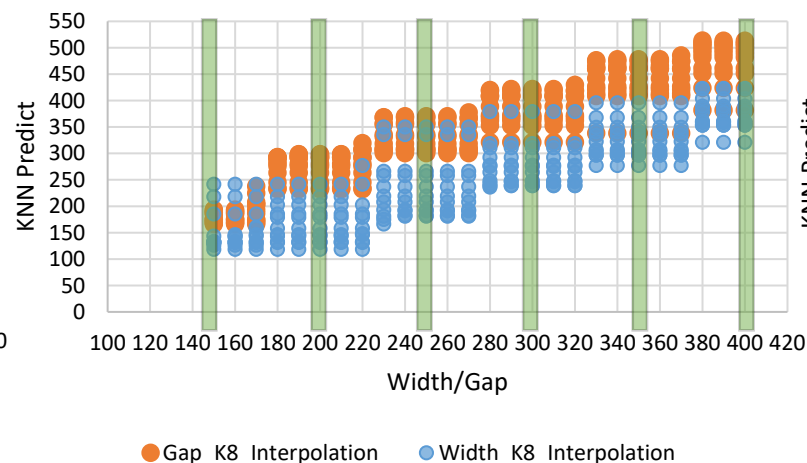
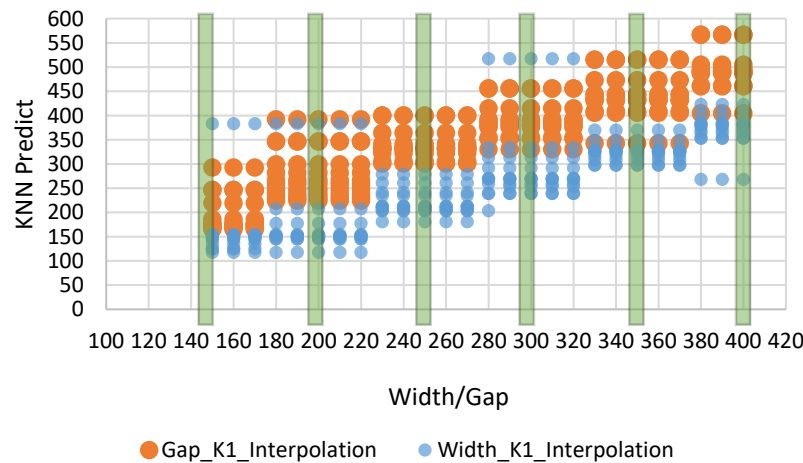
K=1



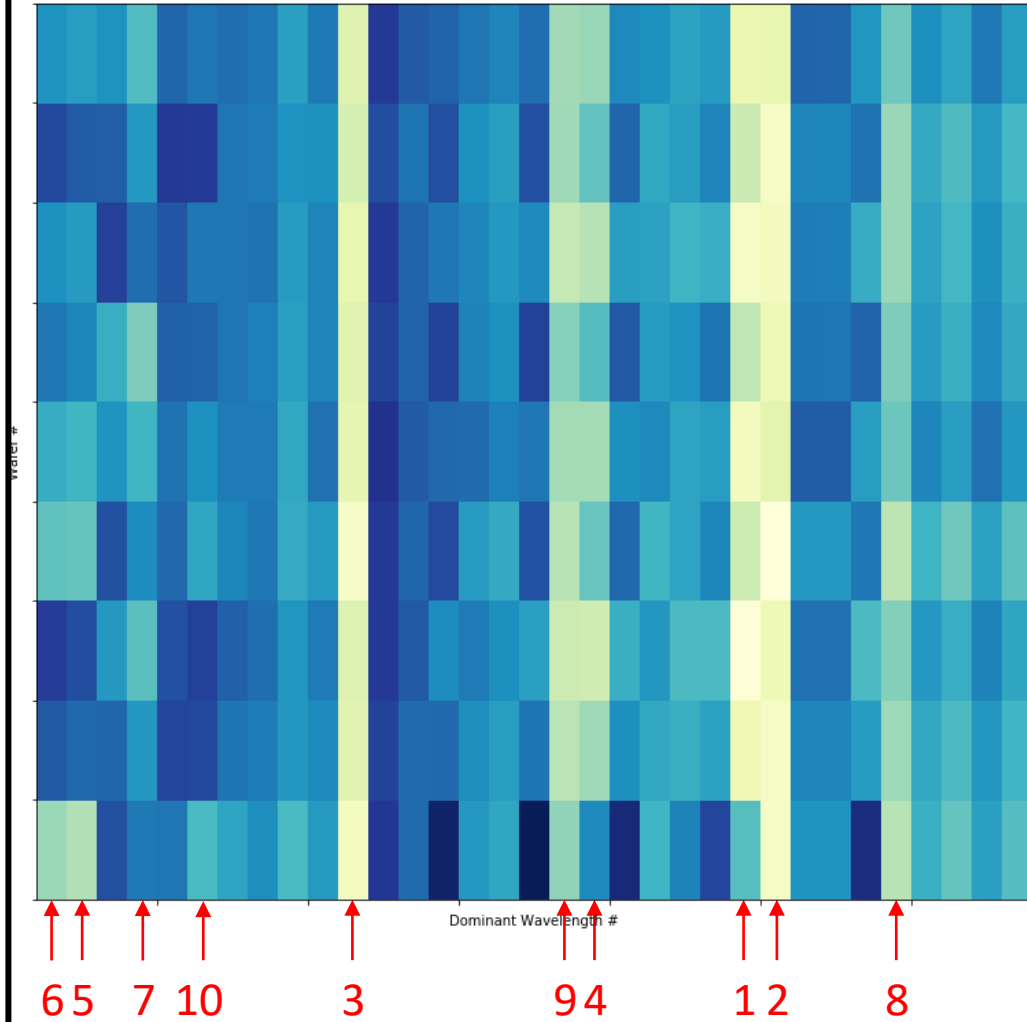
K=8



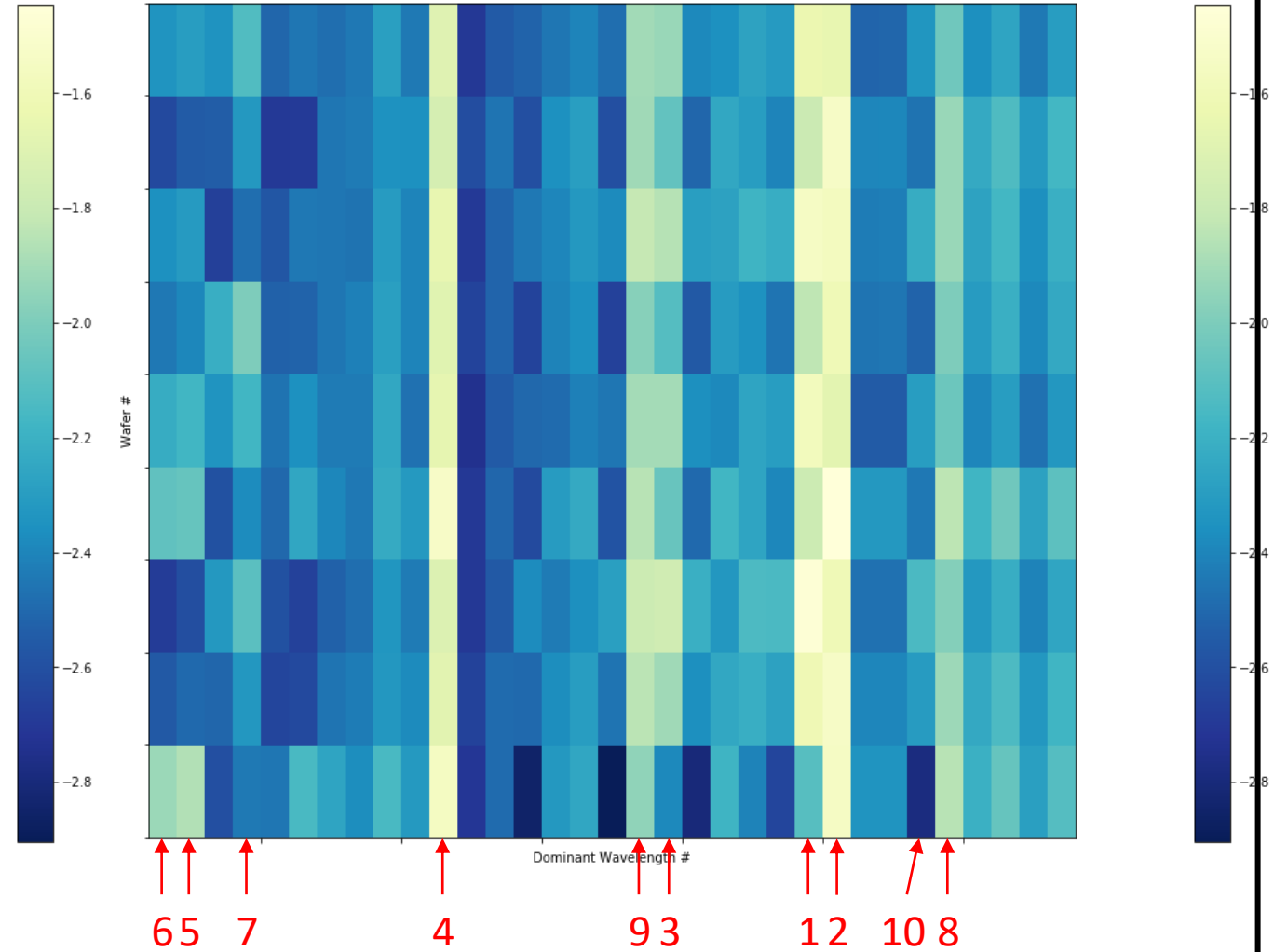
K=32



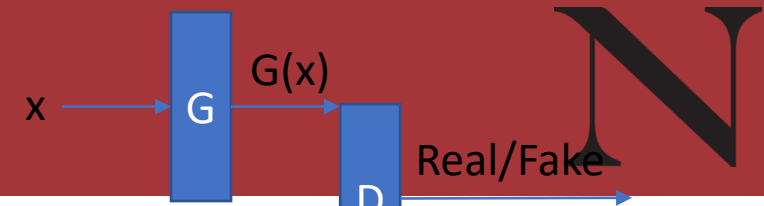
Time-Average Log Peaks for Different Wafers & Same Wavelengths (Normalized, Selected By Variance)



Time-Average Log Peaks for Different Wafers & Same Wavelengths (Normalized, Selected By MAD)

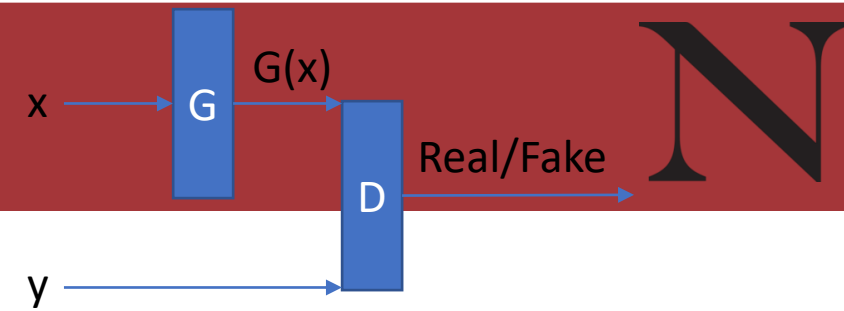


# GAN Evaluation Metrics

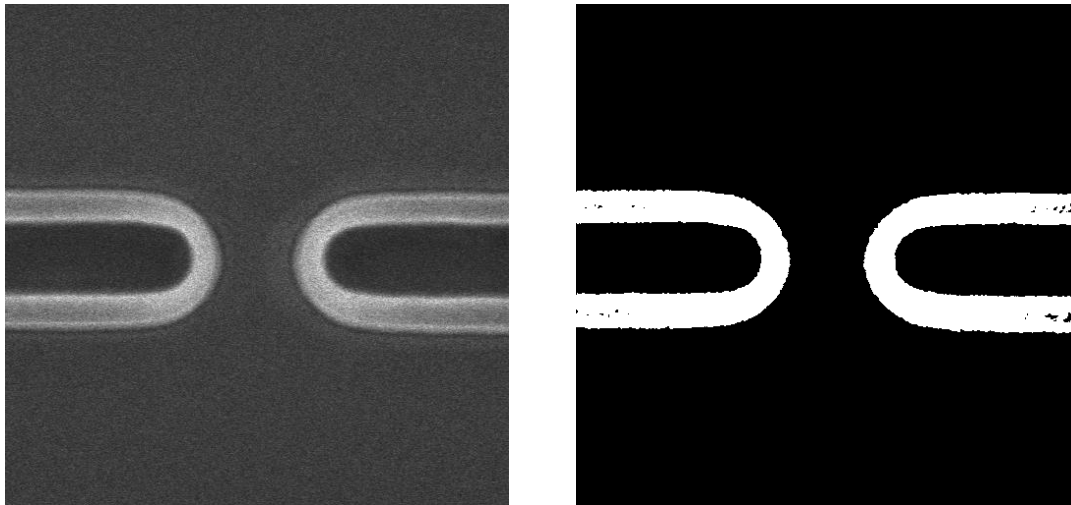


- **Goal:** for each input/output image pair  $(x,y)$ , quantitatively evaluate “how good” the fake output  $G(x)$  is – difficult in general.
- Several approaches taken in previous work:
  - **Segmentation-Based:** if  $x$  is a segmentation of  $y$ , compute segmentation of  $G(x)$  using FCN. Then, segmentation metrics indirectly evaluate generator performance (`pix2pix`, `mAP`).
  - **Frechet Inception Distance:** using pretrained CNN, retrieve output layer vectors for each  $y$  (placing in set  $Y$ ) and for each  $G(x)$  (in set  $X$ ). Compute Frechet distance between the resulting sets  $Y, X$  (`FID`).
  - **Human Perceptual Study:** allow individuals to select which of  $y, G(x)$  looks more natural in controlled study (`pix2pixHD`)
  - **Analyze L1 Loss:** take average (over all images) of the L1 distance between  $y, G(x)$ . Already able to do this, but distance is different from quality of fake.

# Segmentation-Based



- Let  $s$  be the segmentation of  $G(x)$  the fully connected network (FCN) gives.
- Compare **ground truth** ( $x$ ) and **prediction** ( $s$ ) using segmentation metrics, taking results as a pseudo-metric for quality of the generator.
- Idea: our  $x$  is not a segmentation of  $y$ , but binary segmentation of post-etch images ( $y$ ) is relatively easy via heuristic. Segment & compare  $y$ ,  $G(x)$ .



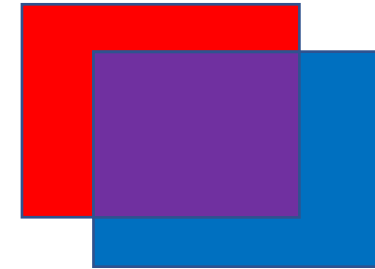
Heuristic (Otsu Thresholding & 3x3 Median Filter)

# Segmentation Metrics



- Compare set of predicted foreground to ground truth for single image.
- Average Precision (AP):
  - Assume that the final step of the segmentation algorithm is a simple threshold.
  - For a set of n thresholds between min and max graylevels, evaluate the precision and recall we get for each (cf. precision-recall curves).
  - $$AP = \sum_{k=1}^n (Recall_k - Recall_{k-1}) \cdot Precision_k$$
- Take the mean over all images for a score with any of these metrics (**mAP**, mIoU, ... )

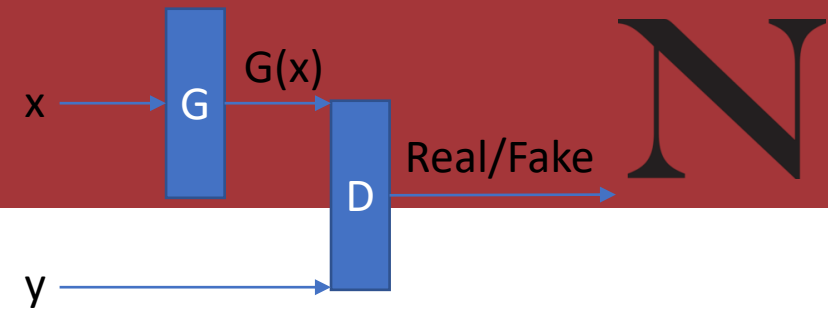
True Foreground (A)



Predicted Foreground (B)

- $IoU = \frac{A \cap B}{A \cup B}$
- $TP = |A \cap B|$
- $TN = |A^C \cap B^C|$
- $FP = |A^C \cap B|$
- $FN = |A \cap B^C|$
- $Accuracy = \frac{TP+TN}{TP+TN+FP+FN}$
- $Precision = \frac{TP}{TP+FP}$
- $Recall = \frac{TP}{TP+FN}$

# Frechet Inception Distance



- Load **InceptionV3** classification network, pre-trained on the ImageNet dataset (or possibly another CNN).
- Form sets  $\mathbf{X} = \{\text{set of Inception v3 output activation vectors for each } G(x)\}$ ,  $\mathbf{Y} = \{\text{set of Inception v3 output activation vectors for each } y\}$ .
- Compute Frechet Distance between  $\mathbf{X}$  and  $\mathbf{Y}$ :

$$d^2 = \|\mu_X - \mu_Y\|^2 + \text{tr}(C_X + C_Y - 2(C_X C_Y)^{1/2})$$

- Where  $\mu_S, C_S$  are the sample mean and covariance of a set  $S$ .
- Lower FID indicates that sets  $X, Y$  are more similar, and thus that our generator produces better fakes.